



# HeuristicLab

A Paradigm-Independent and Extensible  
Environment for Heuristic Optimization

# Algorithm and Experiment Design with HeuristicLab

An Open Source Optimization Environment for  
Research and Education

S. Wagner, G. Kronberger

Heuristic and Evolutionary Algorithms Laboratory (HEAL)

School of Informatics/Communications/Media, Campus Hagenberg

University of Applied Sciences Upper Austria



**HEAL**

Heuristic and Evolutionary  
Algorithms Laboratory



Josef Ressel-Zentrum

**HEUREKA!**

# Instructor Biographies

- Stefan Wagner
  - Full professor for complex software systems (since 2009)  
University of Applied Sciences Upper Austria
  - Co-founder of the HEAL research group
  - Project manager and chief architect of HeuristicLab
  - PhD in technical sciences (2009)  
Johannes Kepler University Linz, Austria
  - Associate professor (2005 – 2009)  
University of Applied Sciences Upper Austria
  - <http://heal.heuristiclab.com/team/wagner>
- Gabriel Kronberger
  - Full professor for business intelligence (since 2011)  
University of Applied Sciences Upper Austria
  - Member of the HEAL research group
  - Architect of HeuristicLab
  - PhD in technical sciences (2010)  
Johannes Kepler University Linz, Austria
  - Research assistant (2005 – 2011)  
University of Applied Sciences Upper Austria
  - <http://heal.heuristiclab.com/team/kronberger>



# Agenda



- Objectives of the Tutorial
- Introduction
- Where to get HeuristicLab?
- Plugin Infrastructure
- Graphical User Interface
- Available Algorithms & Problems
  
- **Demonstration Part I: Working with HeuristicLab**
- **Demonstration Part II: Data-based Modeling**
  
- Some Additional Features
- Planned Features
- Team
- Suggested Readings
- Bibliography
- Questions & Answers

# Objectives of the Tutorial

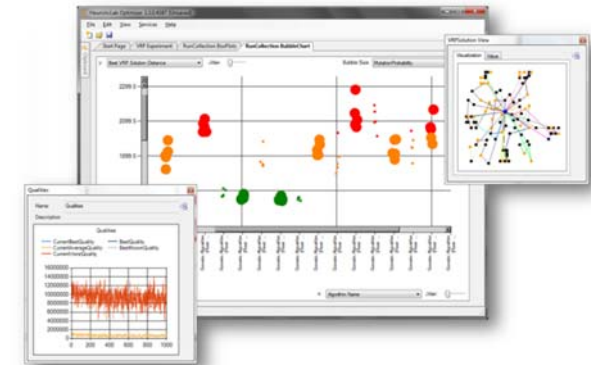


- Introduce general motivation and design principles of HeuristicLab
- Show where to get HeuristicLab
- Explain basic GUI usability concepts
- Demonstrate basic features
- Demonstrate editing and analysis of optimization experiments
- Demonstrate custom algorithms and graphical algorithm designer
- Demonstrate data-based modeling features
- Outline some additional features

# Introduction



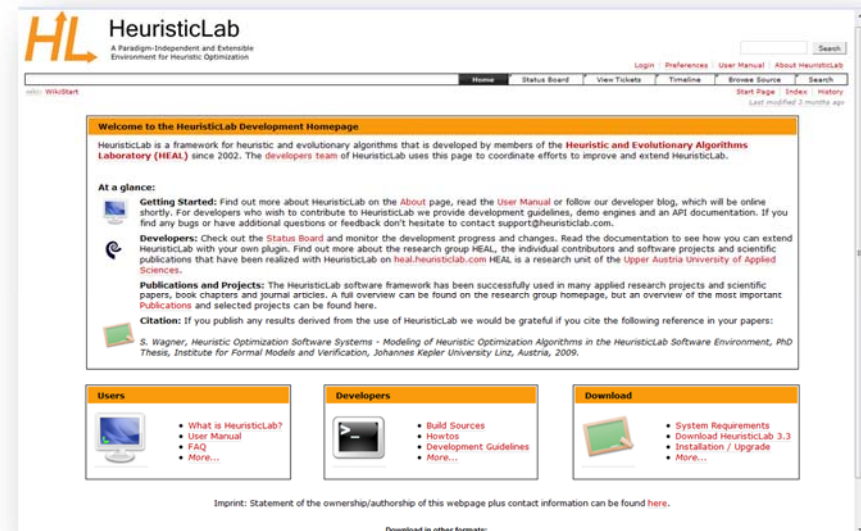
- Motivation and Goals
  - graphical user interface
  - paradigm independence
  - multiple algorithms and problems
  - large scale experiments and analyses
  - parallelization
  - extensibility, flexibility and reusability
  - visual and interactive algorithm development
  - multiple layers of abstraction
- Facts
  - development of HeuristicLab started in 2002
  - based on Microsoft .NET and C#
  - used in research and education
  - second place at the *Microsoft Innovation Award 2009*
  - open source (GNU General Public License)
  - version 3.3.0 released on May 18th, 2010
  - latest version 3.3.7 released on July 8th, 2012



# Where to get HeuristicLab?



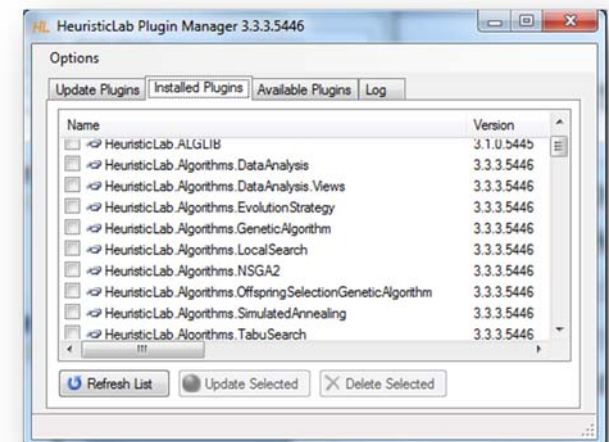
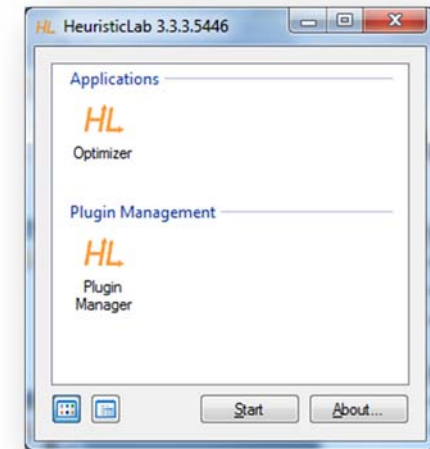
- Download binaries
  - deployed as ZIP archives
  - latest stable version 3.3.7
    - released on July 8th, 2012
  - daily trunk builds
  - <http://dev.heuristiclab.com/download>
- Check out sources
  - SVN repository
  - HeuristicLab 3.3.7 tag
    - <http://dev.heuristiclab.com/svn/hl/core/tags/3.3.7>
  - current development trunk
    - <http://dev.heuristiclab.com/svn/hl/core/trunk>
- License
  - GNU General Public License (Version 3)
- System requirements
  - Microsoft .NET Framework 4.0 Full Version
  - enough RAM and CPU power ;-)



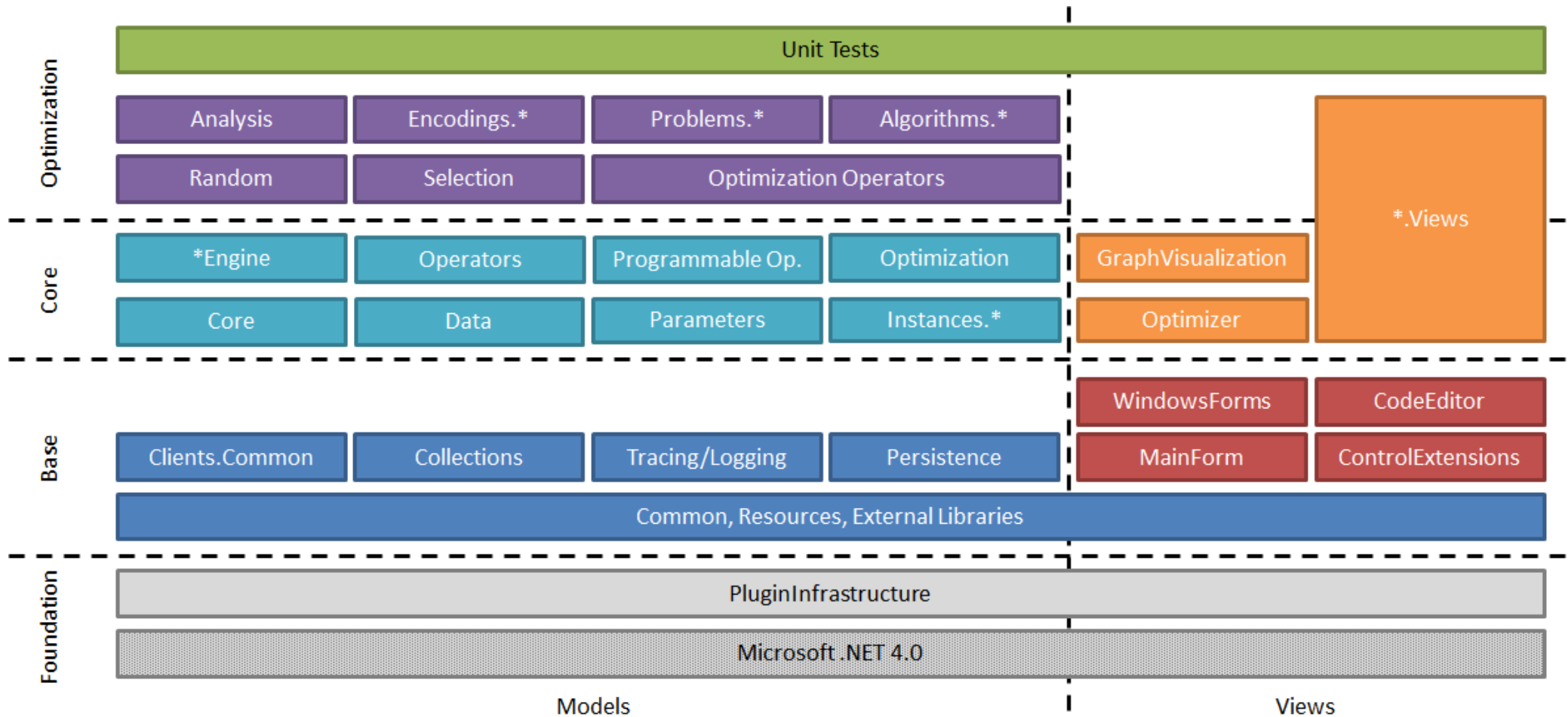
# Plugin Infrastructure



- HeuristicLab consists of many assemblies
  - 119 plugins in HeuristicLab 3.3.7
  - plugins can be loaded or unloaded at runtime
  - plugins can be updated via internet
  - application plugins provide GUI frontends
- Extensibility
  - developing and deploying new plugins is easy
  - dependencies are explicitly defined, automatically checked and resolved
  - automatic discovery of interface implementations (service locator pattern)
- Plugin Manager
  - GUI to check, install, update or delete plugins



# Plugin Architecture

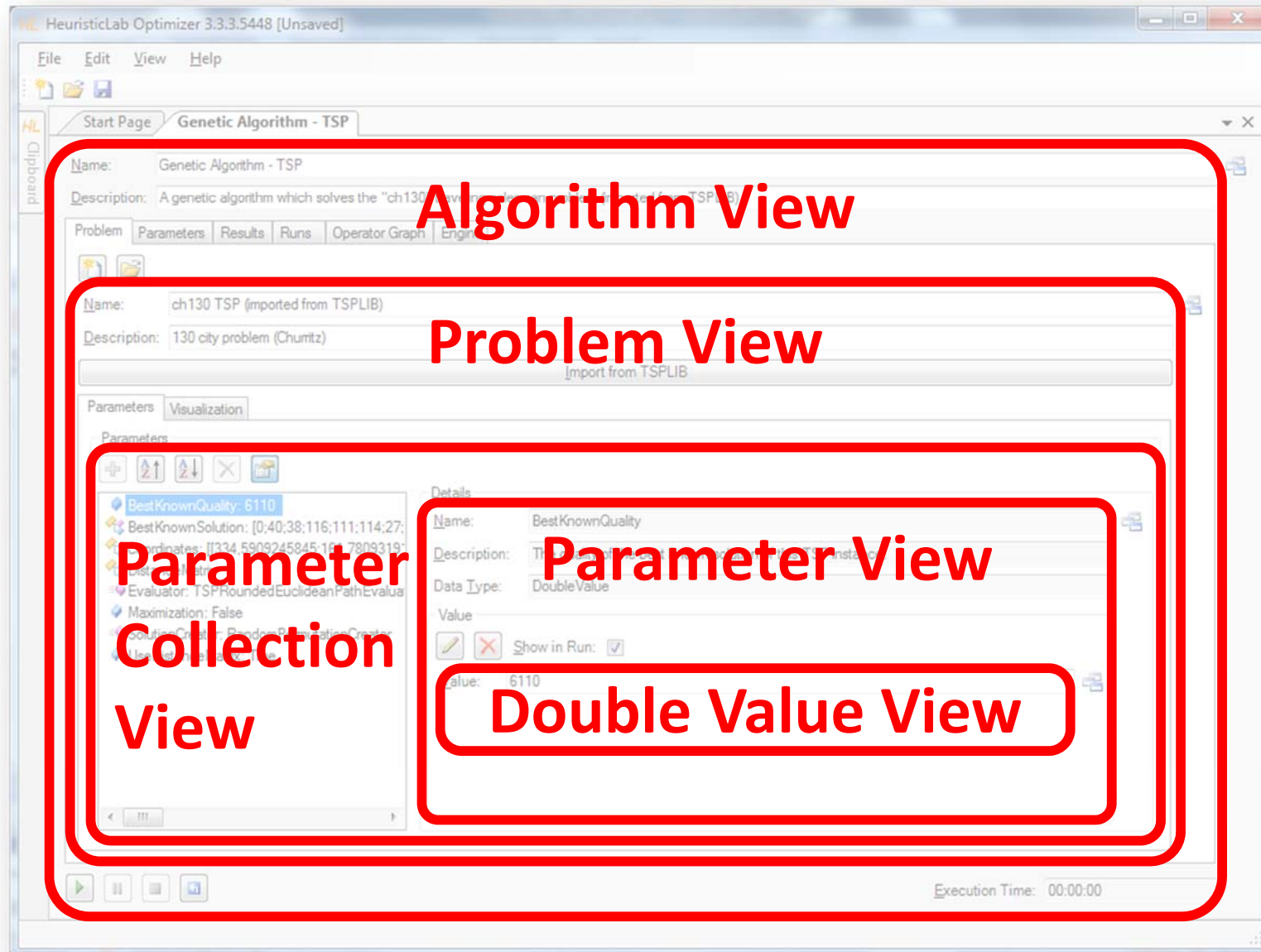




# Graphical User Interface

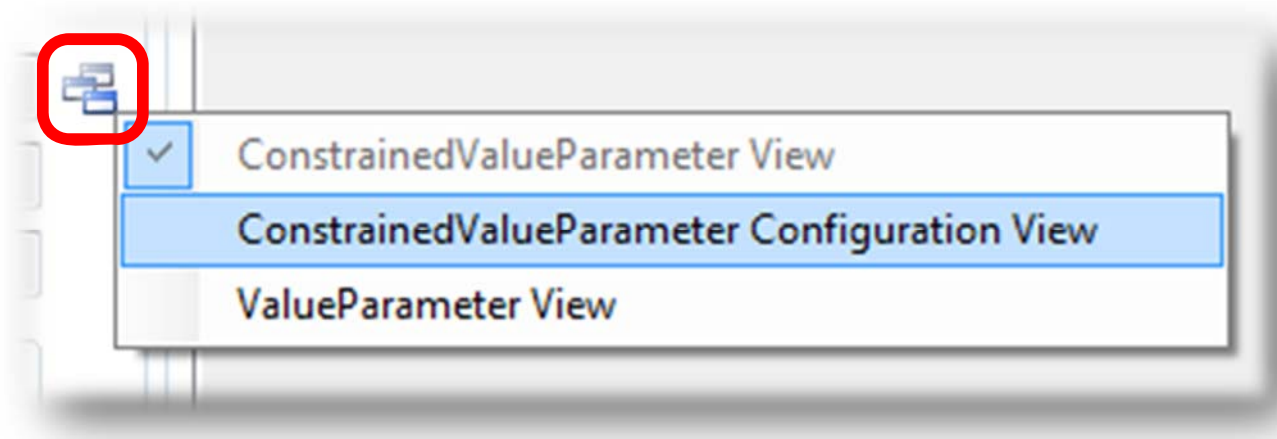
- HeuristicLab GUI is made up of views
  - views are visual representations of content objects
  - views are composed in the same way as their content
  - views and content objects are loosely coupled
  - multiple different views may exist for the same content
  
- Drag & Drop
  - views support drag & drop operations
  - content objects can be copied or moved (shift key)
  - enabled for collection items and content objects

# Graphical User Interface



# Graphical User Interface

- ViewHost
  - control which hosts views
  - right-click on windows icon to switch views
  - double-click on windows icon to open another view
  - drag & drop windows icon to copy contents



# Available Algorithms & Problems



## Algorithms

- Evolution Strategy
- Genetic Algorithm
- Genetic Programming
- Hungarian Algorithm
- Island Genetic Algorithm
- Island Offspring Selection Genetic Algorithm
- Local Search
- NSGA-II
- Offspring Selection Genetic Algorithm
- Particle Swarm Optimization
- Robust Taboo Search
- SASEGASA
- Simulated Annealing
- Tabu Search
- User-defined Algorithm
- Variable Neighborhood Search
- Performance Benchmarks
- Cross Validation
- k-Means
- Linear Discriminant Analysis
- Linear Regression
- Multinomial Logit Classification
- Nearest Neighbor Regression and Classification
- Neural Network Regression and Classification
- Random Forest Regression and Classification
- Support Vector Regression and Classification

## Problems

- Artificial Ant
- Classification
- Clustering
- External Evaluation Problem
- Knapsack
- Lawn Mower
- Linear Assignment
- OneMax
- Quadratic Assignment
- Regression
- Single-Objective Test Function
- Symbolic Classification
- Symbolic Regression
- Traveling Salesman
- User-defined Problem
- Vehicle Routing

# Agenda

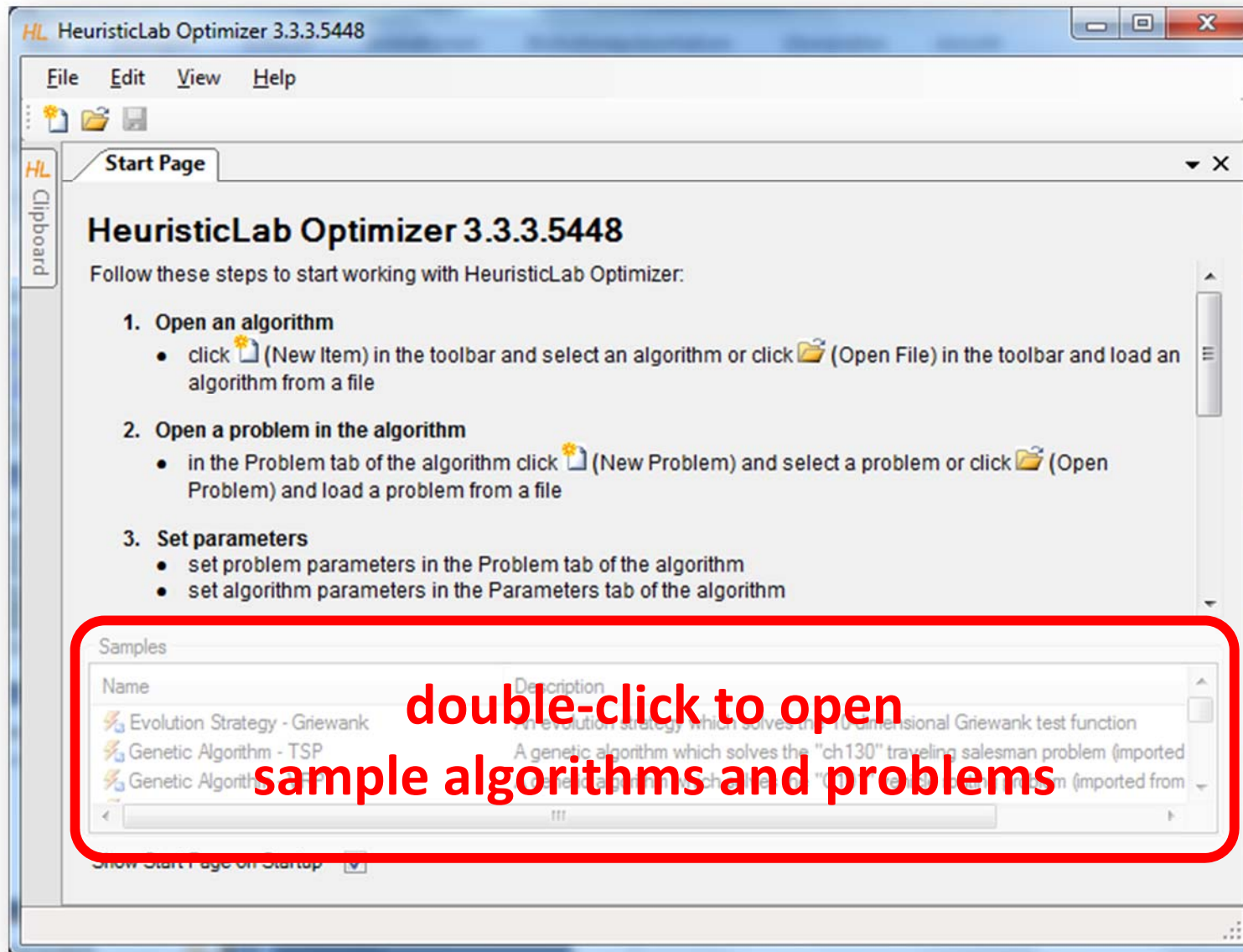


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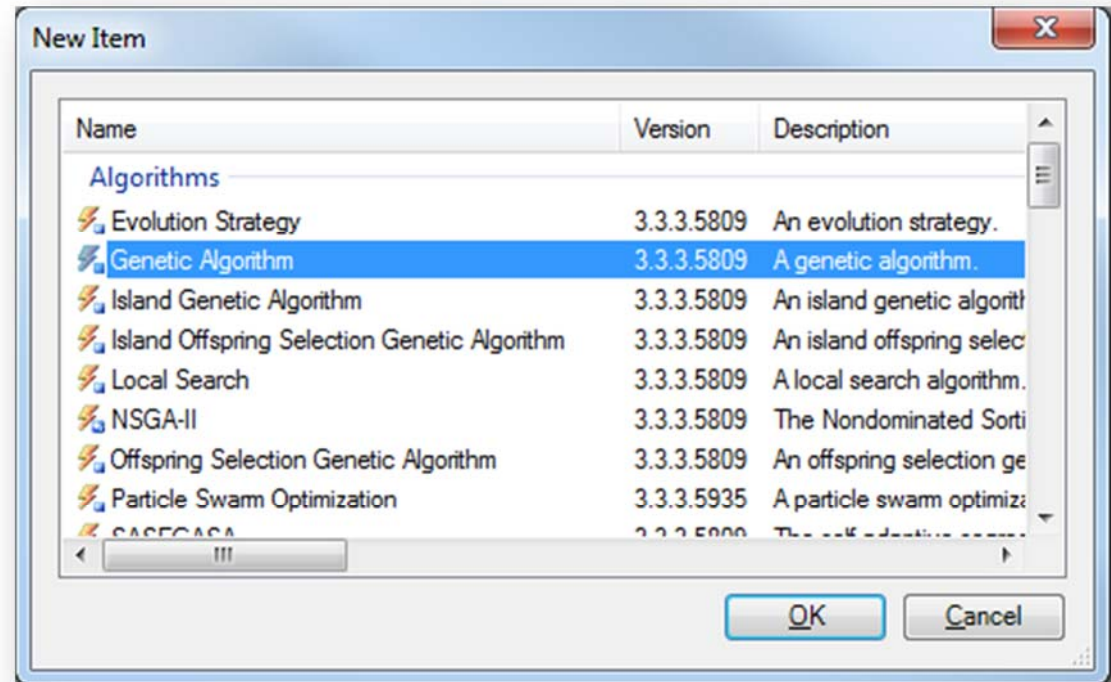
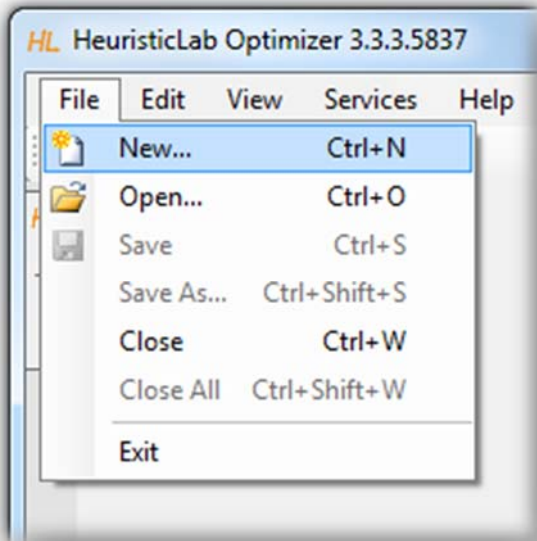
# Demonstration Part I: Working with HeuristicLab

- Create, Parameterize and Execute Algorithms
- Save and Load Items
- Create Batch Runs and Experiments
- Multi-core CPUs and Parallelization
- Analyze Runs
- Analyzers
- Building User-Defined Algorithms

# HeuristicLab Optimizer

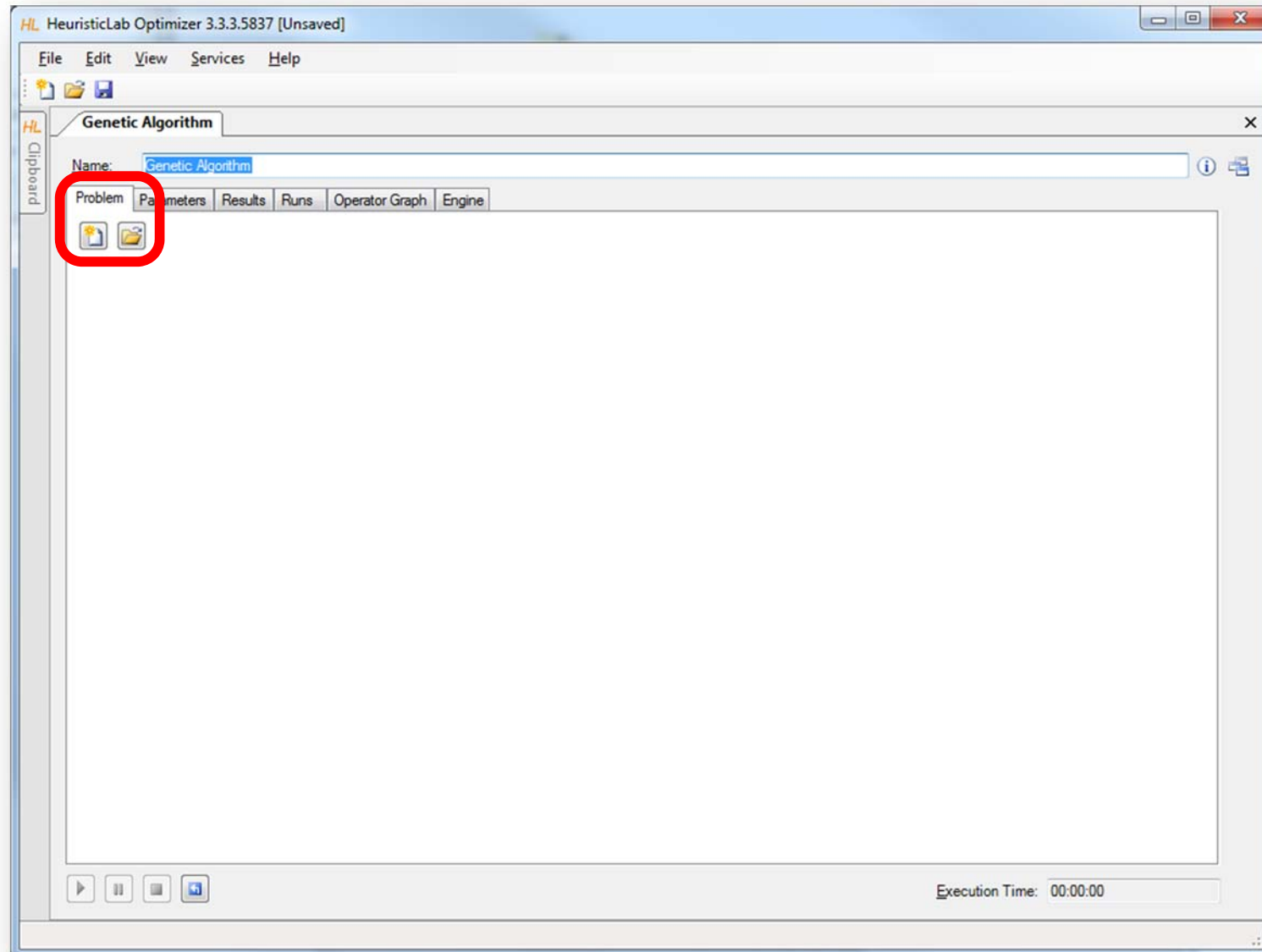


# Create Algorithm

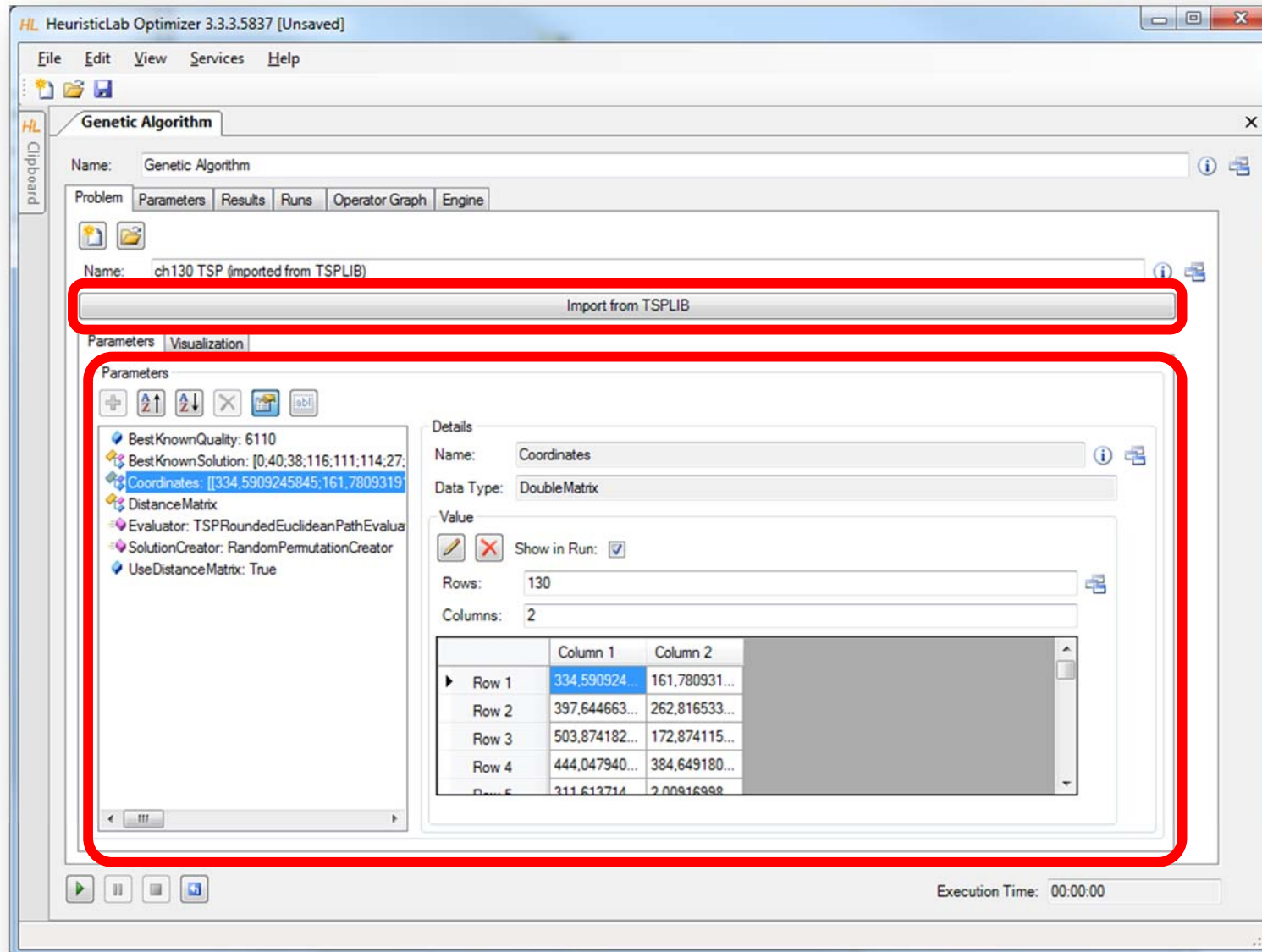




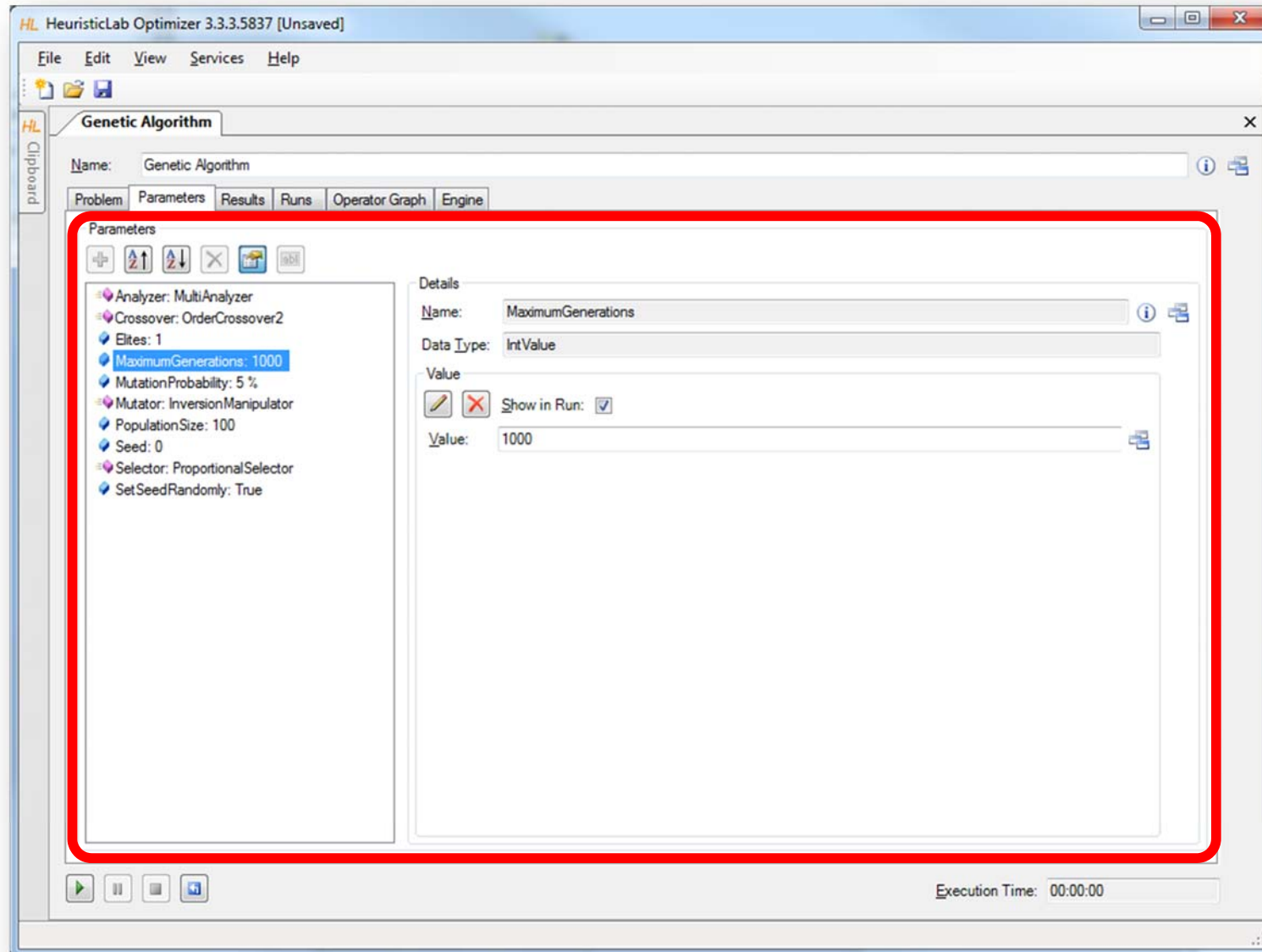
# Create or Load Problem



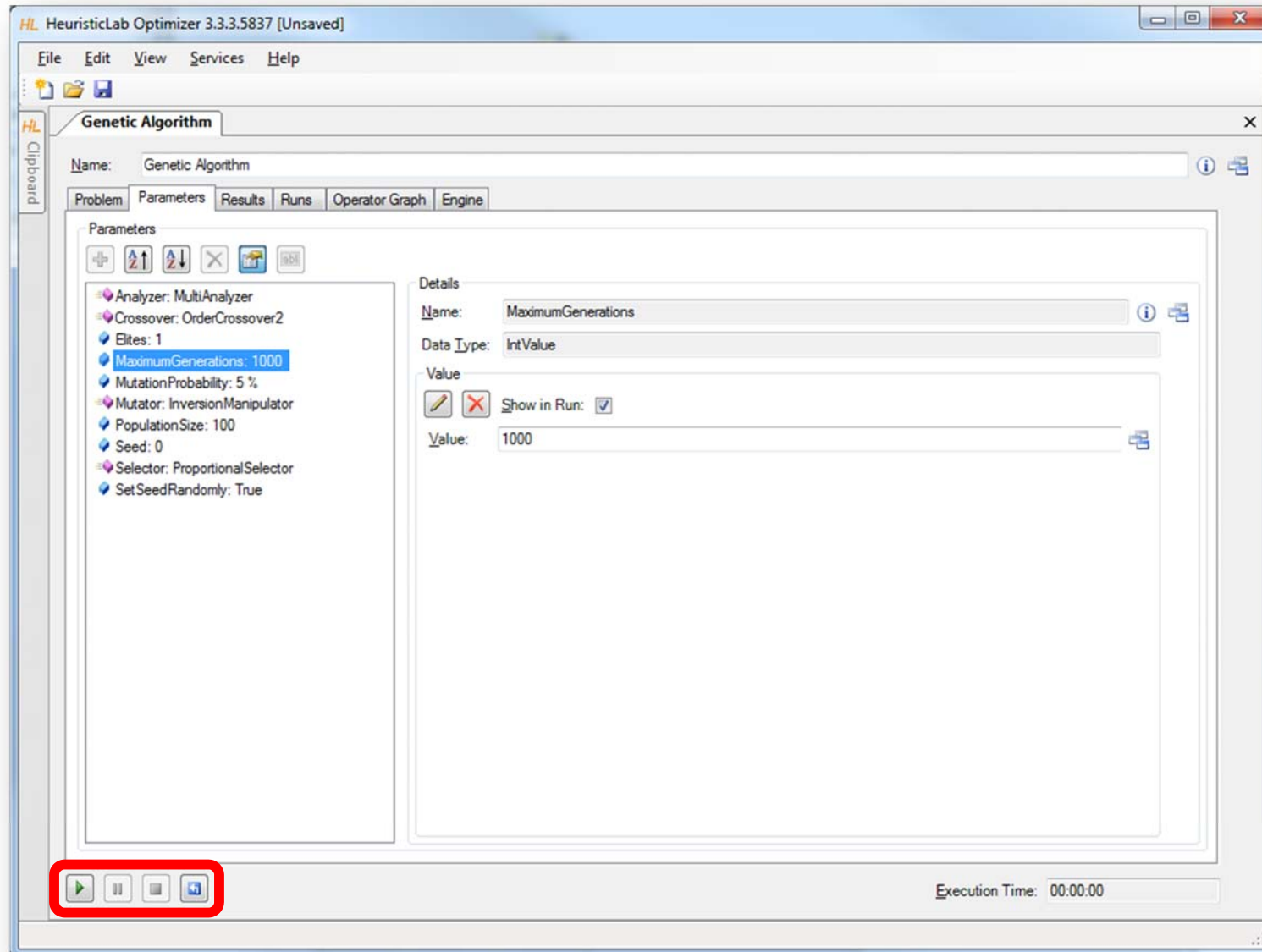
# Import or Parameterize Problem Data



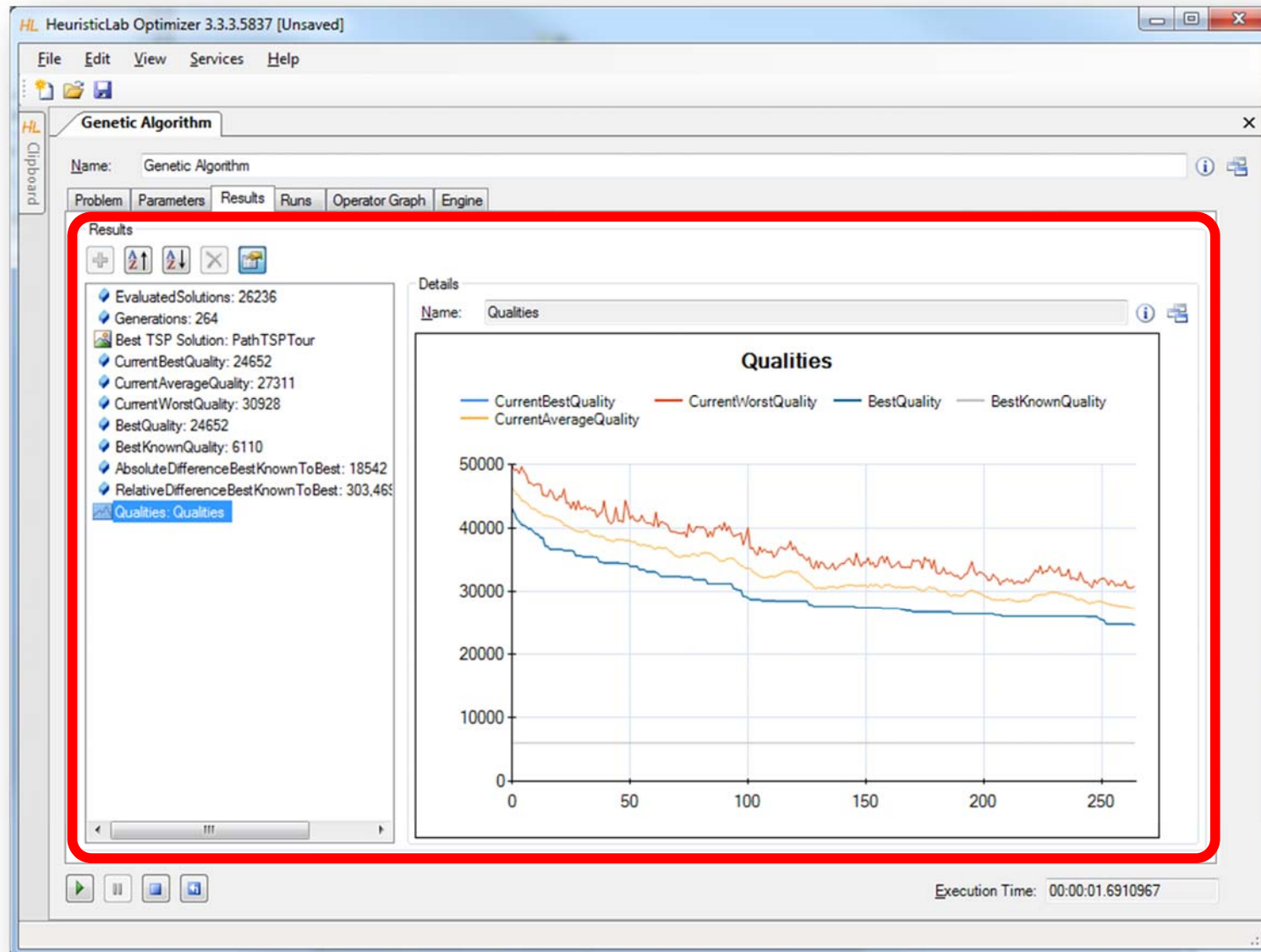
# Parameterize Algorithm



# Start, Pause, Resume, Stop and Reset

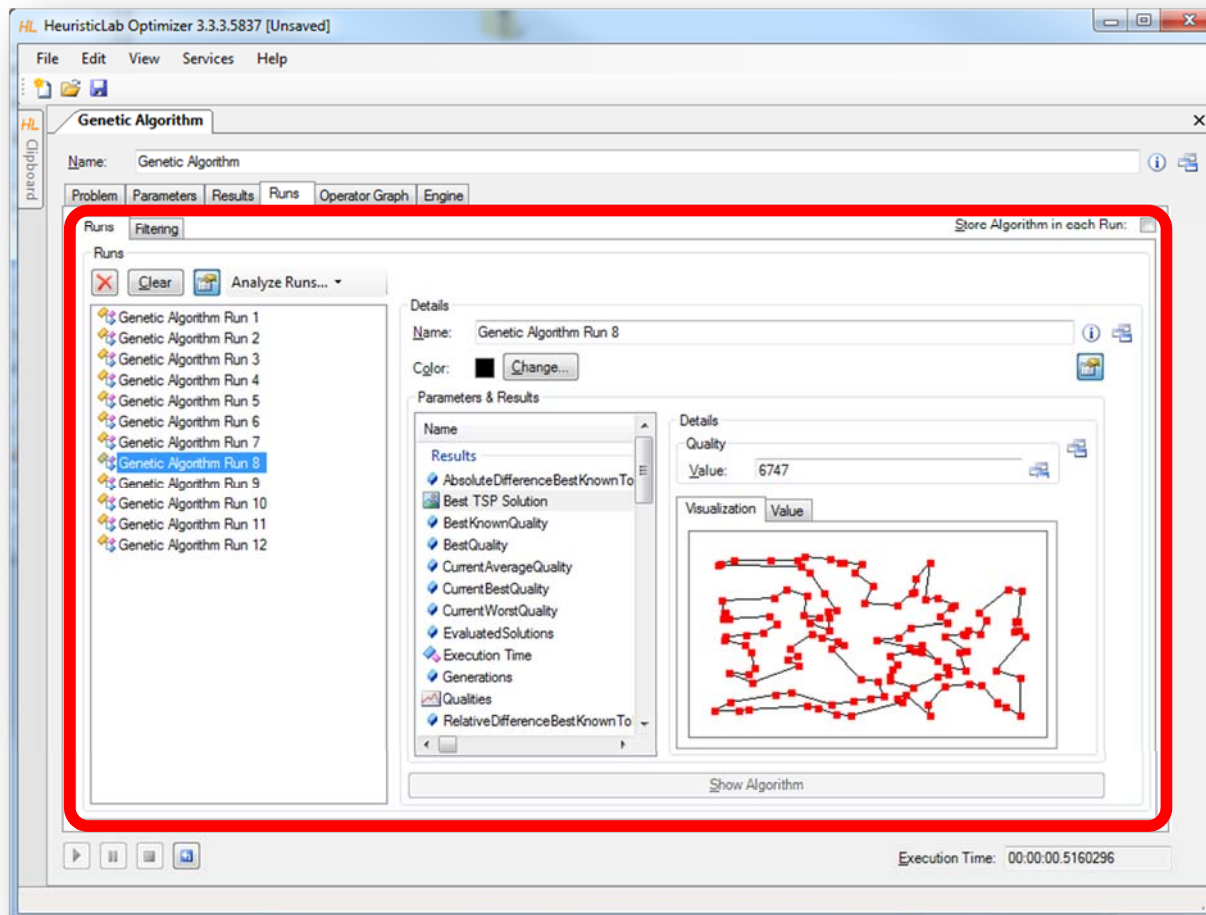


# Inspect Results



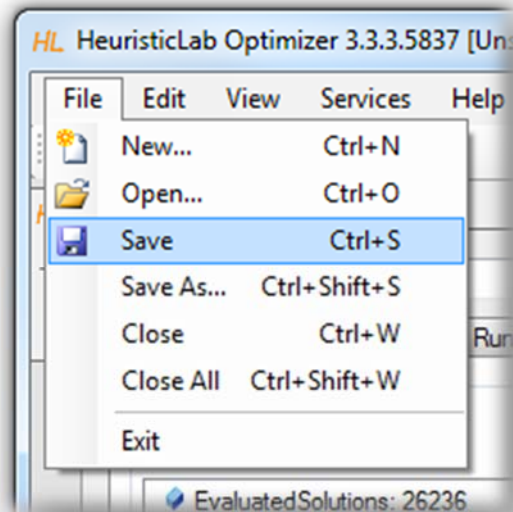
# Compare Runs

- A run is created each time when the algorithm is stopped
  - runs contain all results and parameter settings
  - previous results are not forgotten and can be compared



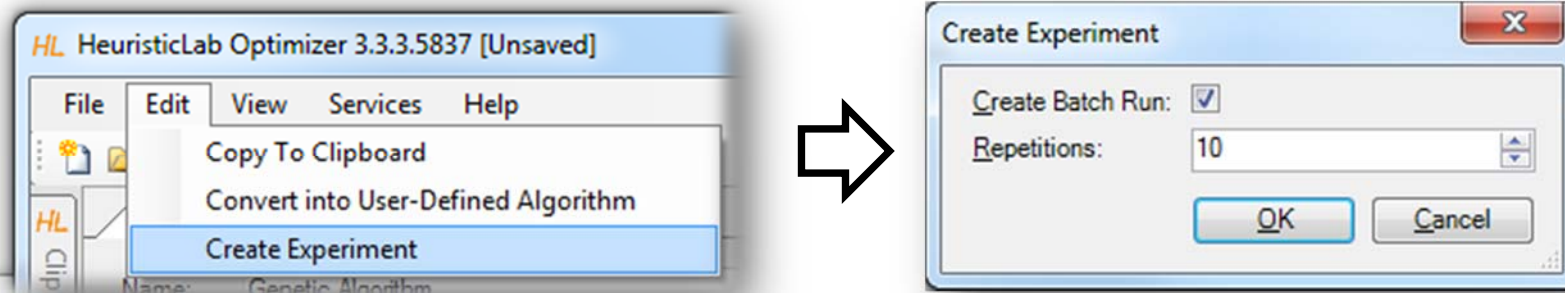
# Save and Load

- Save to and load from disk
  - HeuristicLab items (i.e., algorithms, problems, experiments, ...) can be saved to and loaded from a file
  - algorithms can be paused, saved, loaded and resumed
  - data format is custom compressed XML
  - saving and loading files might take several minutes
  - saving and loading large experiments requires some memory



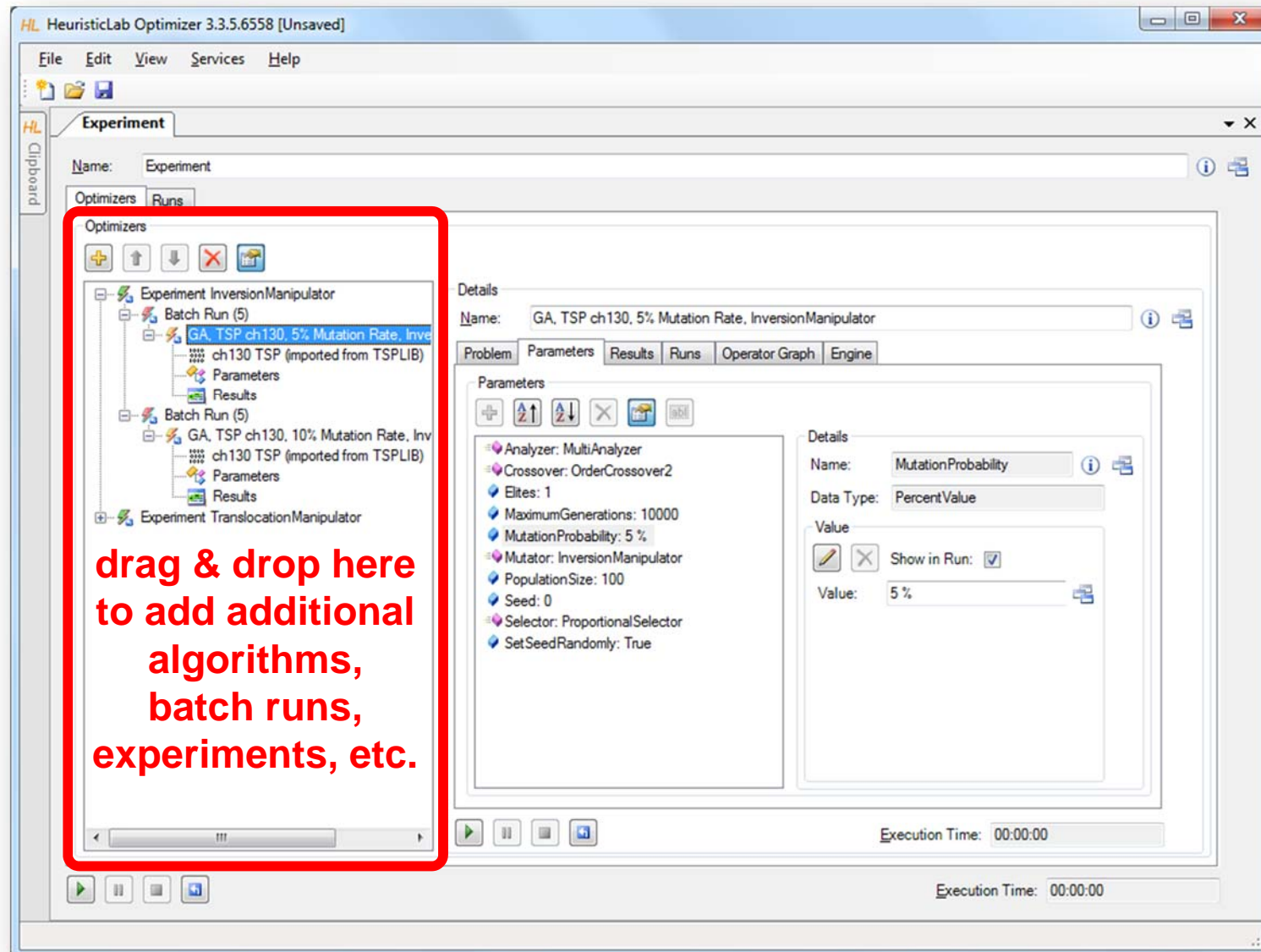
# Create Batch Runs and Experiments

- Batch runs
  - execute the same optimizer (e.g. algorithm, batch run, experiment) several times
- Experiments
  - execute different optimizers
  - suitable for large scale algorithm comparison and analysis
- Experiments and batch runs can be nested
- Generated runs can be compared afterwards

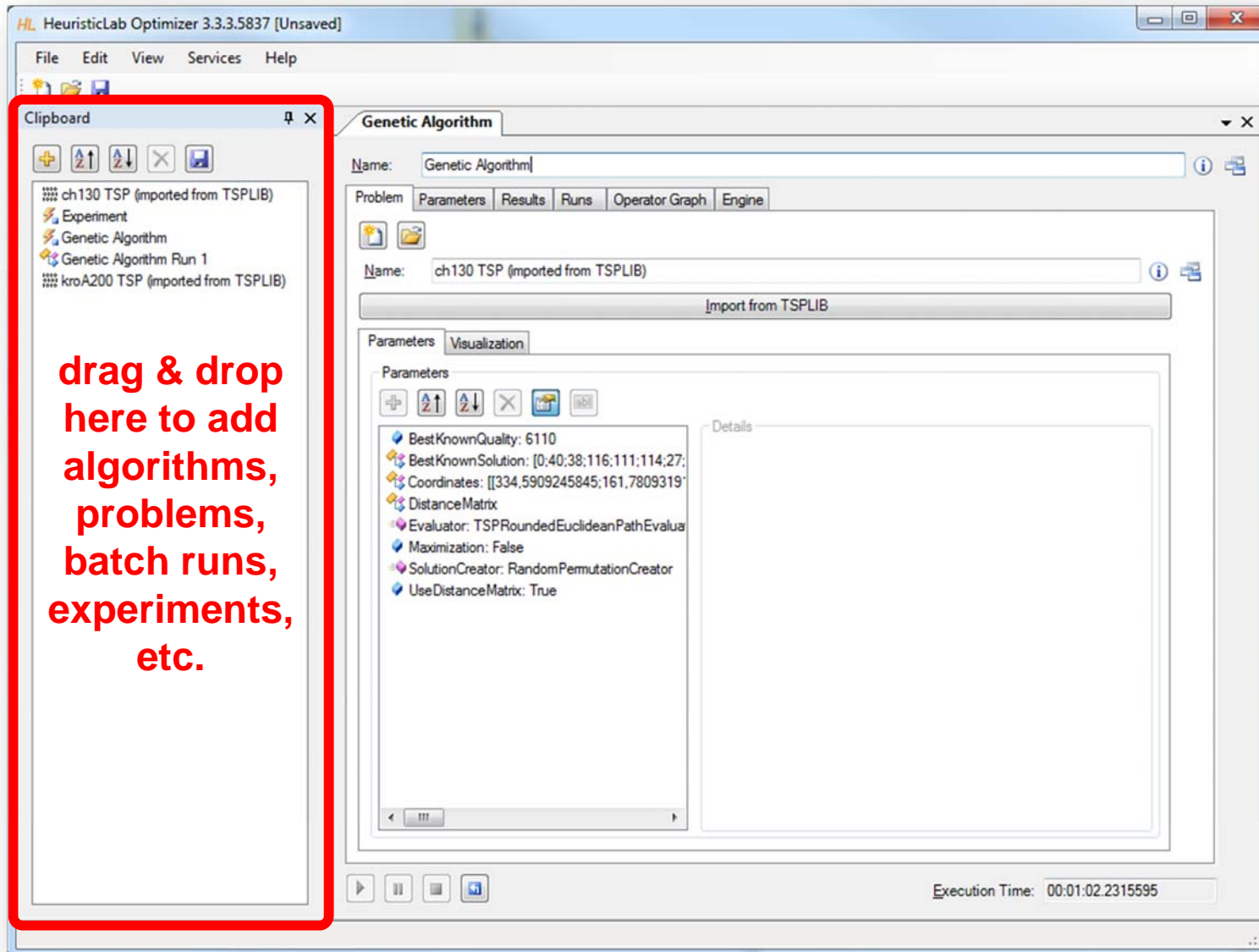




# Create Batch Runs and Experiments



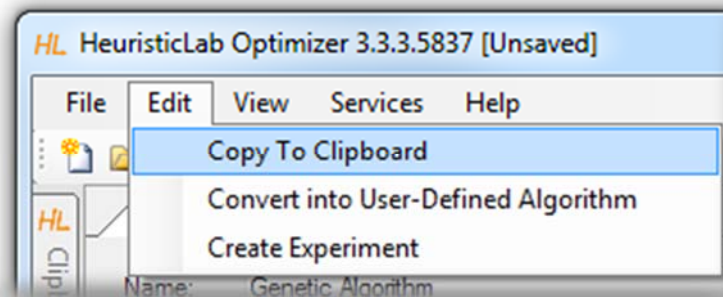
# Clipboard



The screenshot shows the HeuristicLab Optimizer interface. A red-bordered window titled "Clipboard" is open on the left, containing a list of items: "ch130 TSP (imported from TSPLIB)", "Experiment", "Genetic Algorithm", "Genetic Algorithm Run 1", and "kroA200 TSP (imported from TSPLIB)". A red text overlay on the clipboard window reads: "drag & drop here to add algorithms, problems, batch runs, experiments, etc." The main window is titled "Genetic Algorithm" and shows the configuration for a "ch130 TSP (imported from TSPLIB)" problem. The "Parameters" tab is active, displaying various settings such as "BestKnownQuality: 6110", "BestKnownSolution: [0;40;38;116;111;114;27;]", "Coordinates: [[334.5909245845;161.7809319]", "DistanceMatrix", "Evaluator: TSPRoundedEuclideanPathEvaluat", "Maximization: False", "SolutionCreator: RandomPermutationCreator", and "UseDistanceMatrix: True". The "Execution Time" is shown as "00:01:02.2315595".

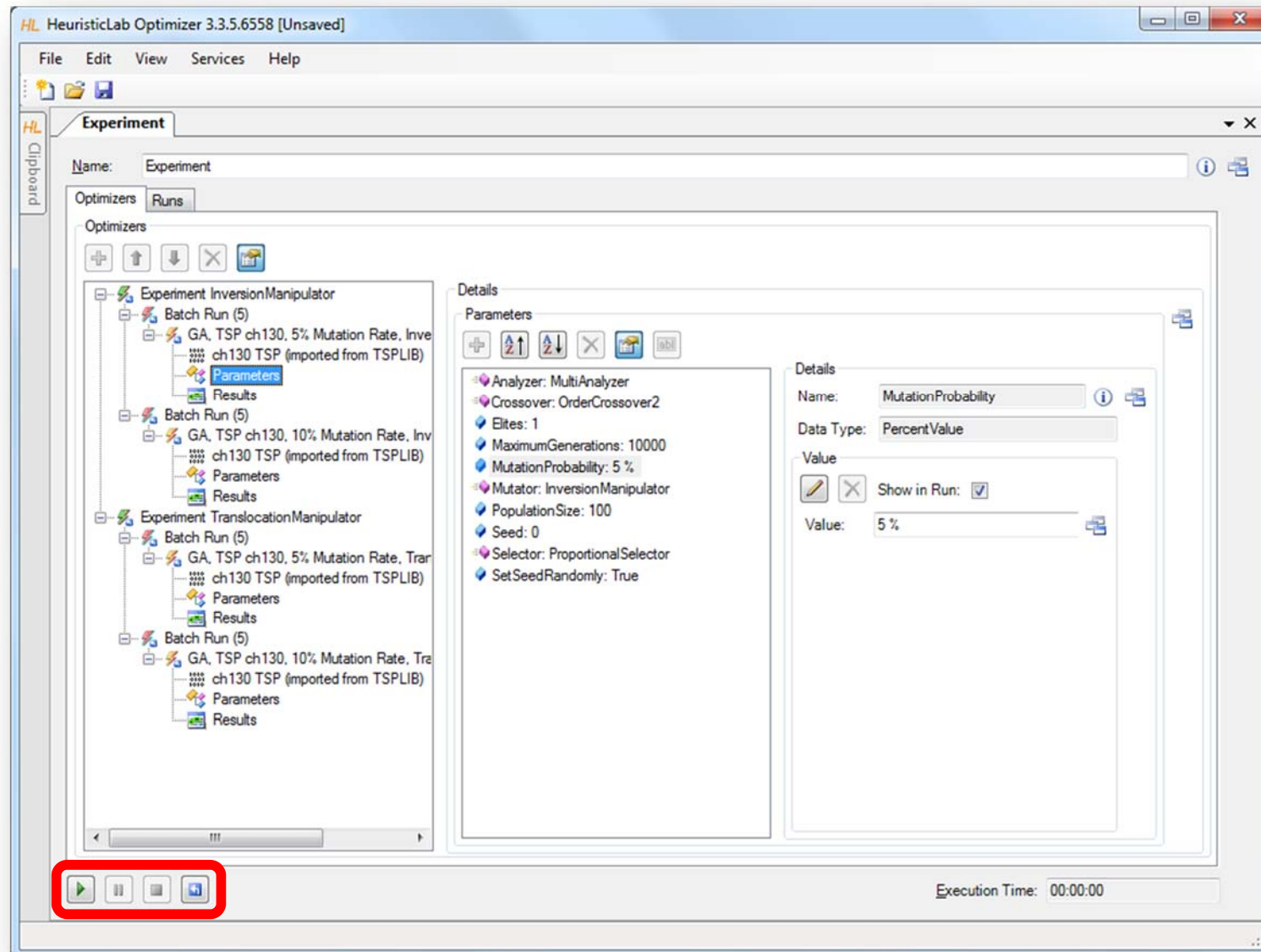
# Clipboard

- Store items
  - click on the buttons to add or remove items
  - drag & drop items on the clipboard
  - use the menu to add a copy of a shown item to the clipboard

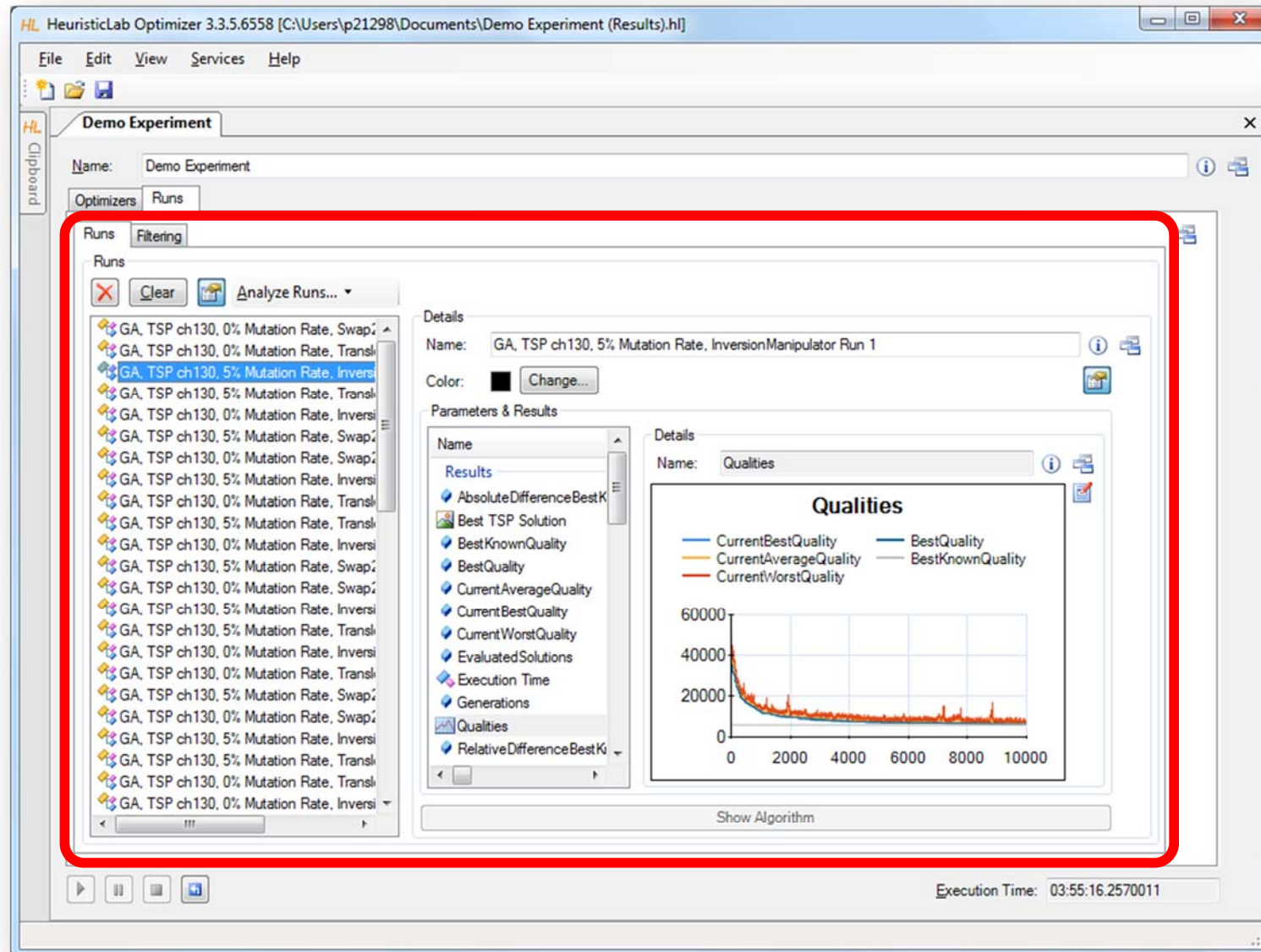


- Show items
  - double-click on an item in the clipboard to show its view
- Save and restore clipboard content
  - click on the save button to write the clipboard content to disk
  - clipboard is automatically restored when HeuristicLab is started the next time

# Start, Pause, Resume, Stop, Reset



# Compare Runs



The screenshot shows the HeuristicLab Optimizer interface. The main window is titled "HL HeuristicLab Optimizer 3.3.5.6558 [C:\Users\p21298\Documents\Demo Experiment (Results).hl]". The interface includes a menu bar (File, Edit, View, Services, Help) and a toolbar. The "Demo Experiment" window is active, showing the "Runs" tab. A red box highlights the "Runs" list and the "Details" panel for a selected run.

**Runs List:**

- GA, TSP ch130, 0% Mutation Rate, Swap
- GA, TSP ch130, 0% Mutation Rate, Transl
- GA, TSP ch130, 5% Mutation Rate, Inversi
- GA, TSP ch130, 5% Mutation Rate, Transl
- GA, TSP ch130, 0% Mutation Rate, Inversi
- GA, TSP ch130, 5% Mutation Rate, Swap
- GA, TSP ch130, 0% Mutation Rate, Swap
- GA, TSP ch130, 5% Mutation Rate, Inversi
- GA, TSP ch130, 0% Mutation Rate, Transl
- GA, TSP ch130, 5% Mutation Rate, Swap
- GA, TSP ch130, 0% Mutation Rate, Swap
- GA, TSP ch130, 5% Mutation Rate, Inversi
- GA, TSP ch130, 5% Mutation Rate, Transl
- GA, TSP ch130, 0% Mutation Rate, Inversi
- GA, TSP ch130, 0% Mutation Rate, Transl
- GA, TSP ch130, 5% Mutation Rate, Swap
- GA, TSP ch130, 0% Mutation Rate, Swap
- GA, TSP ch130, 5% Mutation Rate, Inversi
- GA, TSP ch130, 5% Mutation Rate, Transl
- GA, TSP ch130, 0% Mutation Rate, Transl
- GA, TSP ch130, 0% Mutation Rate, Inversi

**Details Panel:**

Name: GA, TSP ch130, 5% Mutation Rate, InversionManipulator Run 1  
Color:  Change...

**Parameters & Results:**

- AbsoluteDifferenceBestK
- Best TSP Solution
- BestKnownQuality
- BestQuality
- CurrentAverageQuality
- CurrentBestQuality
- CurrentWorstQuality
- EvaluatedSolutions
- Execution Time
- Generations
- Qualities
- RelativeDifferenceBestK

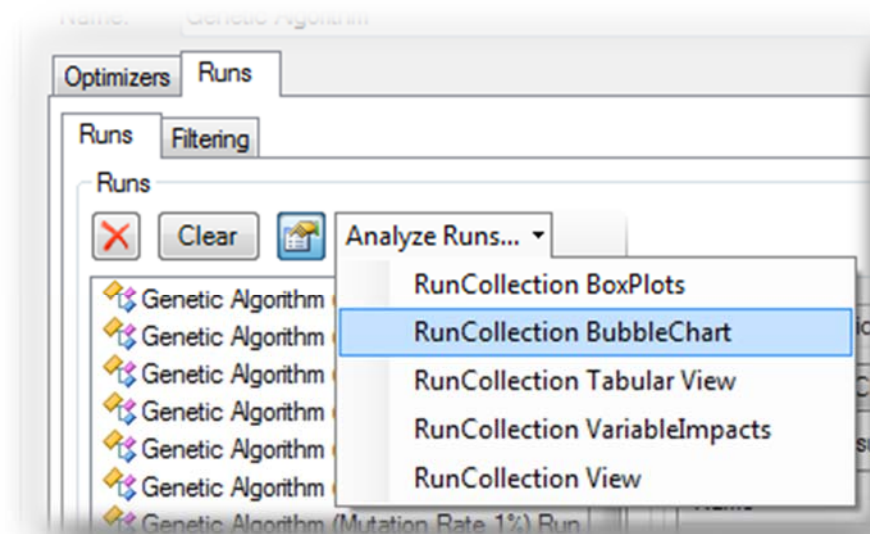
**Qualities Graph:**

The graph shows the quality of solutions over 10,000 generations. The Y-axis represents quality (0 to 60,000) and the X-axis represents generations (0 to 10,000). The legend includes: CurrentBestQuality (blue), CurrentAverageQuality (yellow), CurrentWorstQuality (orange), BestQuality (green), and BestKnownQuality (grey). The graph shows a sharp initial drop in quality, followed by a plateau around 10,000.

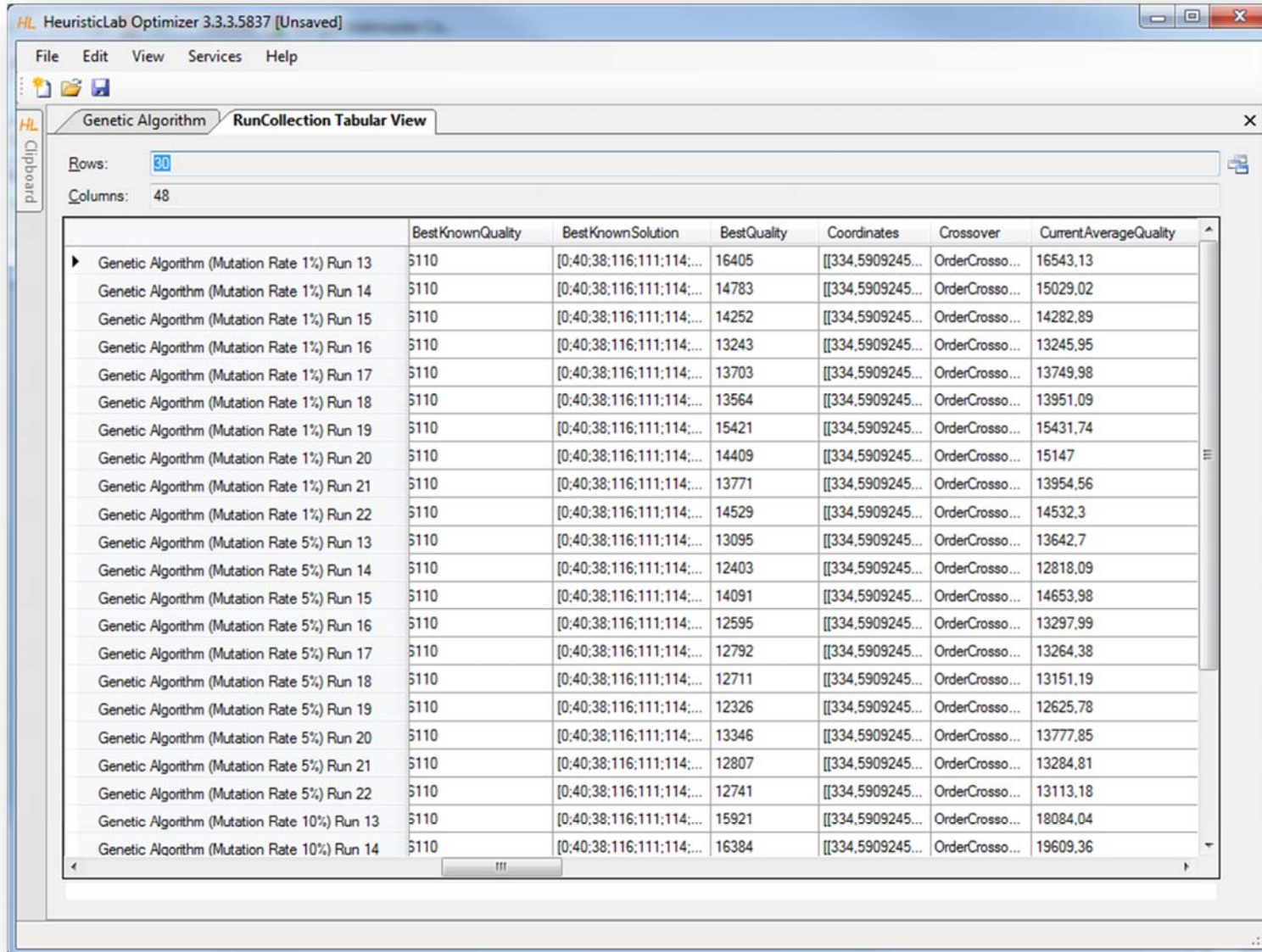
Execution Time: 03:55:16.2570011

# Analyze Runs

- HeuristicLab provides interactive views to analyze and compare all runs of a run collection
  - textual analysis
    - RunCollection Tabular View
  - graphical analysis
    - RunCollection BubbleChart
    - RunCollection BoxPlots
- Filtering is automatically applied to all open run collection views



# RunCollection Tabular View



	BestKnownQuality	BestKnownSolution	BestQuality	Coordinates	Crossover	CurrentAverageQuality
▶ Genetic Algorithm (Mutation Rate 1%) Run 13	5110	[0:40:38:116:111:114:...	16405	[[334,5909245...	OrderCrosso...	16543,13
Genetic Algorithm (Mutation Rate 1%) Run 14	5110	[0:40:38:116:111:114:...	14783	[[334,5909245...	OrderCrosso...	15029,02
Genetic Algorithm (Mutation Rate 1%) Run 15	5110	[0:40:38:116:111:114:...	14252	[[334,5909245...	OrderCrosso...	14282,89
Genetic Algorithm (Mutation Rate 1%) Run 16	5110	[0:40:38:116:111:114:...	13243	[[334,5909245...	OrderCrosso...	13245,95
Genetic Algorithm (Mutation Rate 1%) Run 17	5110	[0:40:38:116:111:114:...	13703	[[334,5909245...	OrderCrosso...	13749,98
Genetic Algorithm (Mutation Rate 1%) Run 18	5110	[0:40:38:116:111:114:...	13564	[[334,5909245...	OrderCrosso...	13951,09
Genetic Algorithm (Mutation Rate 1%) Run 19	5110	[0:40:38:116:111:114:...	15421	[[334,5909245...	OrderCrosso...	15431,74
Genetic Algorithm (Mutation Rate 1%) Run 20	5110	[0:40:38:116:111:114:...	14409	[[334,5909245...	OrderCrosso...	15147
Genetic Algorithm (Mutation Rate 1%) Run 21	5110	[0:40:38:116:111:114:...	13771	[[334,5909245...	OrderCrosso...	13954,56
Genetic Algorithm (Mutation Rate 1%) Run 22	5110	[0:40:38:116:111:114:...	14529	[[334,5909245...	OrderCrosso...	14532,3
Genetic Algorithm (Mutation Rate 5%) Run 13	5110	[0:40:38:116:111:114:...	13095	[[334,5909245...	OrderCrosso...	13642,7
Genetic Algorithm (Mutation Rate 5%) Run 14	5110	[0:40:38:116:111:114:...	12403	[[334,5909245...	OrderCrosso...	12818,09
Genetic Algorithm (Mutation Rate 5%) Run 15	5110	[0:40:38:116:111:114:...	14091	[[334,5909245...	OrderCrosso...	14653,98
Genetic Algorithm (Mutation Rate 5%) Run 16	5110	[0:40:38:116:111:114:...	12595	[[334,5909245...	OrderCrosso...	13297,99
Genetic Algorithm (Mutation Rate 5%) Run 17	5110	[0:40:38:116:111:114:...	12792	[[334,5909245...	OrderCrosso...	13264,38
Genetic Algorithm (Mutation Rate 5%) Run 18	5110	[0:40:38:116:111:114:...	12711	[[334,5909245...	OrderCrosso...	13151,19
Genetic Algorithm (Mutation Rate 5%) Run 19	5110	[0:40:38:116:111:114:...	12326	[[334,5909245...	OrderCrosso...	12625,78
Genetic Algorithm (Mutation Rate 5%) Run 20	5110	[0:40:38:116:111:114:...	13346	[[334,5909245...	OrderCrosso...	13777,85
Genetic Algorithm (Mutation Rate 5%) Run 21	5110	[0:40:38:116:111:114:...	12807	[[334,5909245...	OrderCrosso...	13284,81
Genetic Algorithm (Mutation Rate 5%) Run 22	5110	[0:40:38:116:111:114:...	12741	[[334,5909245...	OrderCrosso...	13113,18
Genetic Algorithm (Mutation Rate 10%) Run 13	5110	[0:40:38:116:111:114:...	15921	[[334,5909245...	OrderCrosso...	18084,04
Genetic Algorithm (Mutation Rate 10%) Run 14	5110	[0:40:38:116:111:114:...	16384	[[334,5909245...	OrderCrosso...	19609,36

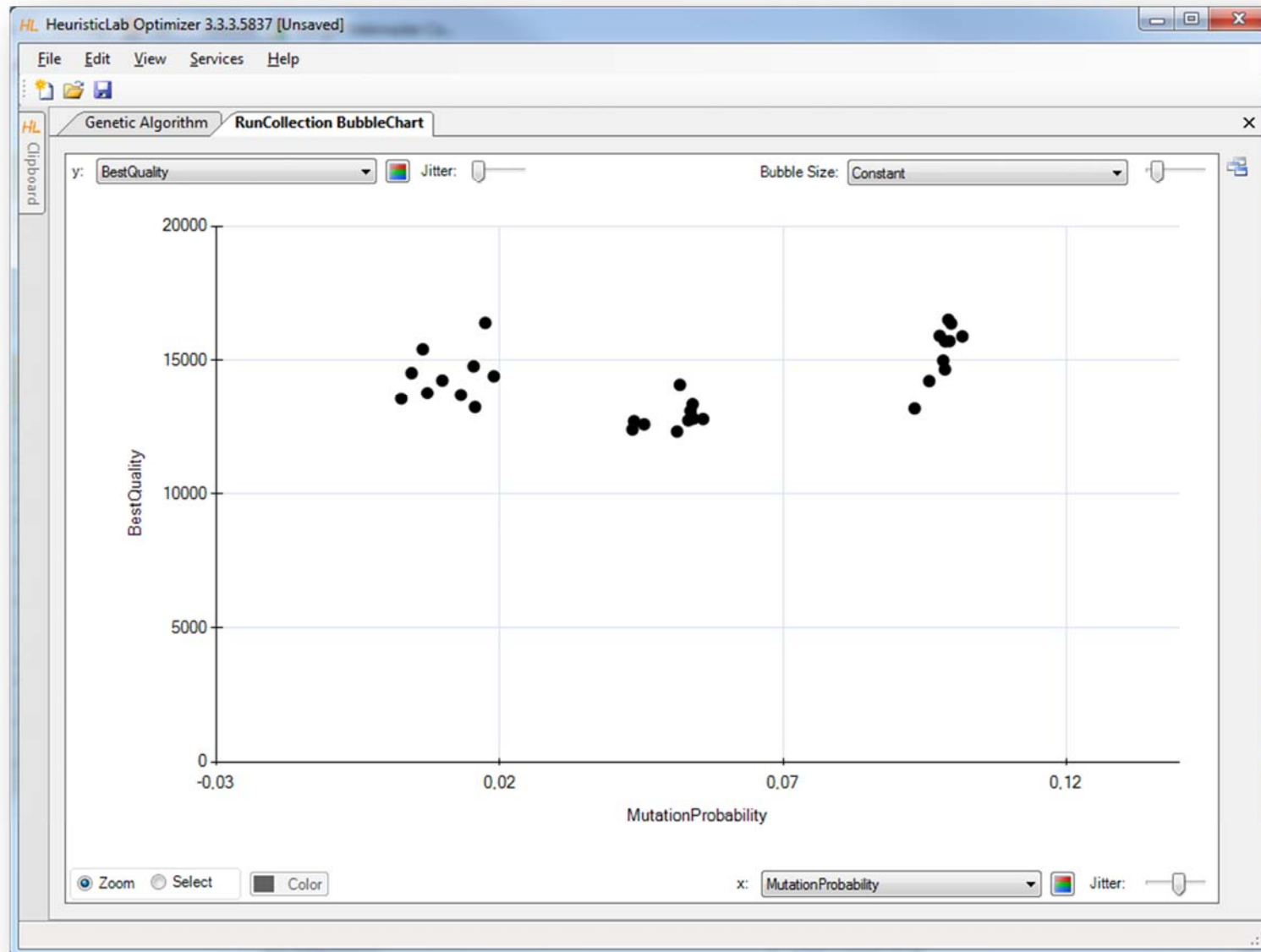
# RunCollection Tabular View



- Sort columns
  - click on column header to sort column
  - Ctrl-click on column header to sort multiple columns
- Show or hide columns
  - right-click on table to open dialog to show or hide columns
- Compute statistical values
  - select multiple numerical values to see count, sum, minimum, maximum, average and standard deviation
- Select, copy and paste into other applications



# RunCollection BubbleChart

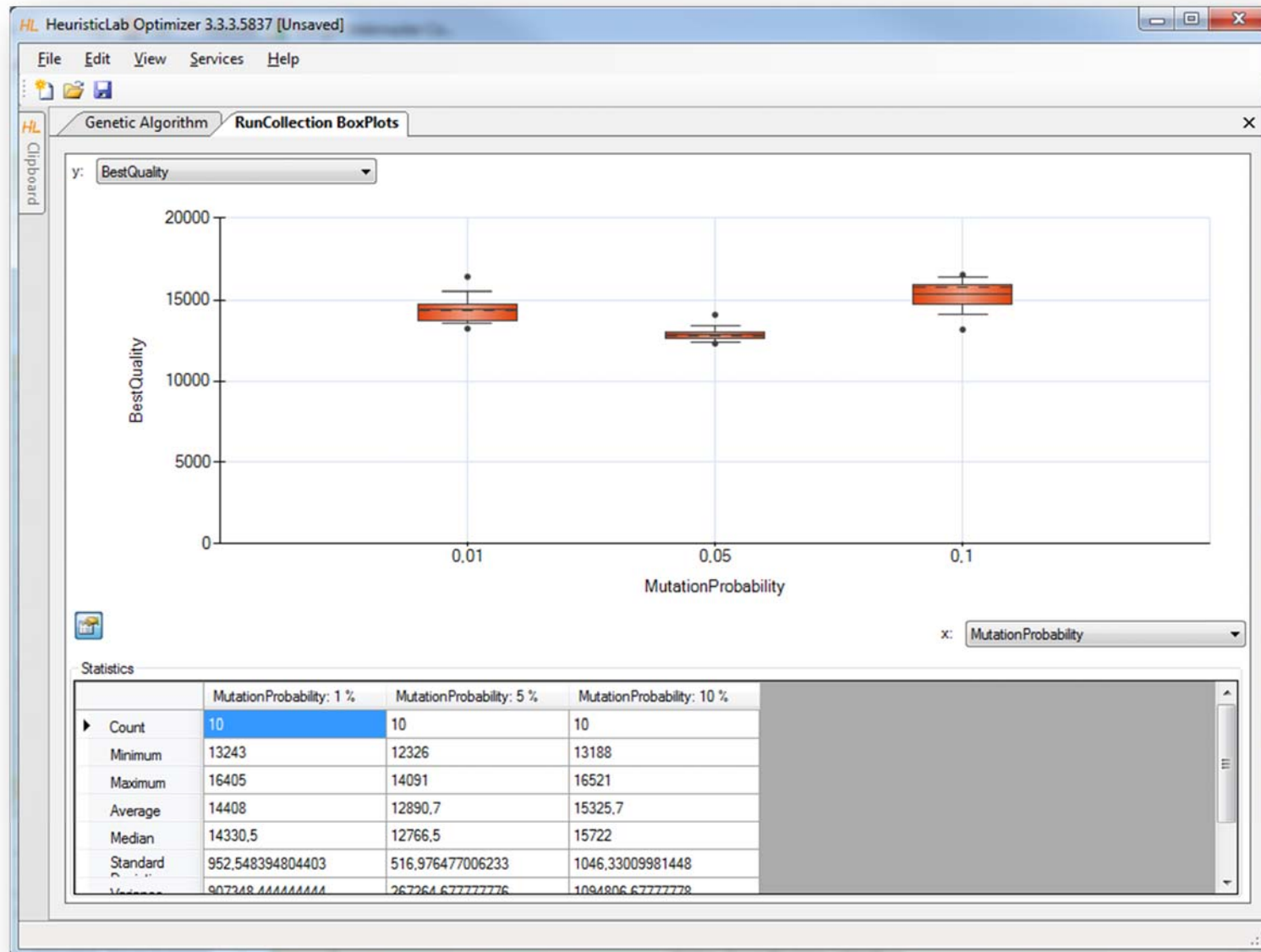


# RunCollection BubbleChart



- Choose values to plot
  - choose which values to show on the x-axis, the y-axis and as bubble size
  - possible values are all parameter settings and results
- Add jitter
  - add jitter to separate overlapping bubbles
- Zoom in and out
  - click on Zoom and click and drag in the chart area to zoom in
  - double click on the chart area background or on the circle buttons beside the scroll bars to zoom out
- Color bubbles
  - click on Select, choose a color and click and drag in the chart area to select and color bubbles
  - apply coloring automatically by clicking on the axis coloring buttons
- Show runs
  - double click on a bubble to open its run
- Export image
  - right-click to open context menu to copy or save image
  - save image as pixel (BMP, JPG, PNG, GIF, TIF) or vector graphics (EMF)
- Show box plots
  - right-click to open context menu to show box plots view

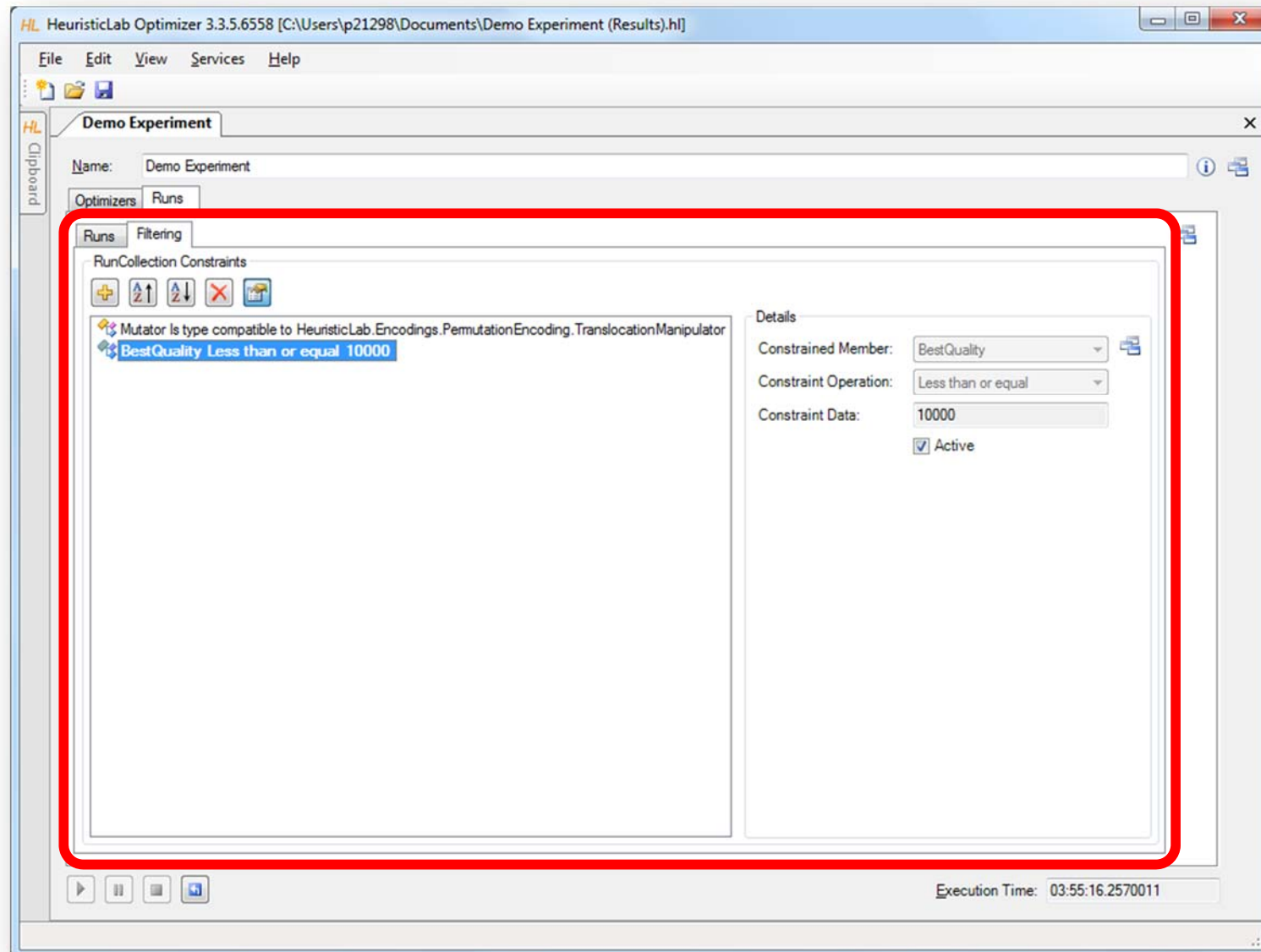
# RunCollection BoxPlots



# RunCollection BoxPlots

- Choose values to plot
  - choose which values to show on the x-axis and y-axis
  - possible values are all parameter settings and results
- Zoom in and out
  - click on Zoom and click and drag in the chart area to zoom in
  - double click on the chart area background or on the circle buttons beside the scroll bars to zoom out
- Show or hide statistical values
  - click on the lower left button to show or hide statistical values
- Export image
  - right-click to open context menu to copy or save image
  - save image as pixel (BMP, JPG, PNG, GIF, TIF) or vector graphics (EMF)

# Filter Runs

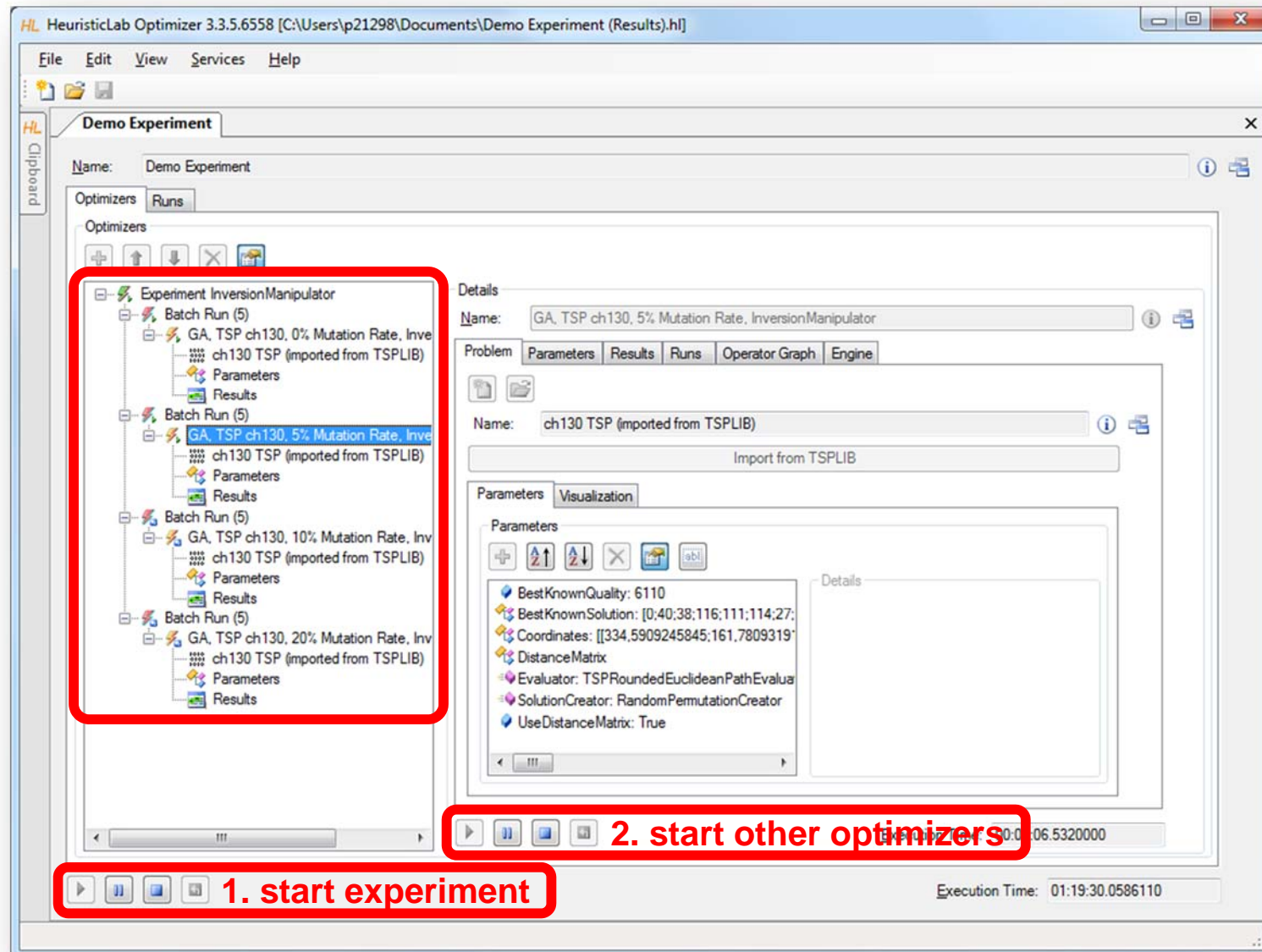


# Multi-core CPUs and Parallelization



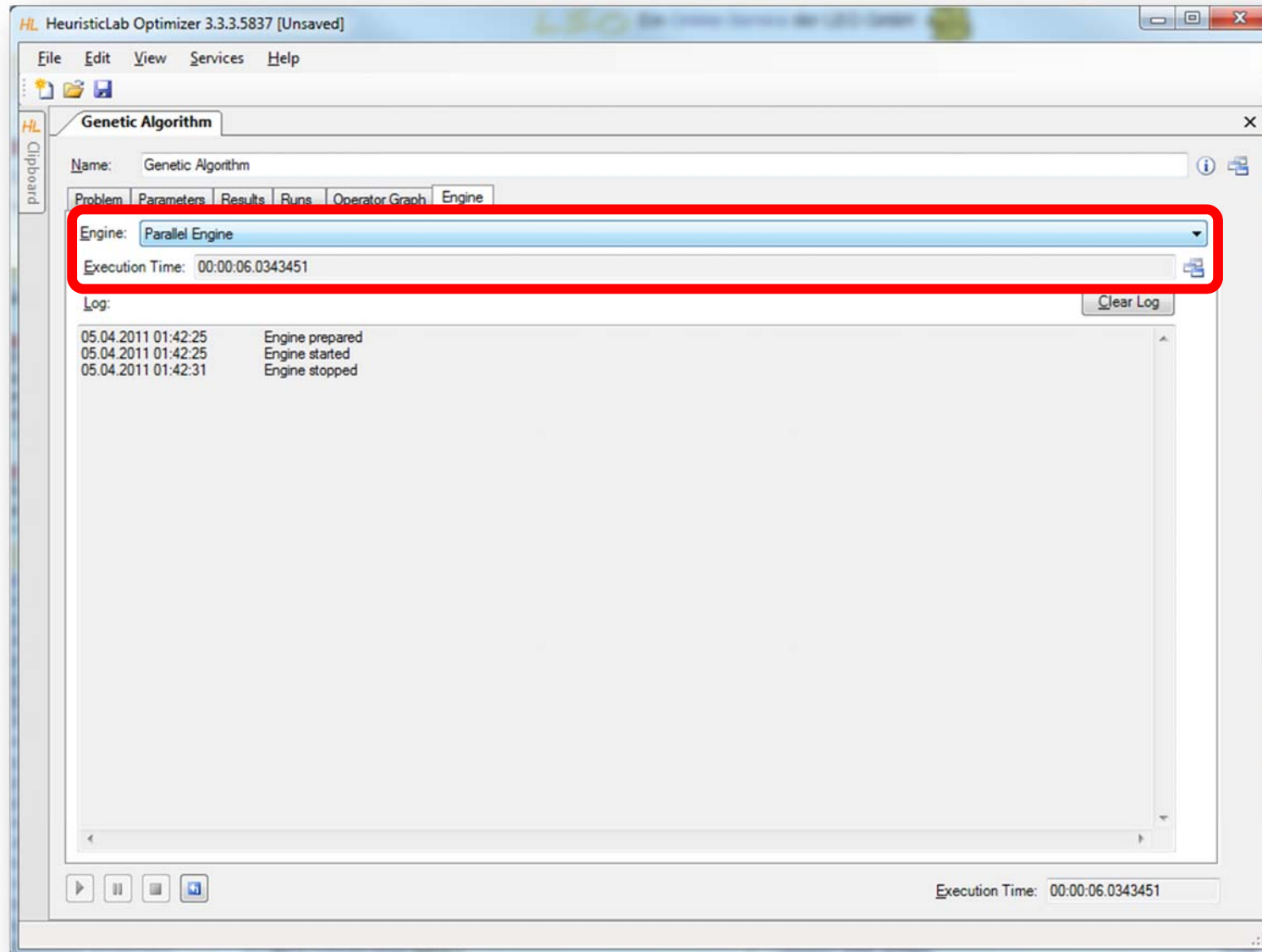
- Parallel execution of optimizers in experiments
  - optimizers in an experiment are executed sequentially from top to bottom per default
  - experiments support parallel execution of their optimizers
  - select a not yet executed optimizer and start it manually to utilize another core
  - execution of one of the next optimizers is started automatically after an optimizer is finished
- Parallel execution of algorithms
  - HeuristicLab provides special operators for parallelization
  - engines decide how to execute parallel operations
  - sequential engine executes everything sequentially
  - parallel engine executes parallel operations on multiple cores
  - Hive engine (under development) executes parallel operations on multiple computers
  - all implemented algorithms support parallel solution evaluation

# Parallel Execution of Experiments



The screenshot shows the HeuristicLab Optimizer interface. On the left, a tree view under 'Demo Experiment' shows a hierarchy of 'Batch Run (5)' nodes, each containing an optimizer and its results. One node is highlighted with a red box. On the right, the 'Details' panel shows the configuration for the selected optimizer: 'GA, TSP ch130, 5% Mutation Rate, Inve...'. Below this, the 'Parameters' tab is active, showing various parameters like 'BestKnownQuality: 6110' and 'UseDistanceMatrix: True'. At the bottom, a red box highlights the '1. start experiment' button, and another red box highlights the '2. start other optimizers' button.

# Parallel Execution of Algorithms



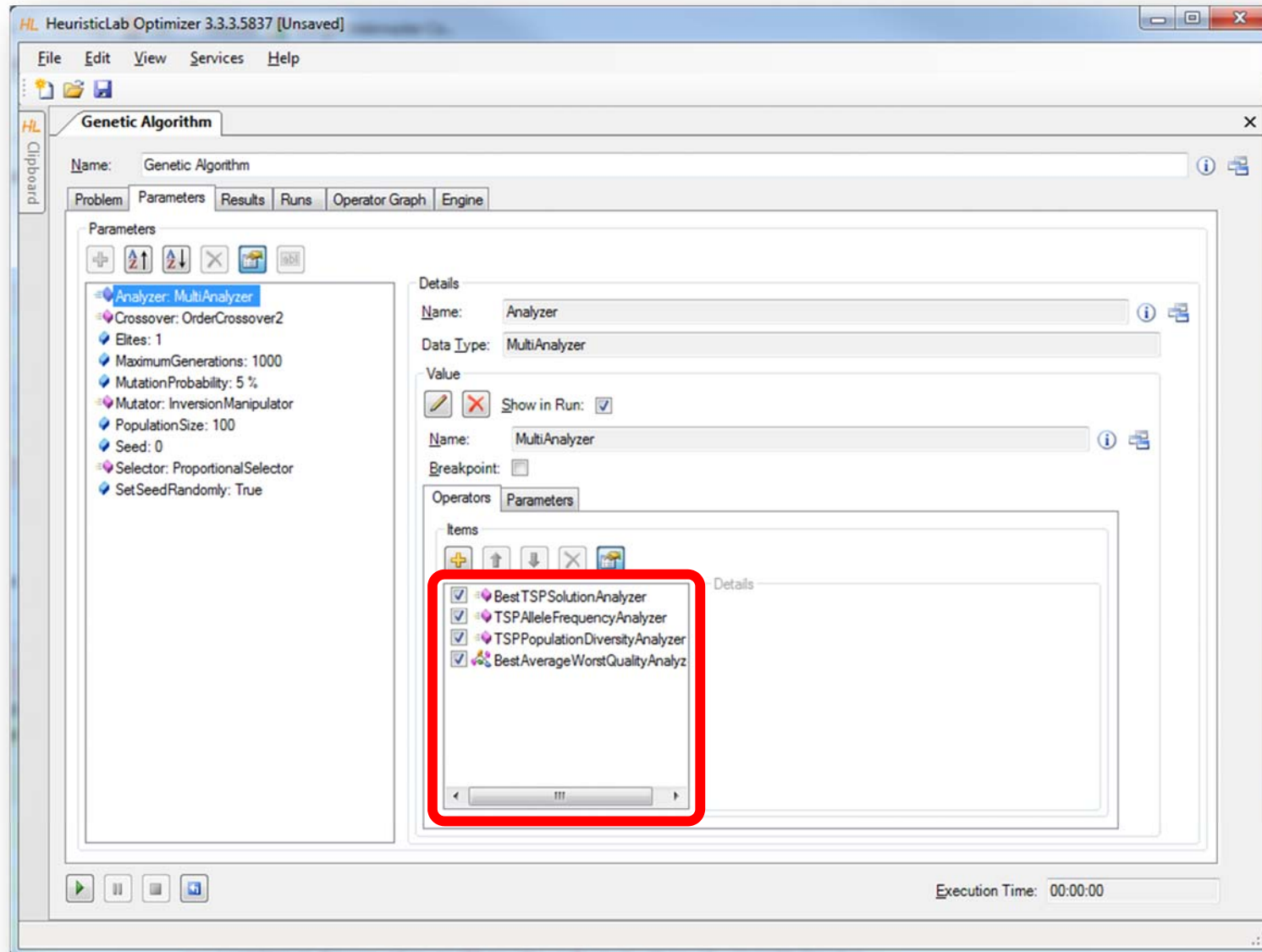


# Analyzers

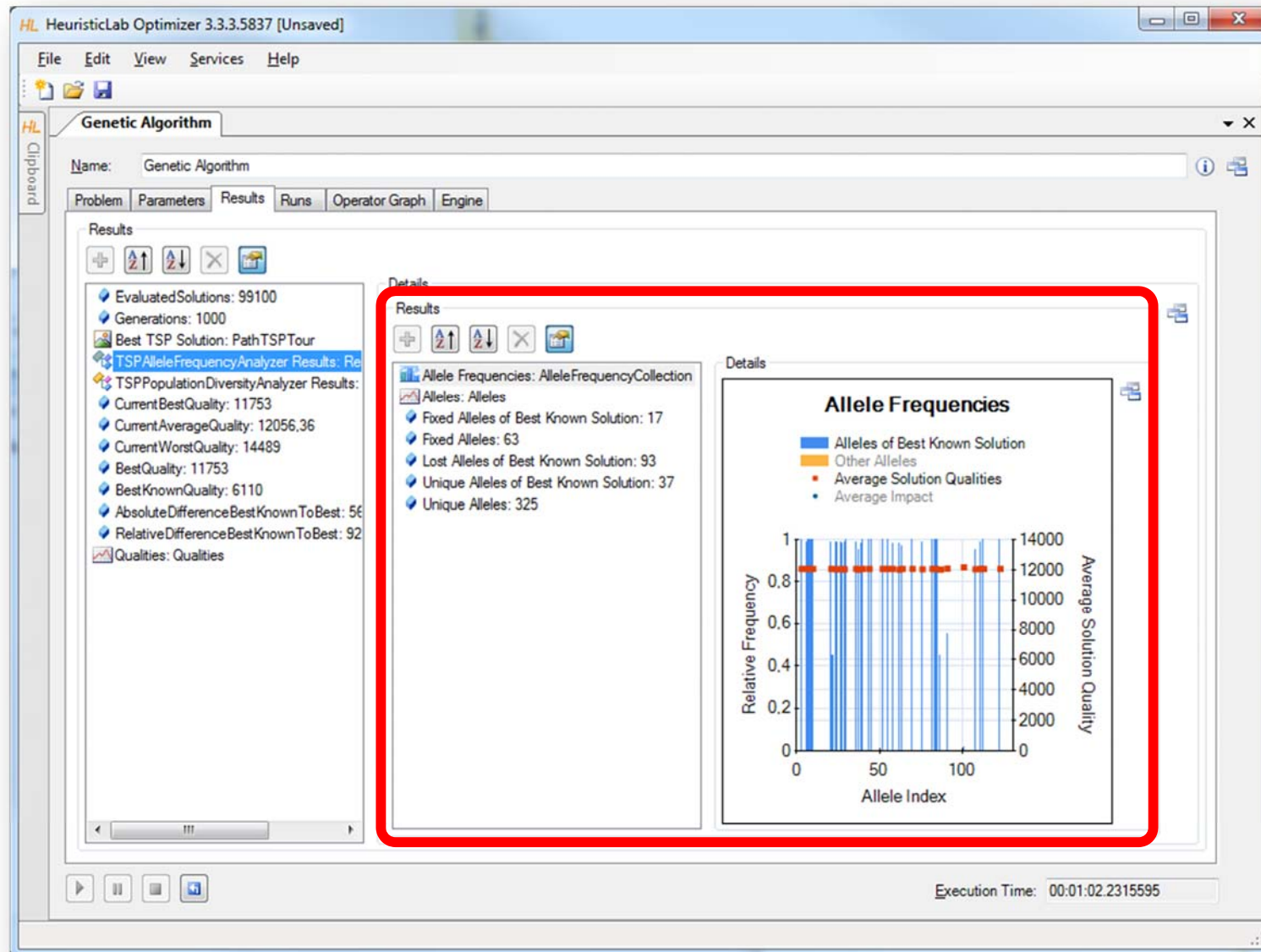


- Special operators for analysis purposes
  - are executed after each iteration
  - serve as general purpose extension points of algorithms
  - can be selected and parameterized in the algorithm
  - perform algorithm-specific and/or problem-specific tasks
  - some analyzers are quite costly regarding runtime and memory
  - implementing and adding custom analyzers is easy
- Examples
  - TSPAlleleFrequencyAnalyzer
  - TSPPopulationDiversityAnalyzer
  - SuccessfulOffspringAnalyzer
  - SymbolicDataAnalysisVariableFrequencyAnalyzer
  - SymbolicRegressionSingleObjectiveTrainingBestSolutionAnalyzer
  - ...

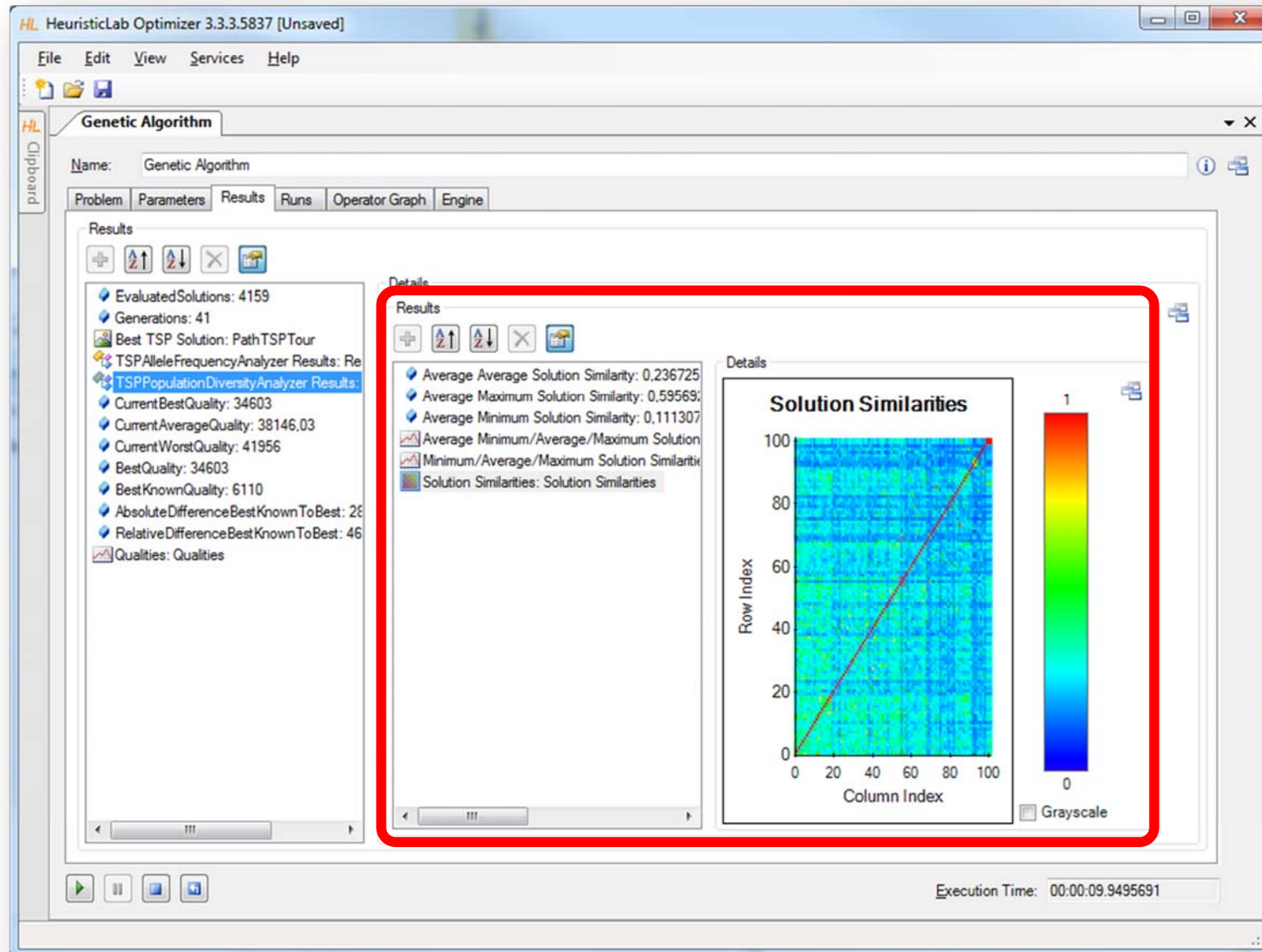
# Analyzers



# TSPAlleleFrequencyAnalyzer

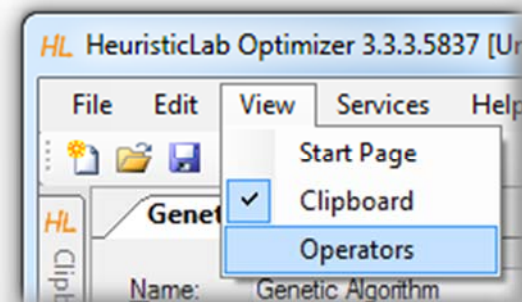
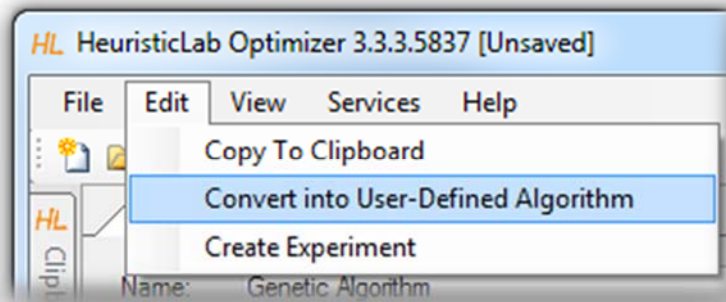


# TSP Population Diversity Analyzer



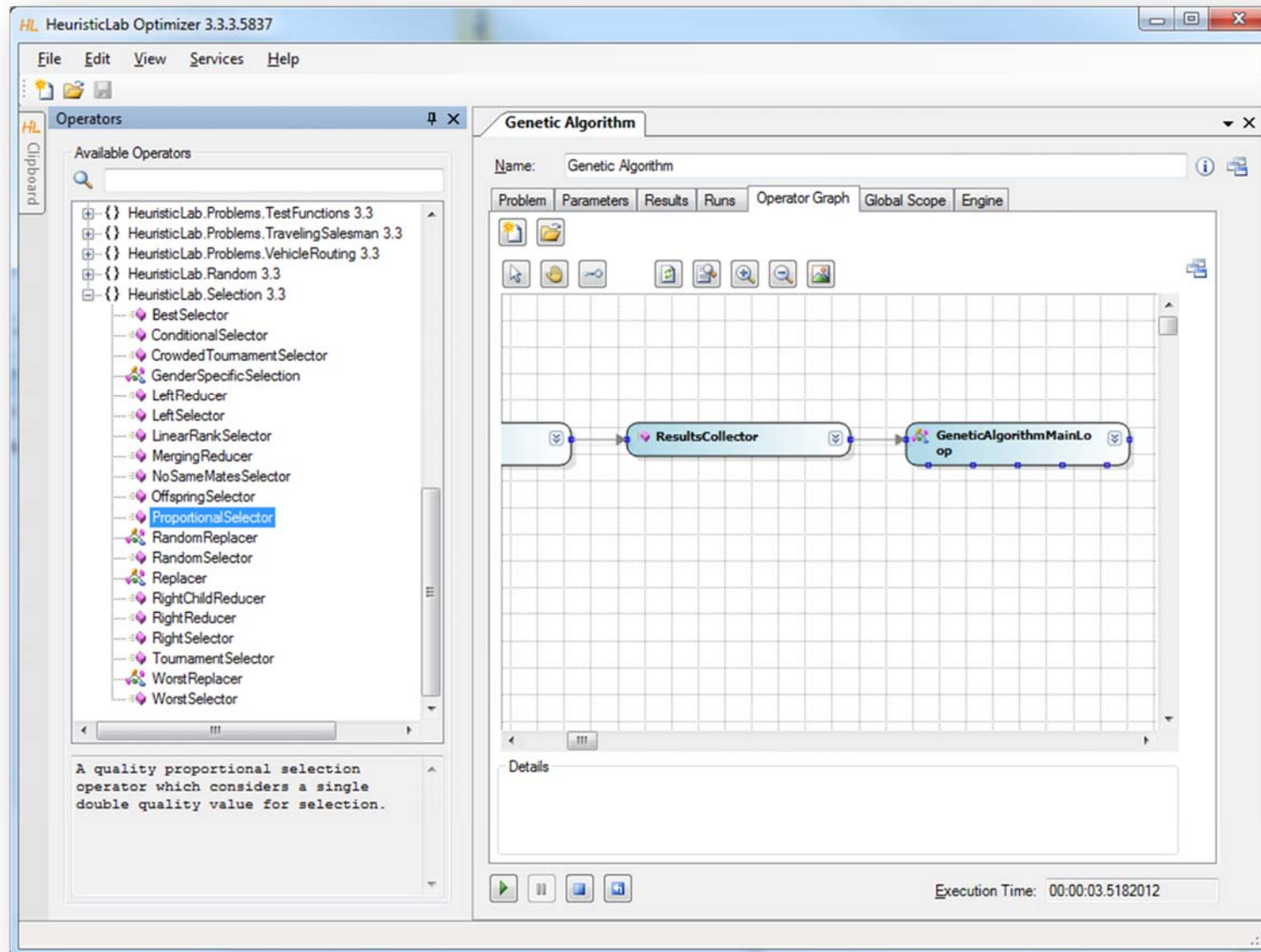
# Building User-Defined Algorithms

- Operator graphs
  - algorithms are represented as operator graphs
  - operator graphs of user-defined algorithms can be changed
  - algorithms can be defined in the graphical algorithm designer
  - use the menu to convert a standard algorithm into a user-defined algorithm



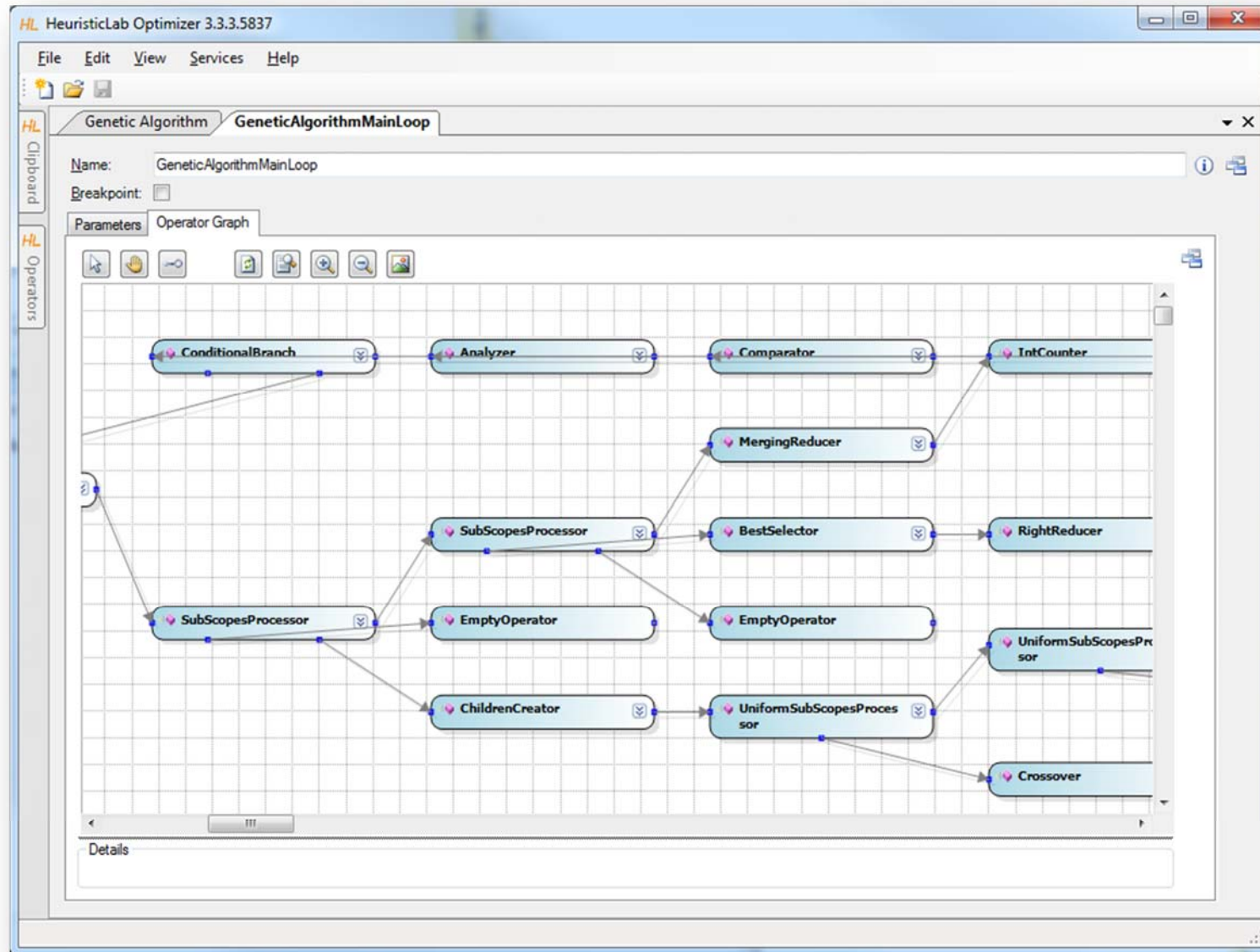
- Operators sidebar
  - drag & drop operators into an operator graph
- Programmable operators
  - add programmable operators in order to implement custom logic in an algorithm
  - no additional development environment needed
- Debug algorithms
  - use the debug engine to obtain detailed information during algorithm execution

# Building User-Defined Algorithms

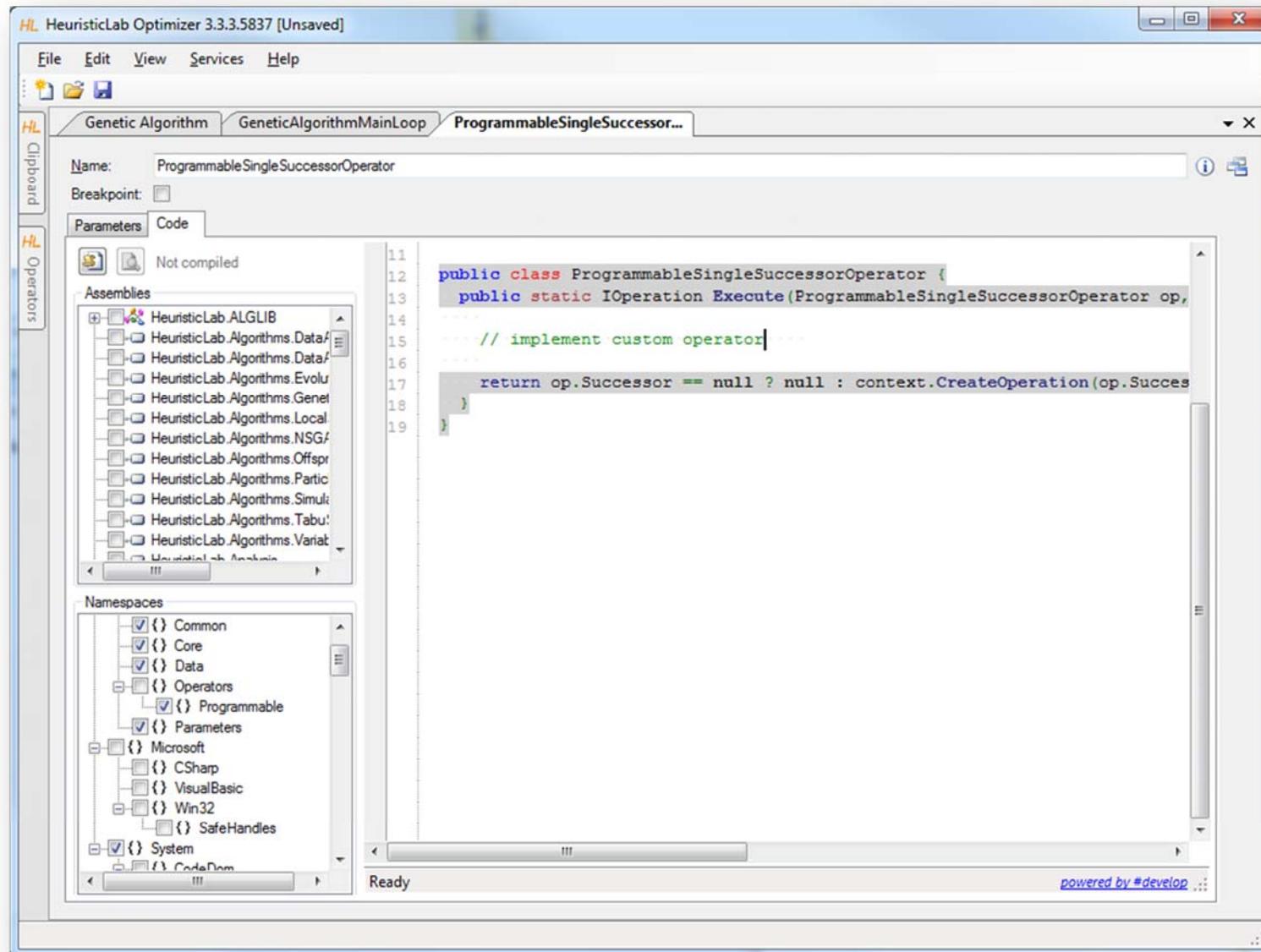


The screenshot displays the HeuristicLab Optimizer 3.3.3.5837 interface. On the left, the 'Operators' panel lists various selection and reduction operators, with 'ProportionalSelector' highlighted. Below this list is a description: 'A quality proportional selection operator which considers a single double quality value for selection.' The main workspace shows the 'Genetic Algorithm' configuration. The 'Operator Graph' tab is active, displaying a flowchart with two nodes: 'ResultsCollector' and 'GeneticAlgorithmMainLo op', connected by an arrow. The 'Details' section at the bottom is empty. The 'Execution Time' is shown as 00:00:03.5182012.

# Building User-Defined Algorithms

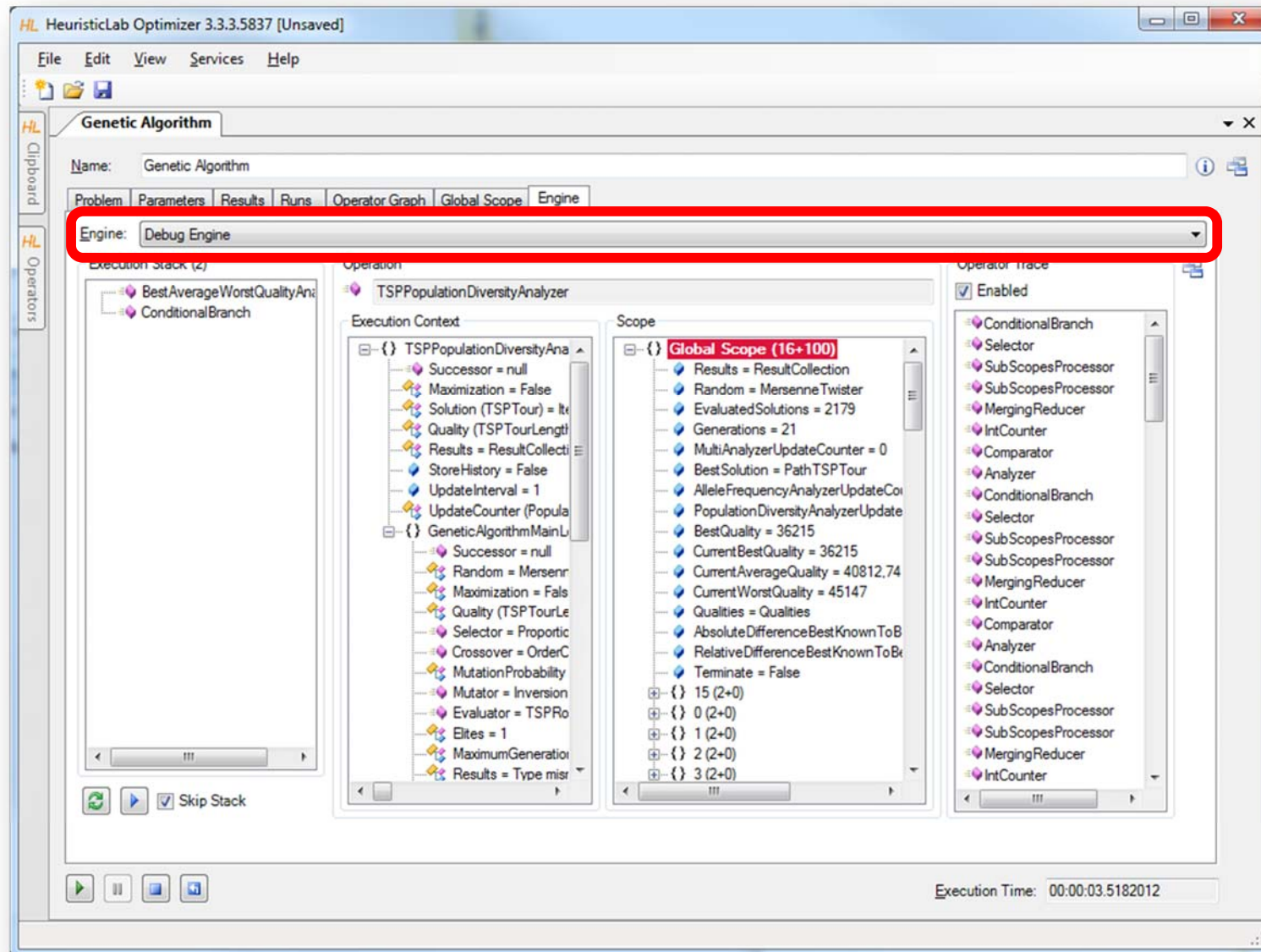


# Programmable Operators





# Debugging Algorithms



# Agenda



- Objectives of the Tutorial
- Introduction
- Where to get HeuristicLab?
- Plugin Infrastructure
- Graphical User Interface
- Available Algorithms & Problems
  
- **Demonstration Part I: Working with HeuristicLab**
- **Demonstration Part II: Data-based Modeling**
  
- Some Additional Features
- Planned Features
- Team
- Suggested Readings
- Bibliography
- Questions & Answers

# Demonstration Part II: Data-based Modeling



- Introduction
- Regression with HeuristicLab
- Model simplification and export
- Variable relevance analysis
- Classification with HeuristicLab

# Introduction to Data-based Modeling



- Dataset: Matrix  $(x_{i,j})_{i=1..N, j=1..K}$ 
  - N observations of K input variables
  - $x_{i,j}$  = i-th observation of j-th variable
  - Additionally: Vector of labels  $(y_1 \dots y_N)^T$
- Goal: learn association of input variable values to labels
- Common tasks
  - Regression (real-valued labels)
  - Classification (discrete labels)
  - Clustering (no labels, group similar observations)

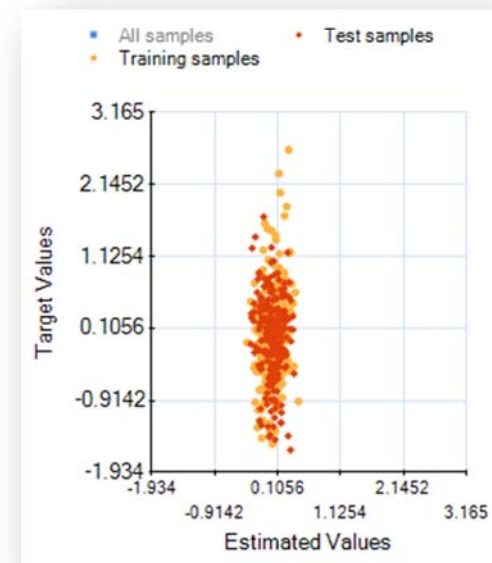
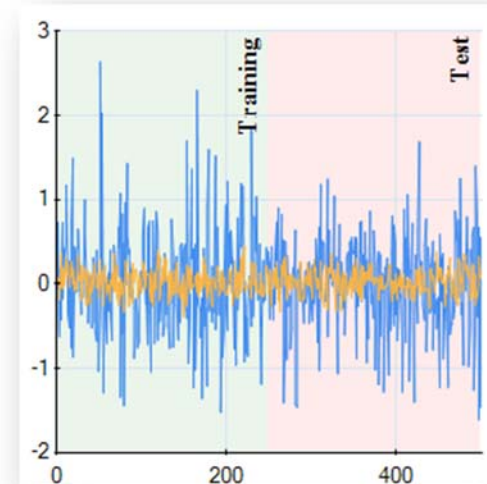
# Data-based Modeling Algorithms in HeuristicLab



- Symbolic regression and classification based on genetic programming
- External Libraries:
  - Support Vector Machines for Regression and Classification
  - Linear Regression
  - Linear Discriminate Analysis
  - K-Means clustering

# Case Studies

- Demonstration
  - problem configuration
    - data import
    - target variable
    - input variables
    - data partitions (training and test)
  - analysis of results
    - accuracy metrics
    - visualization of model output

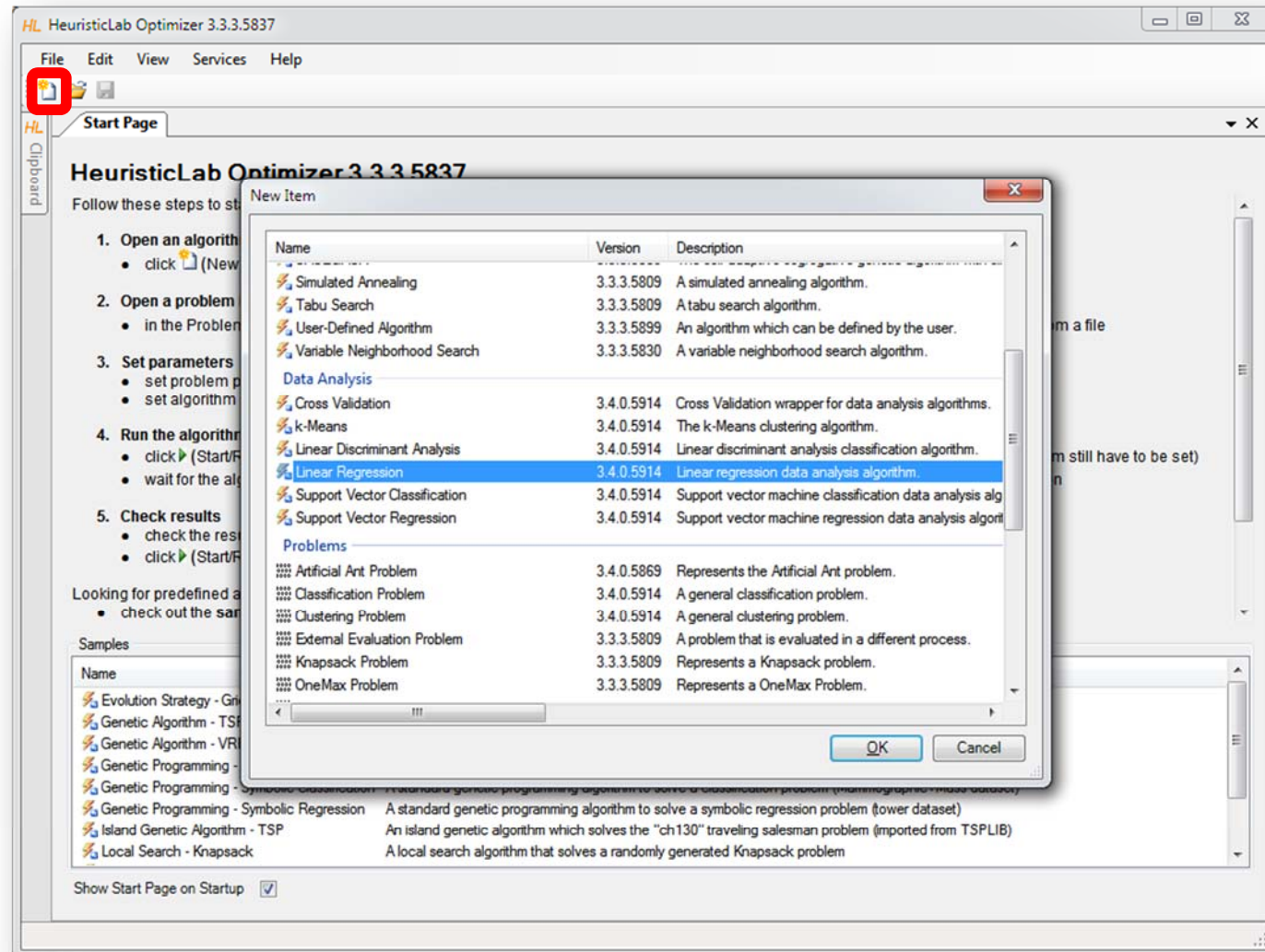


# Case Study: Regression

- Poly-10 benchmark problem dataset
  - 10 input variables  $x_1 \dots x_{10}$
  - $y = x_1 \cdot x_2 + x_3 \cdot x_4 + x_5 \cdot x_6 + x_1 \cdot x_7 \cdot x_9 + x_3 \cdot x_6 \cdot x_{10}$
  - non-linear modeling approach necessary
  - frequently used in GP literature
  - download  
<http://dev.heuristiclab.com/AdditionalMaterial#GECCO2012>

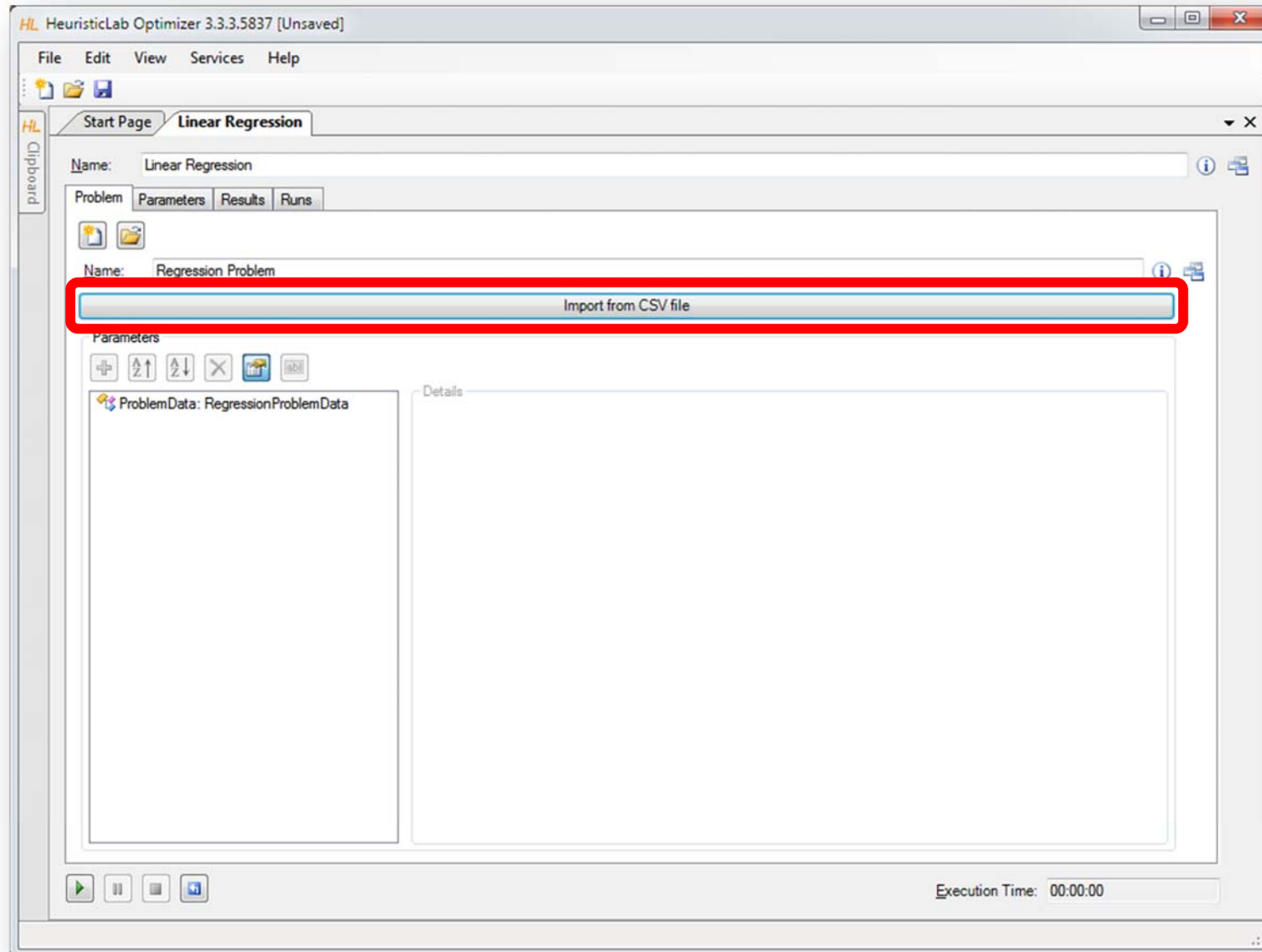
# Linear Regression

- Create new algorithm

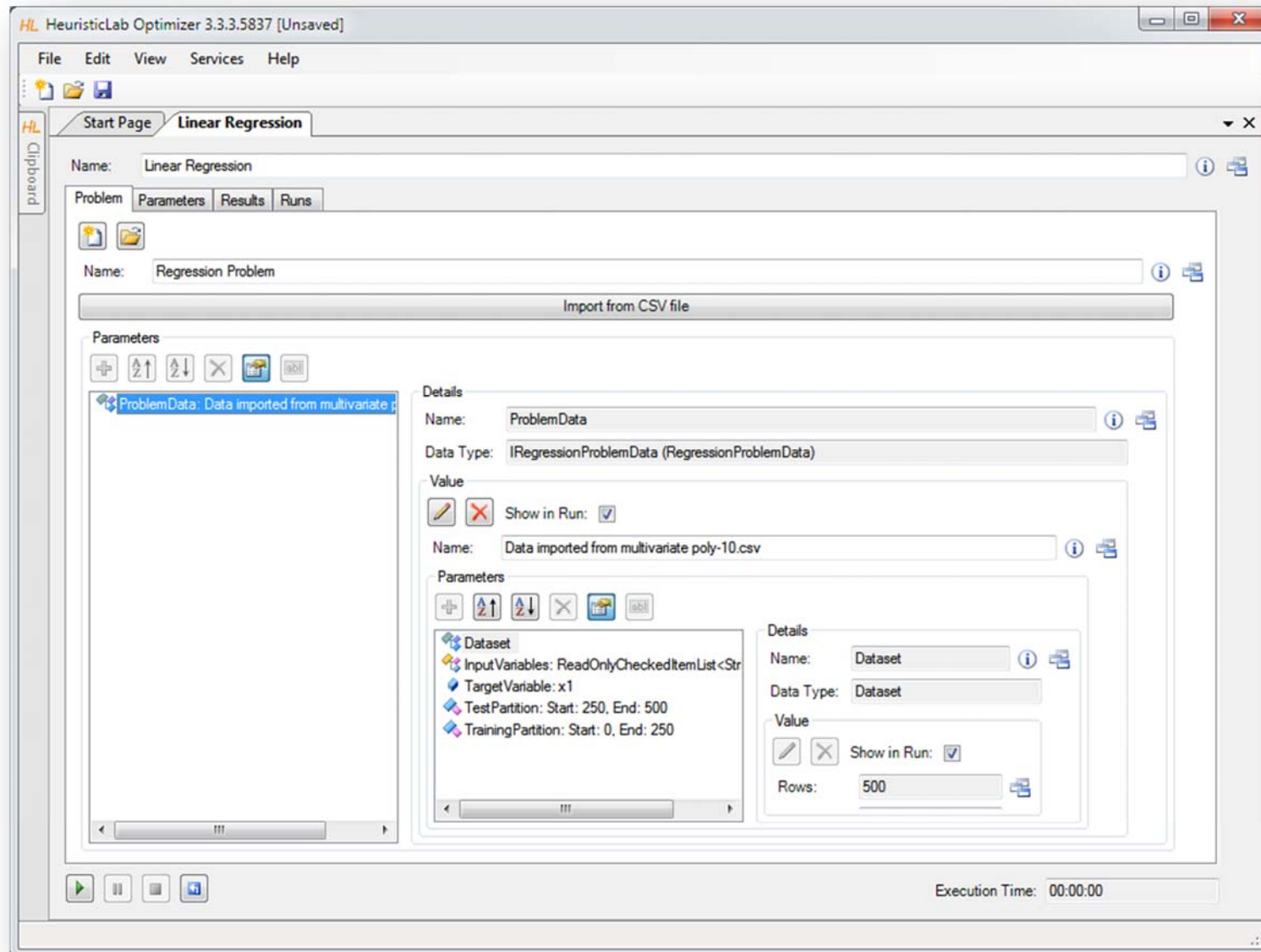




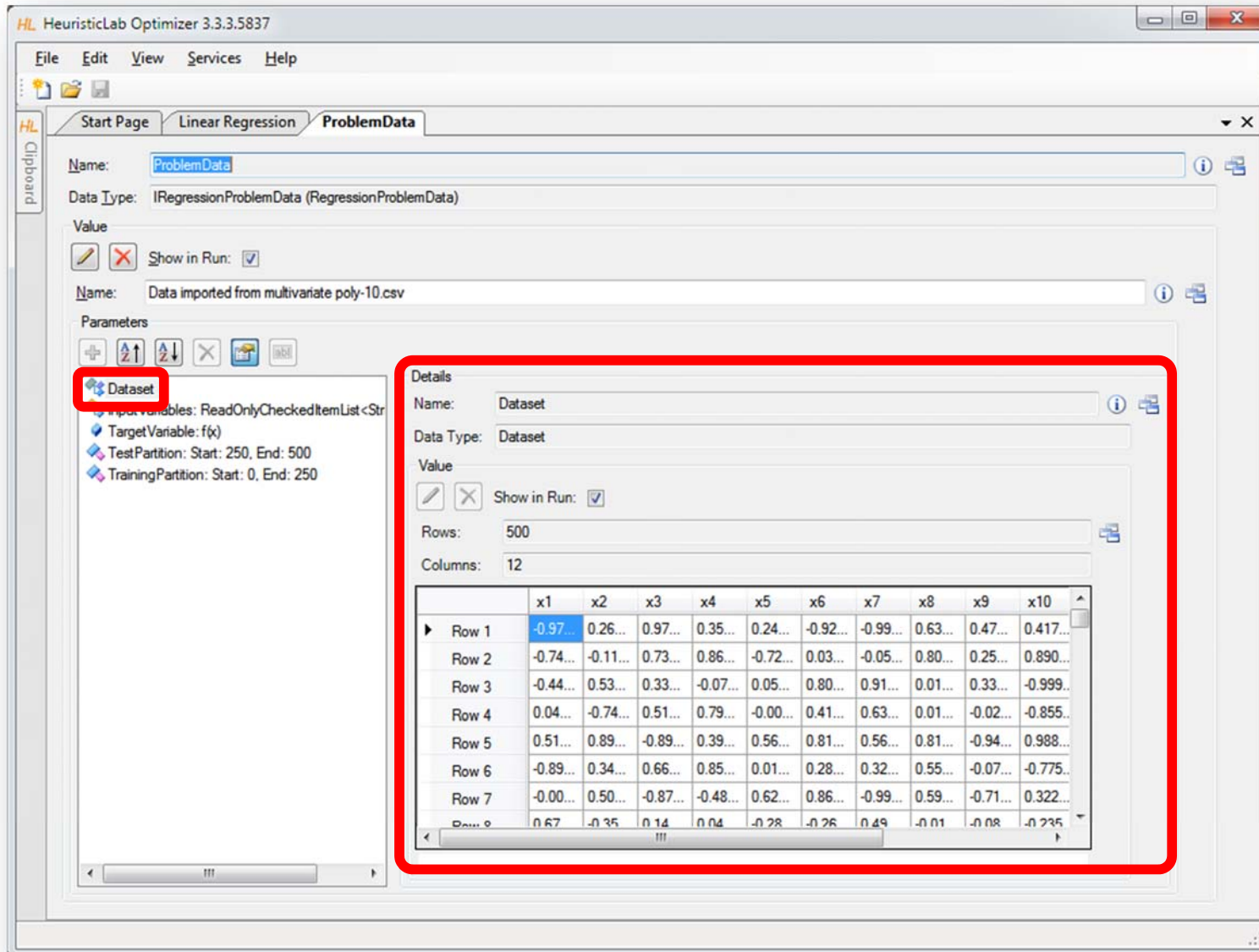
# Import Data from CSV-File



# Inspect and Configure Dataset



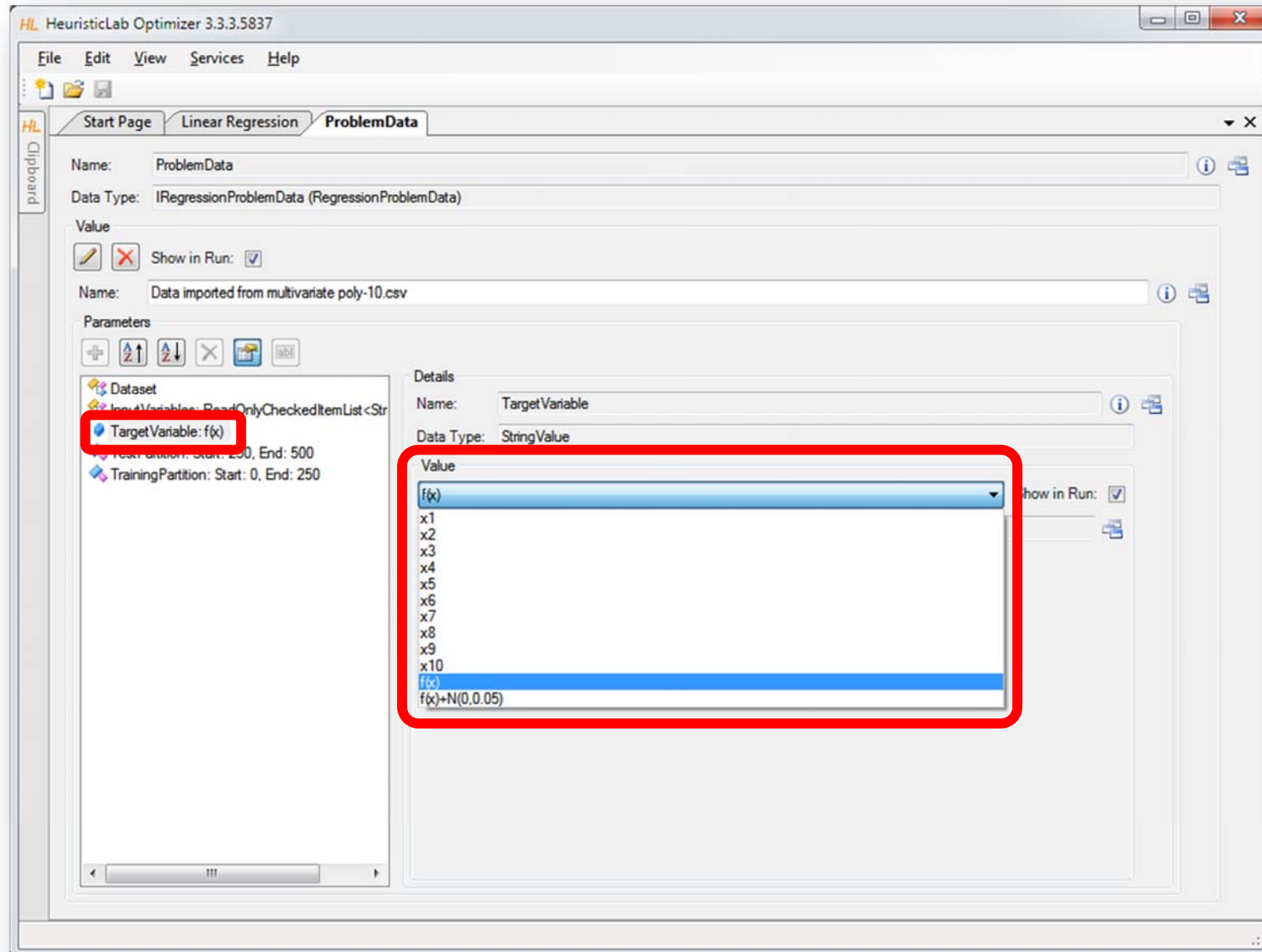
# Inspect Imported Data



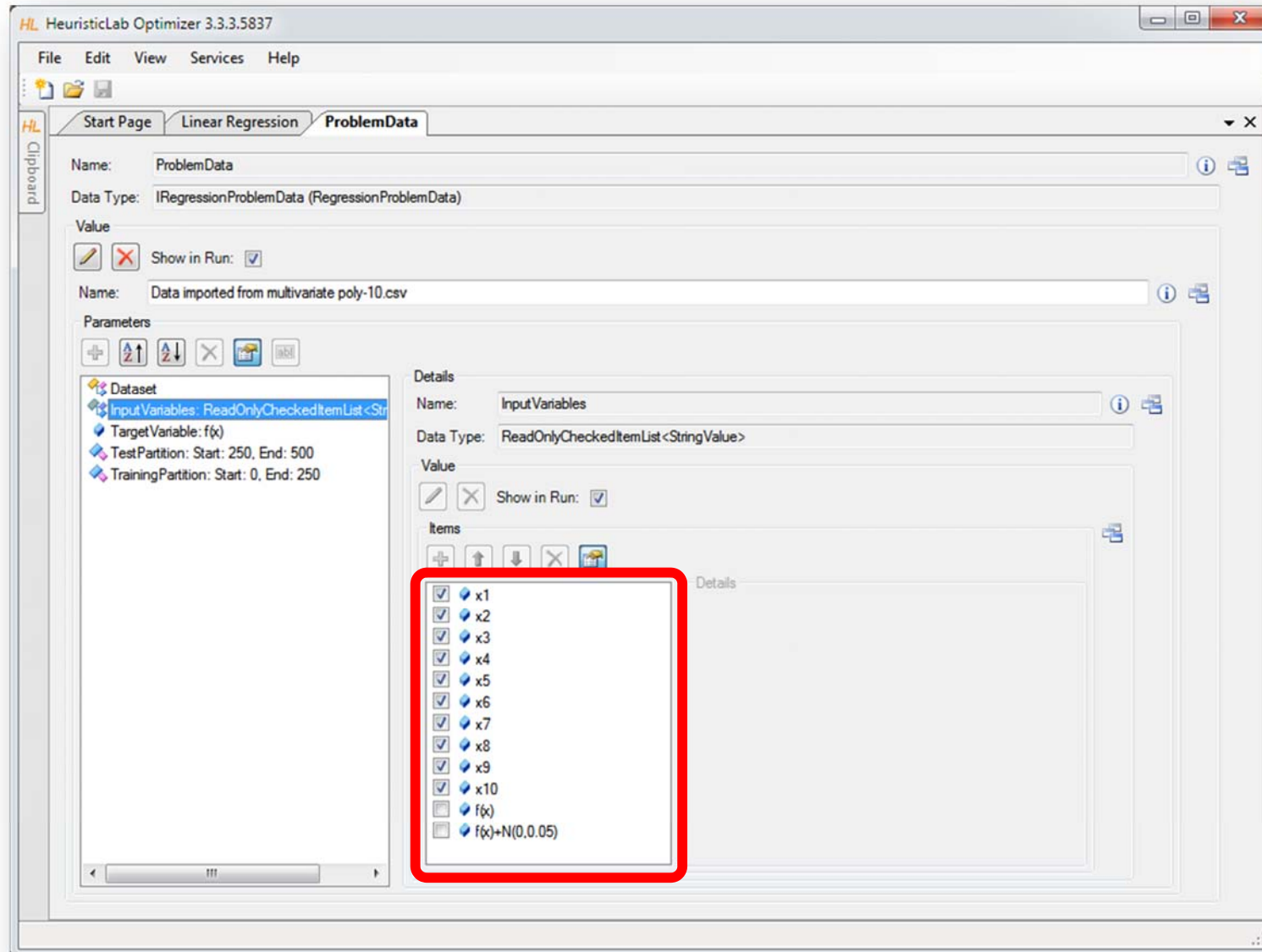
The screenshot shows the HeuristicLab Optimizer interface. The 'ProblemData' tab is active, and the 'Dataset' component is highlighted with a red box. The 'Dataset' details panel shows the following data:

	x1	x2	x3	x4	x5	x6	x7	x8	x9	x10
Row 1	-0.97...	0.26...	0.97...	0.35...	0.24...	-0.92...	-0.99...	0.63...	0.47...	0.417...
Row 2	-0.74...	-0.11...	0.73...	0.86...	-0.72...	0.03...	-0.05...	0.80...	0.25...	0.890...
Row 3	-0.44...	0.53...	0.33...	-0.07...	0.05...	0.80...	0.91...	0.01...	0.33...	-0.999...
Row 4	0.04...	-0.74...	0.51...	0.79...	-0.00...	0.41...	0.63...	0.01...	-0.02...	-0.855...
Row 5	0.51...	0.89...	-0.89...	0.39...	0.56...	0.81...	0.56...	0.81...	-0.94...	0.988...
Row 6	-0.89...	0.34...	0.66...	0.85...	0.01...	0.28...	0.32...	0.55...	-0.07...	-0.775...
Row 7	-0.00...	0.50...	-0.87...	-0.48...	0.62...	0.86...	-0.99...	0.59...	-0.71...	0.322...
Row 8	0.67...	-0.35...	0.14...	0.04...	-0.28...	-0.26...	0.49...	-0.01...	-0.08...	-0.235...

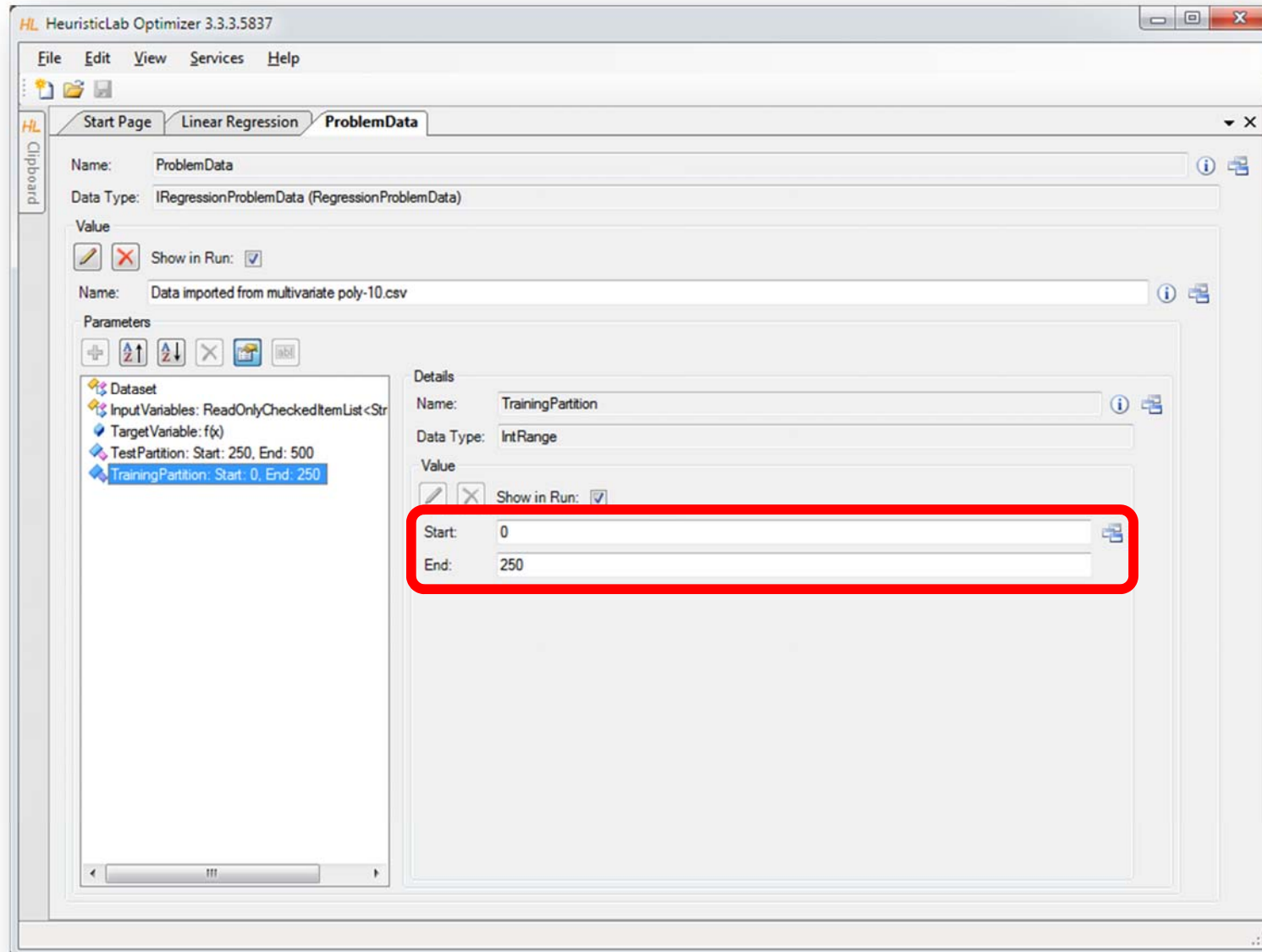
# Set Target Variable



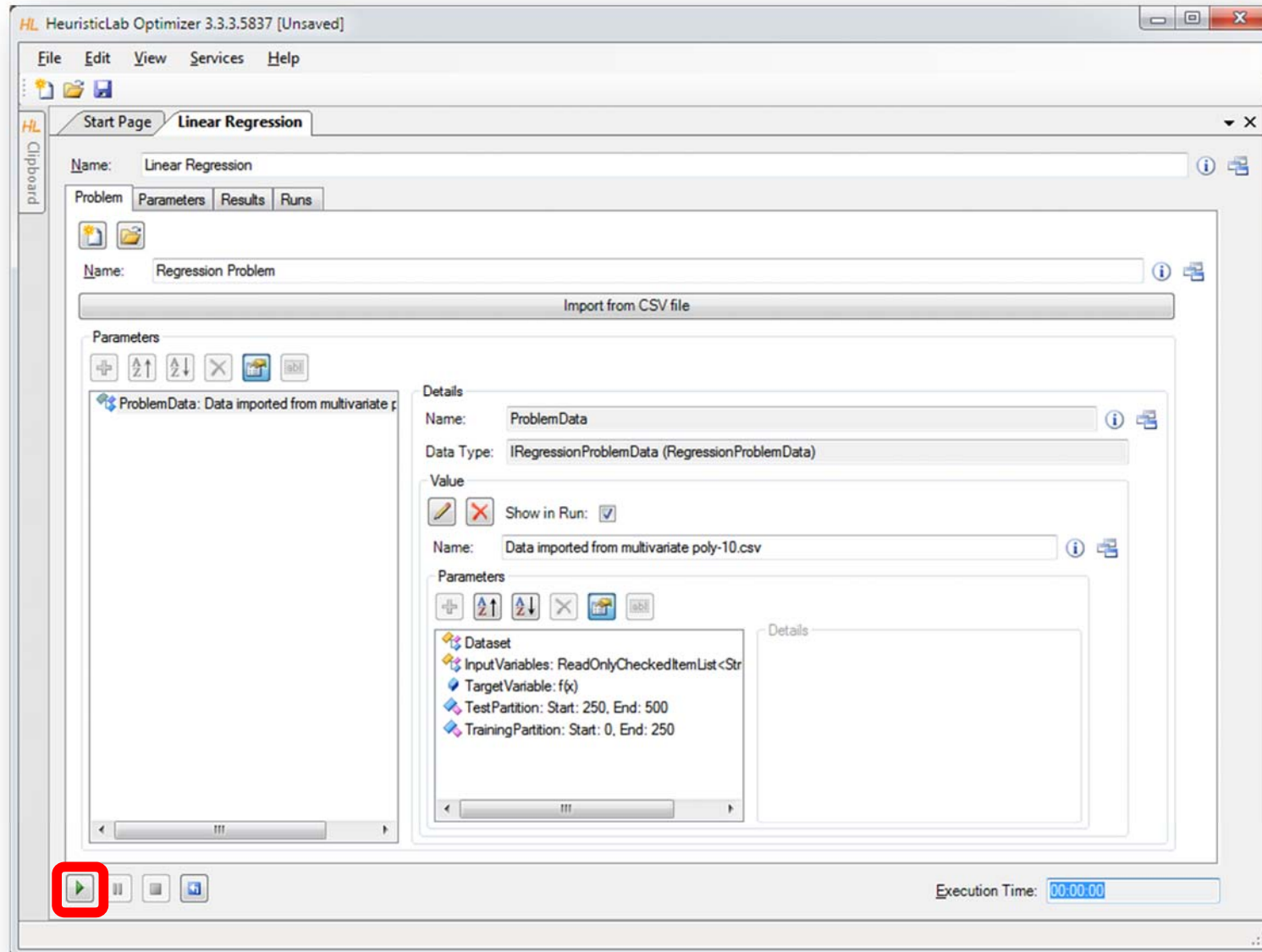
# Select Input Variables



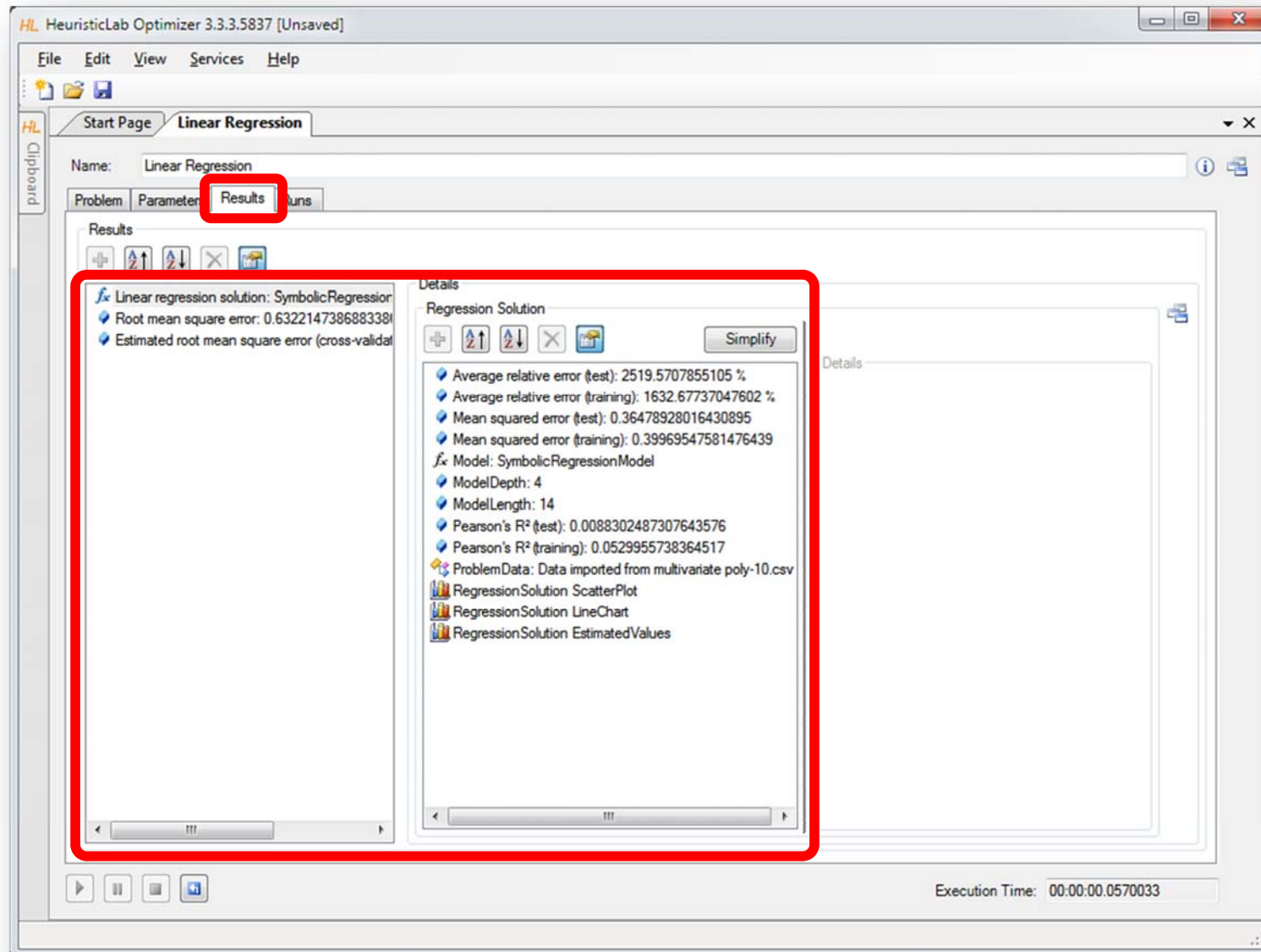
# Configure Training and Test Partitions



# Run Linear Regression

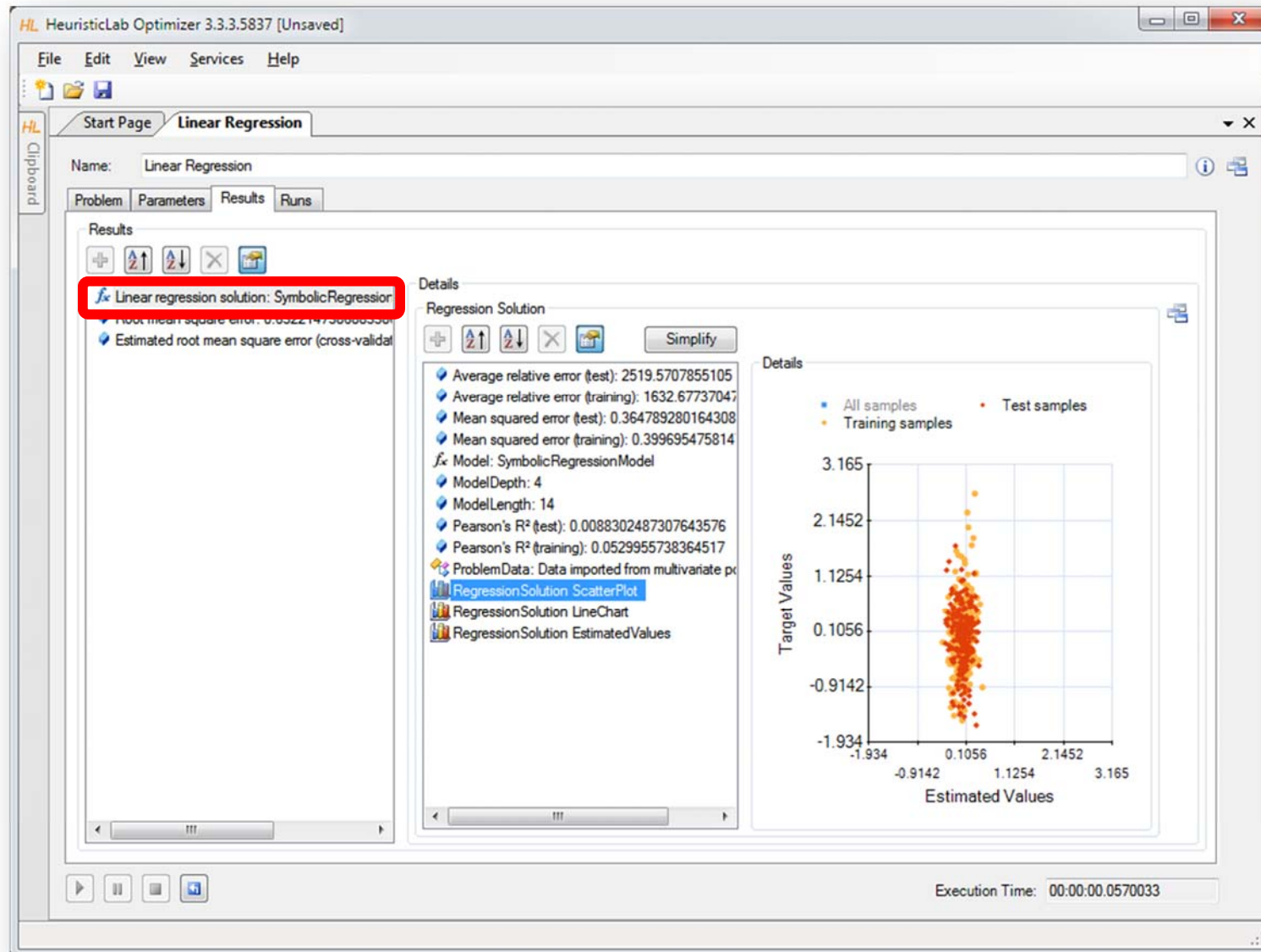


# Inspect Results

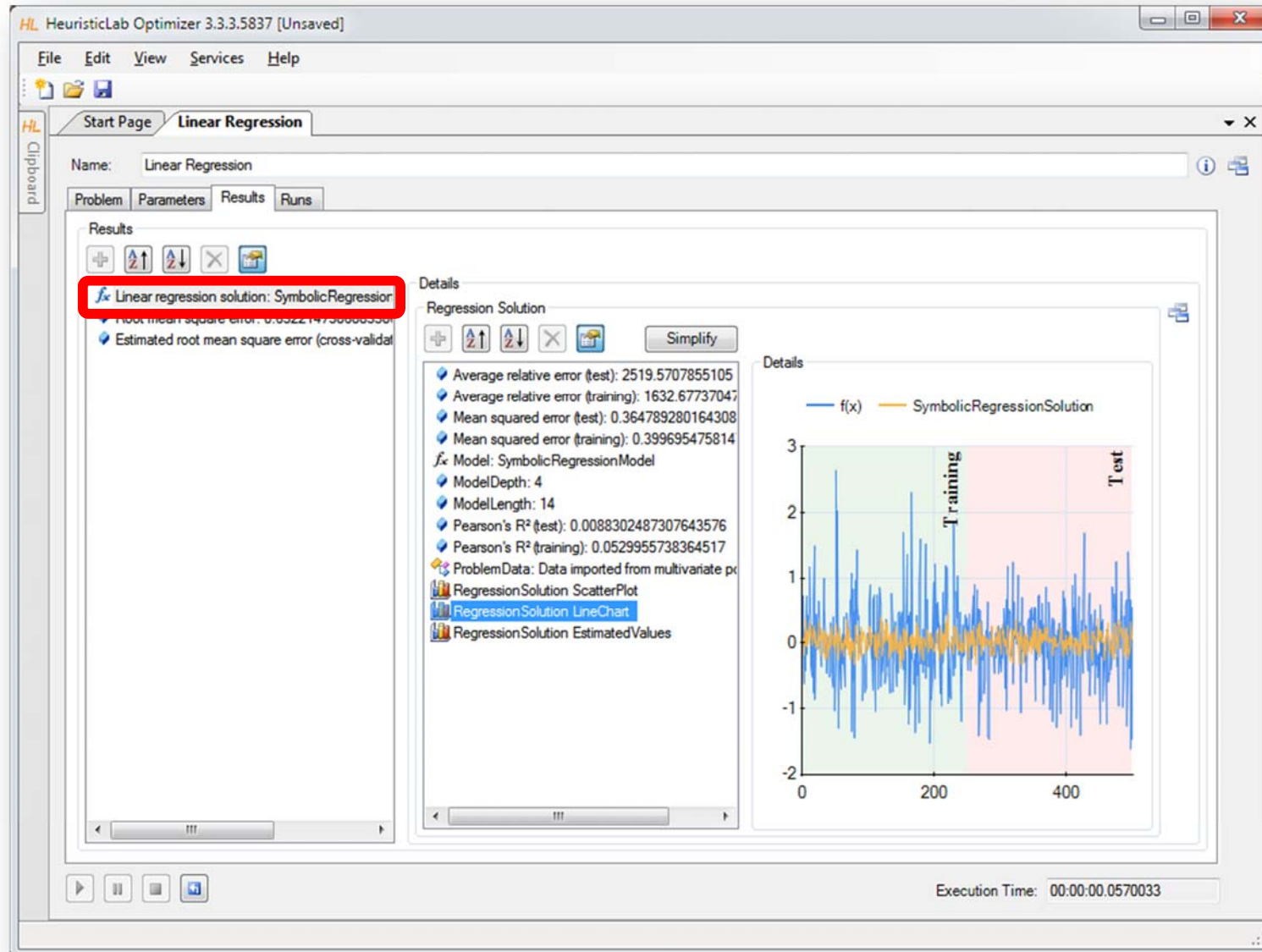




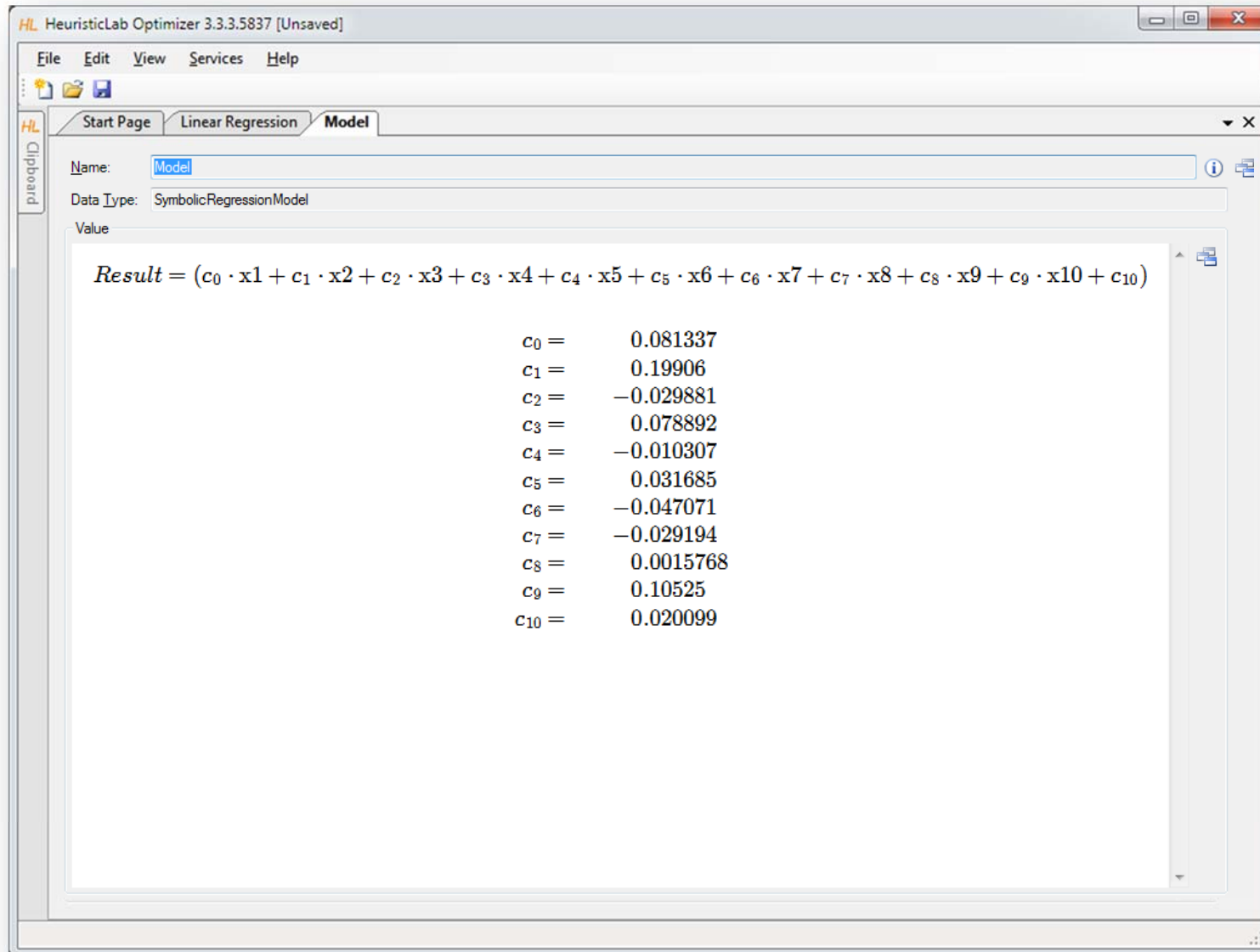
# Inspect Scatterplot of Predicted and Target Values



# Inspect Linechart



# Inspect the Model



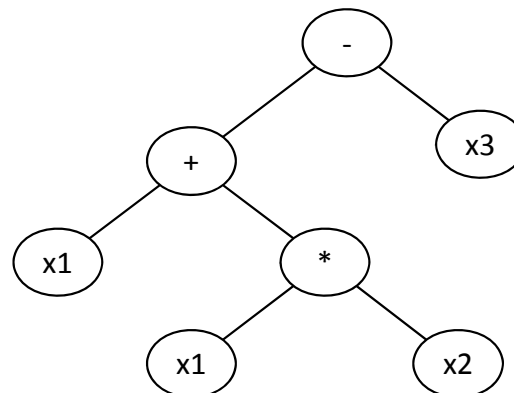
The screenshot shows the HeuristicLab Optimizer interface. The window title is "HL HeuristicLab Optimizer 3.3.3.5837 [Unsaved]". The menu bar includes "File", "Edit", "View", "Services", and "Help". The main area has tabs for "Start Page", "Linear Regression", and "Model". The "Model" tab is active, showing a "Name" field with "Model" and a "Data Type" of "SymbolicRegressionModel". The "Value" field displays the following linear regression equation and its coefficients:

$$\text{Result} = (c_0 \cdot x_1 + c_1 \cdot x_2 + c_2 \cdot x_3 + c_3 \cdot x_4 + c_4 \cdot x_5 + c_5 \cdot x_6 + c_6 \cdot x_7 + c_7 \cdot x_8 + c_8 \cdot x_9 + c_9 \cdot x_{10} + c_{10})$$

$c_0 =$	0.081337
$c_1 =$	0.19906
$c_2 =$	-0.029881
$c_3 =$	0.078892
$c_4 =$	-0.010307
$c_5 =$	0.031685
$c_6 =$	-0.047071
$c_7 =$	-0.029194
$c_8 =$	0.0015768
$c_9 =$	0.10525
$c_{10} =$	0.020099

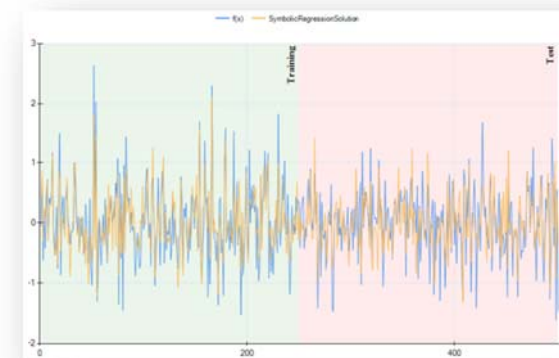
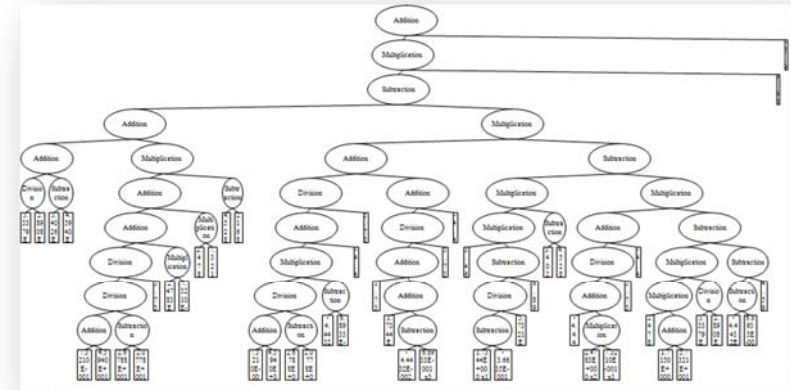
# Symbolic Regression with HeuristicLab

- Linear regression produced an inaccurate model.
- Next: produce a nonlinear symbolic regression model using genetic programming
- Genetic programming
  - evolve variable-length models
  - model representation: symbolic expression tree
  - structure and model parameters are evolved side-by-side
  - white-box models

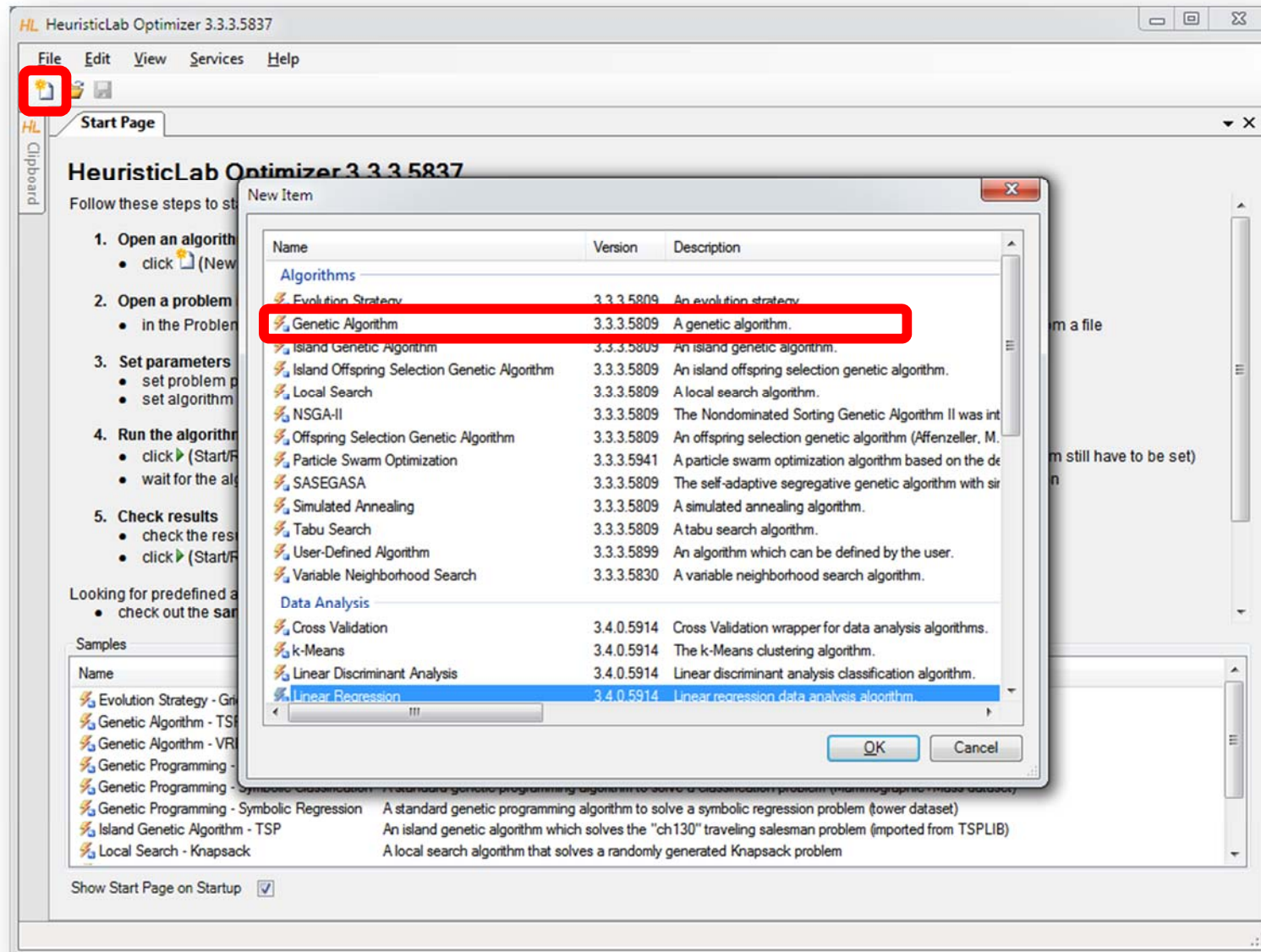


# Symbolic Regression with HeuristicLab

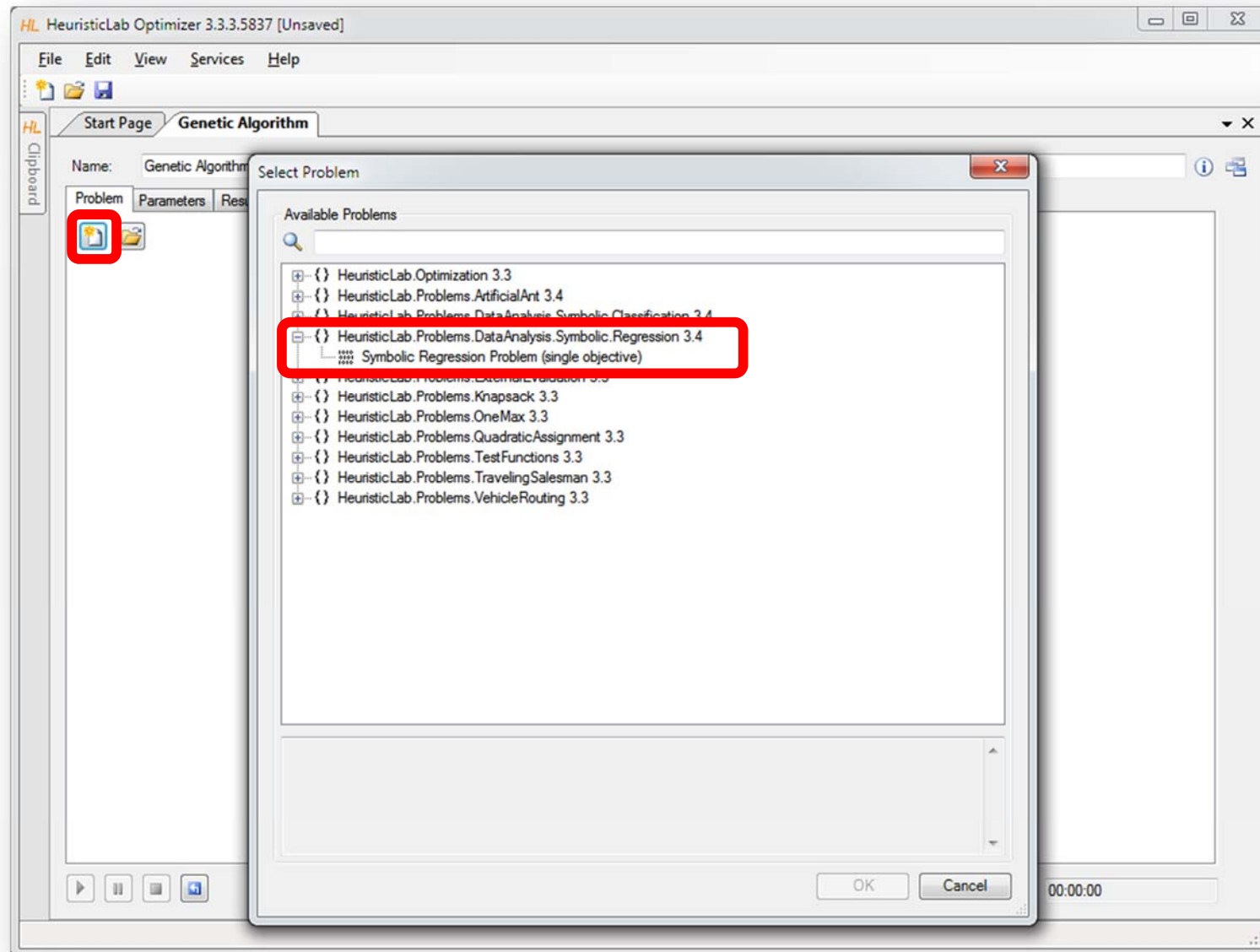
- Demonstration
  - problem configuration
  - function set and terminal set
  - model size constraints
  - Evaluation
- Algorithm configuration
  - selection
  - Mutation
- Analysis of results
  - model accuracy
  - model structure and parameters



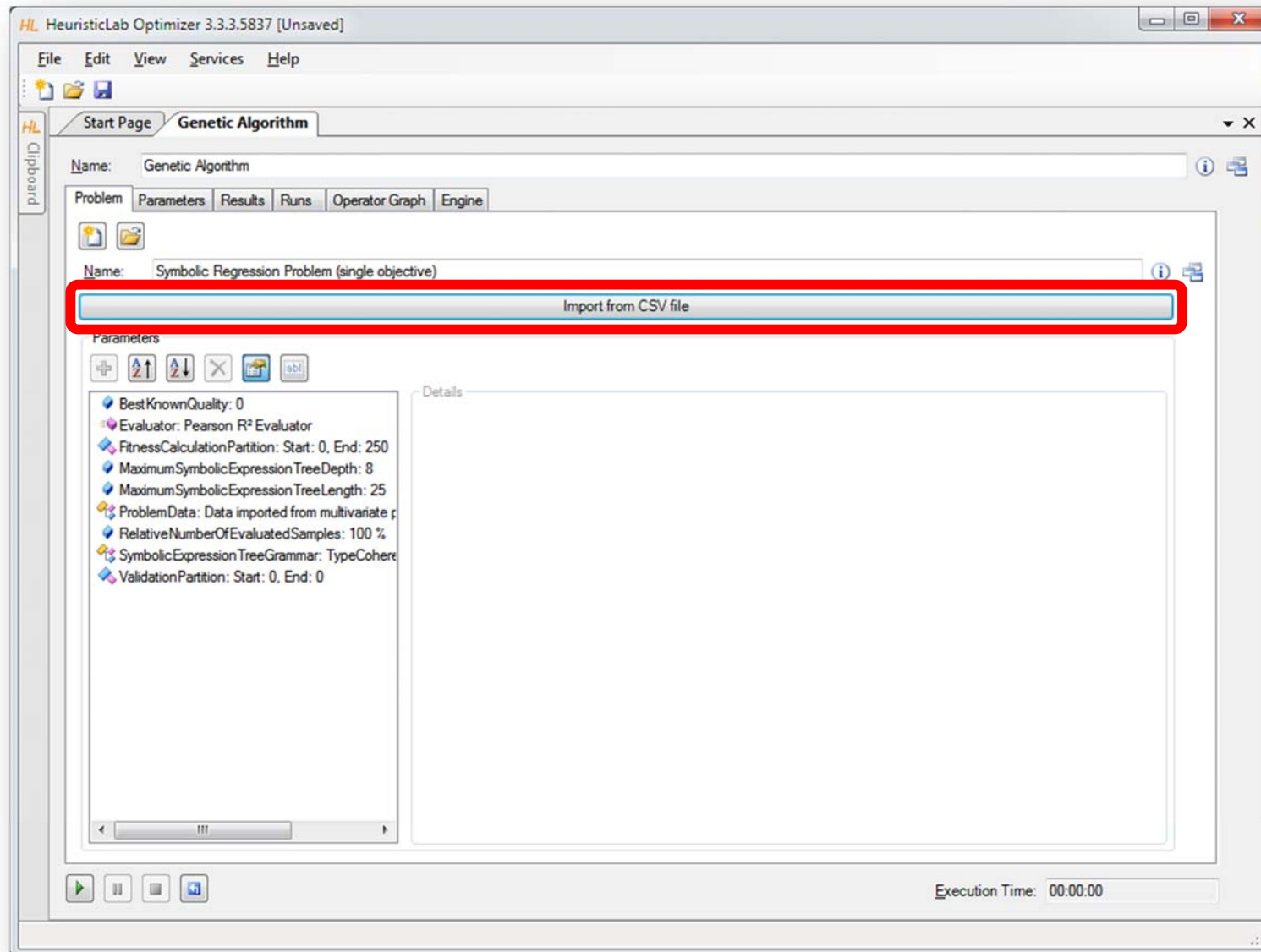
# Create New Genetic Algorithm



# Create New Symbolic Regression Problem

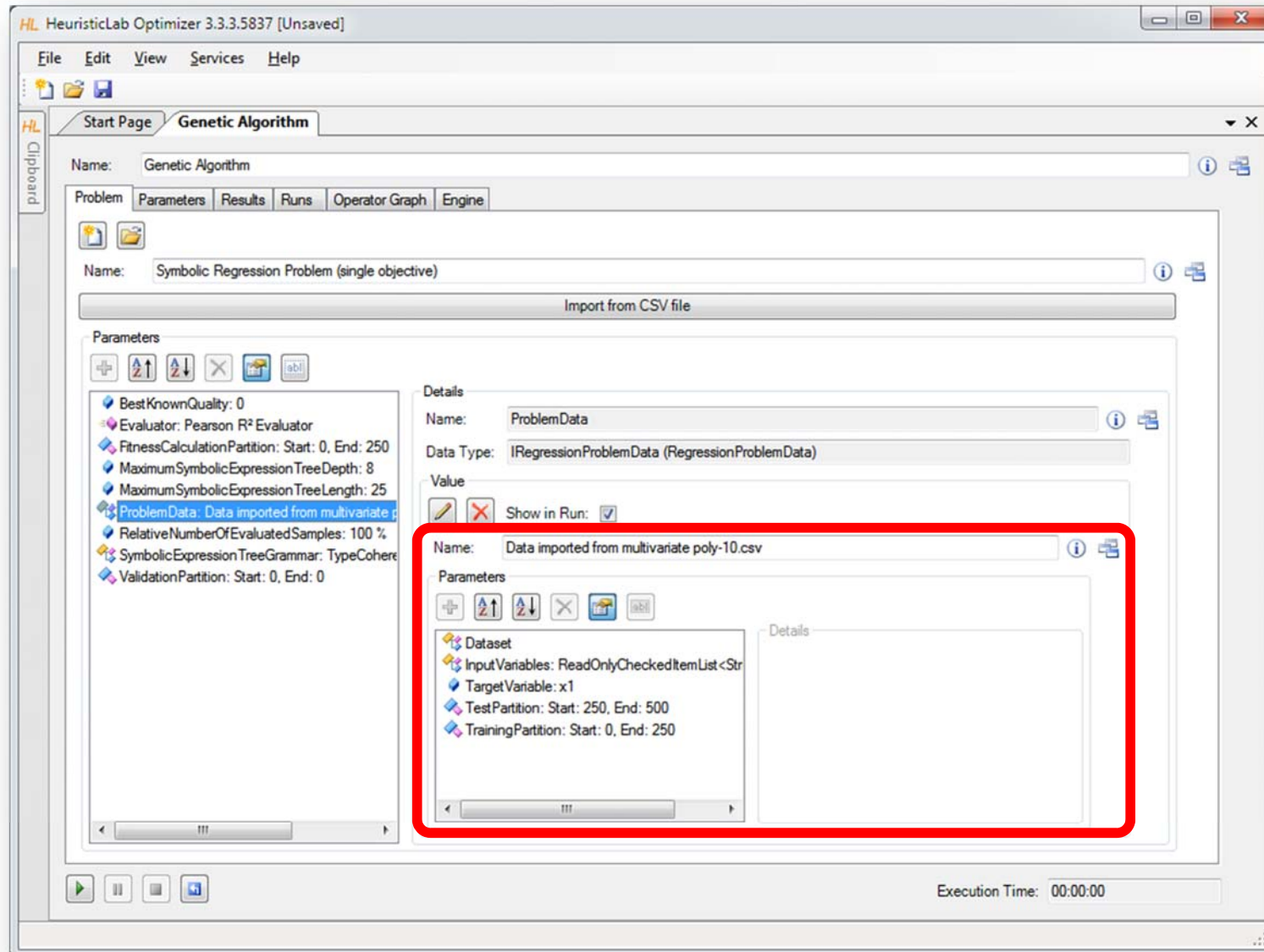


# Import Data

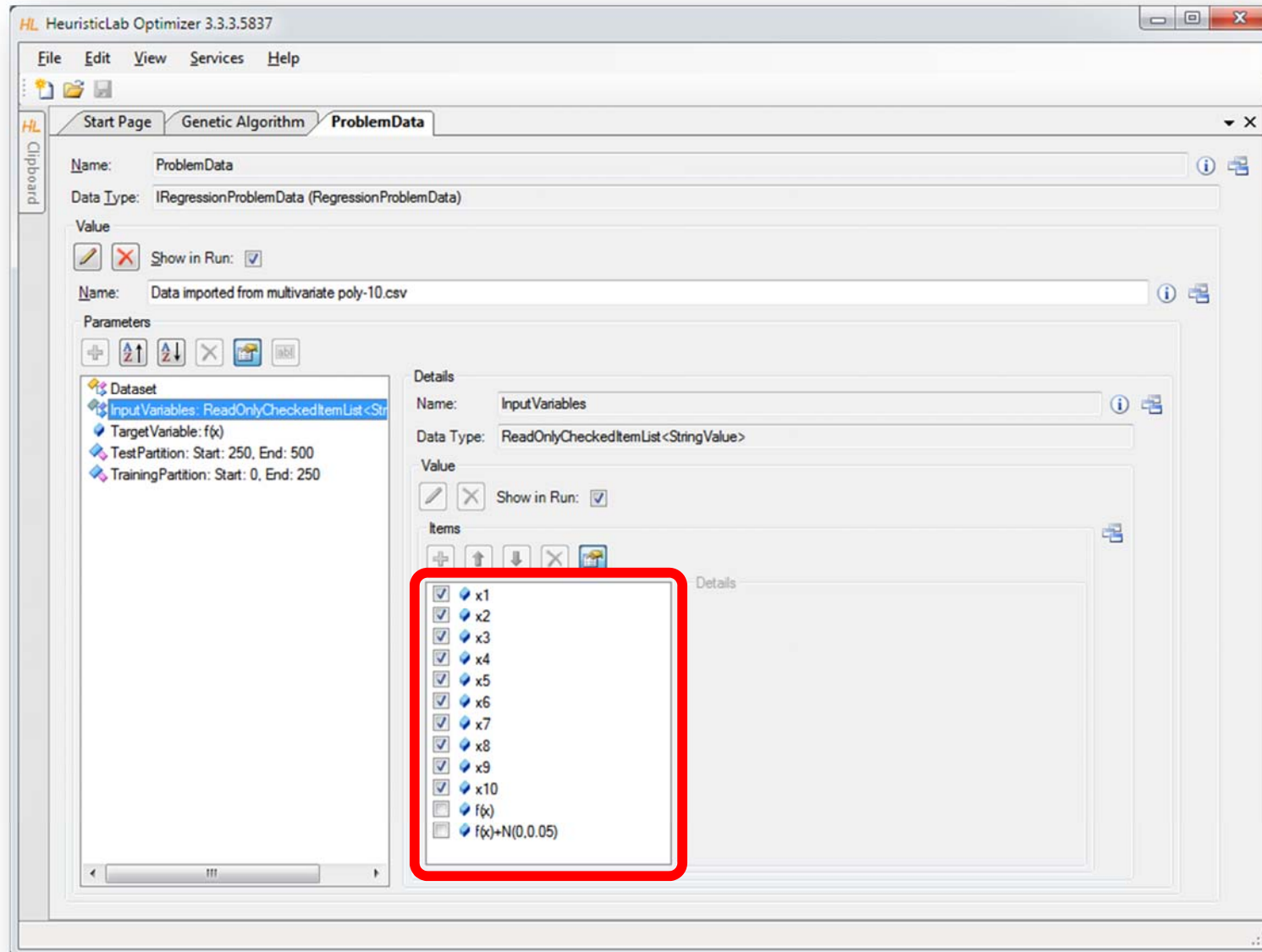




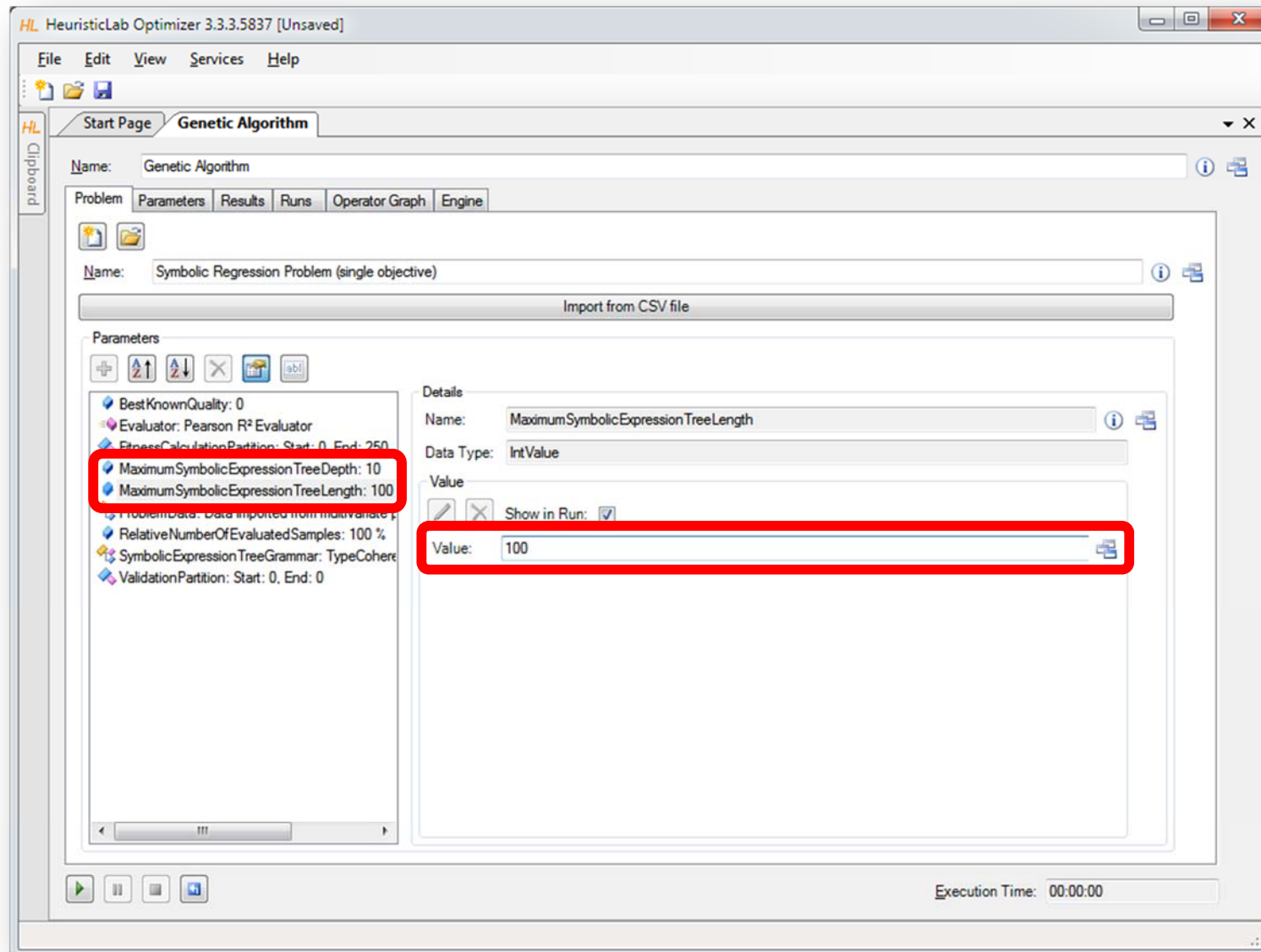
# Inspect Data and Configure Dataset



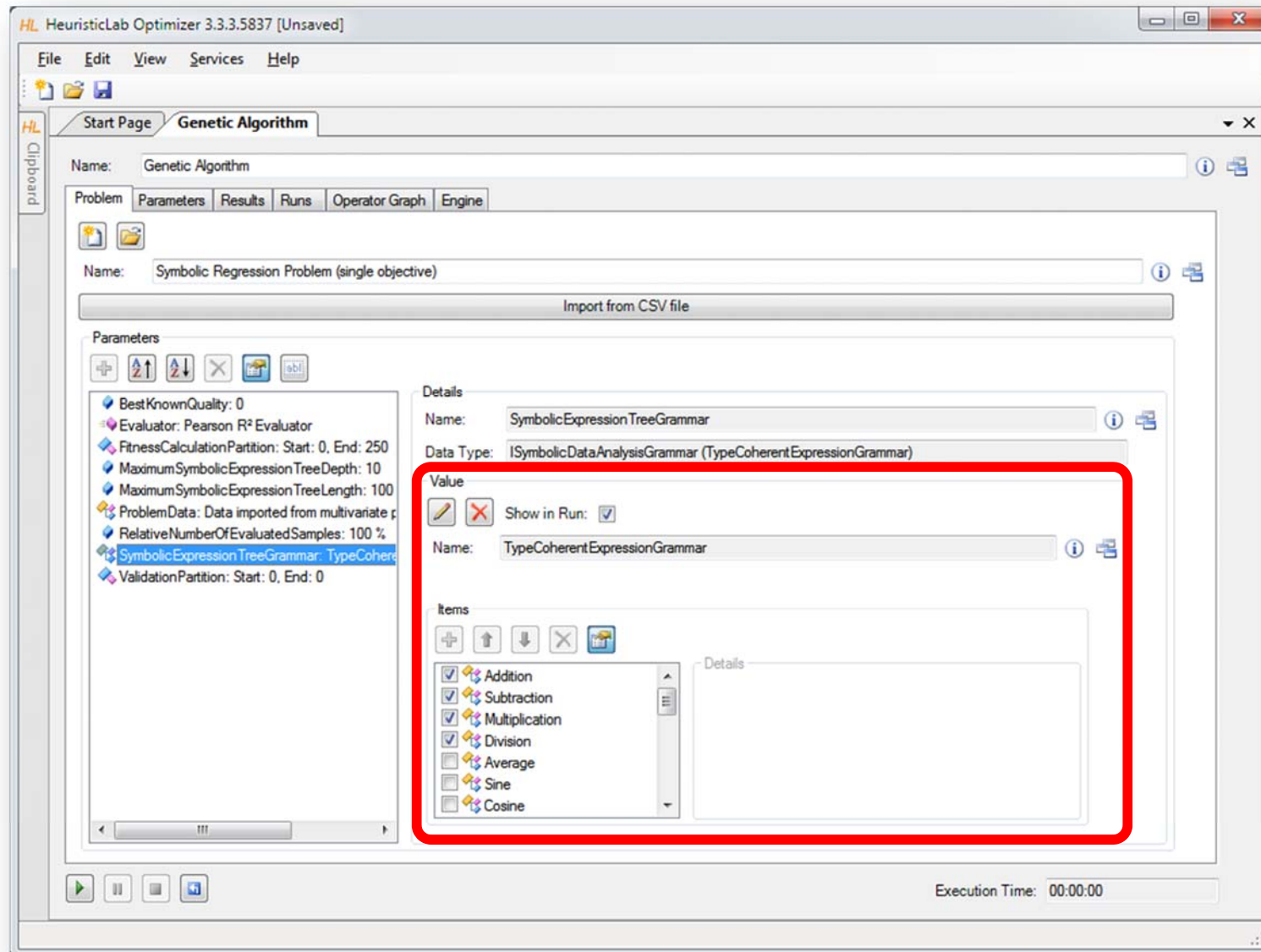
# Set Target and Input Variables



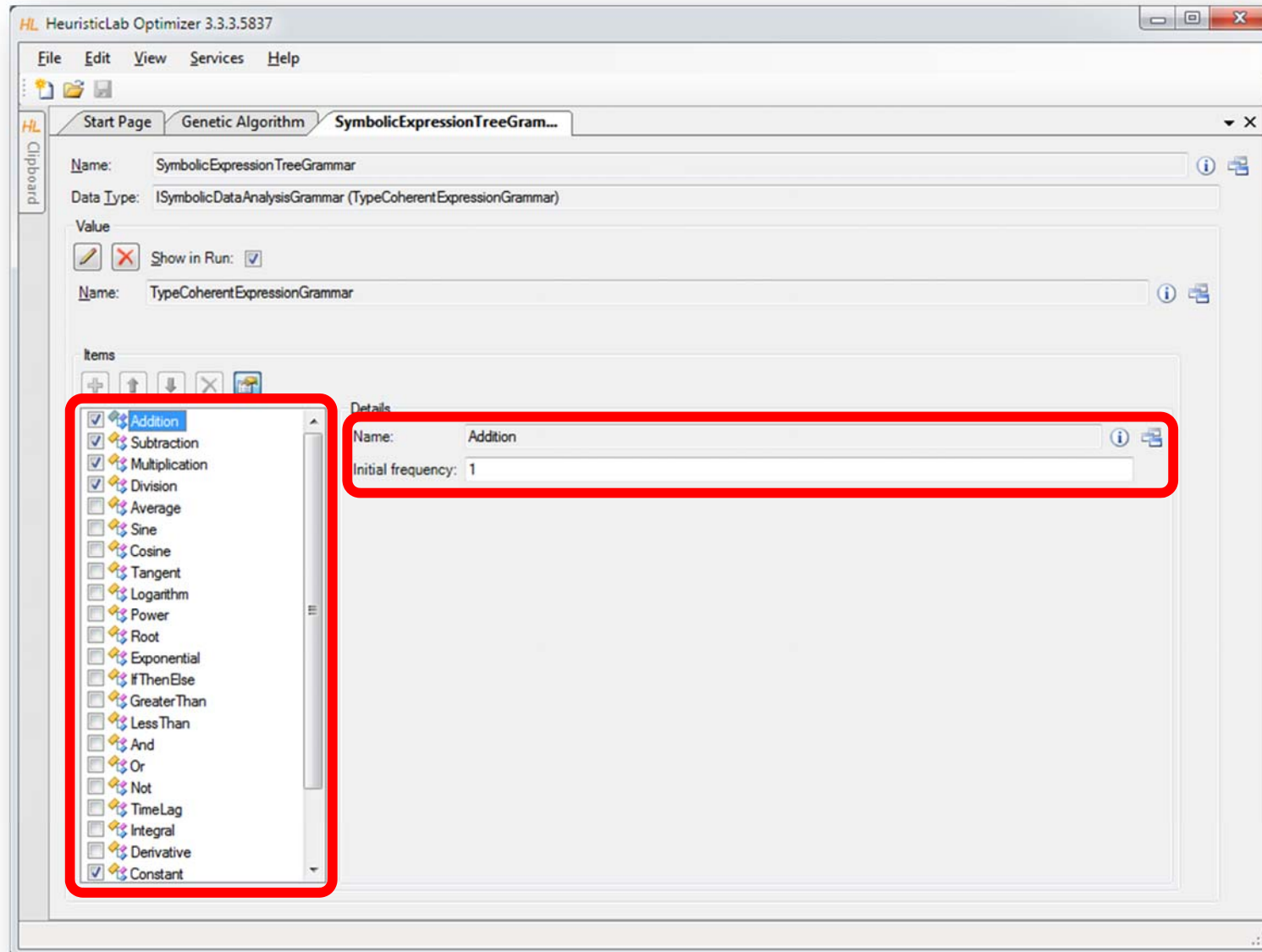
# Configure Maximal Model Depth and Length



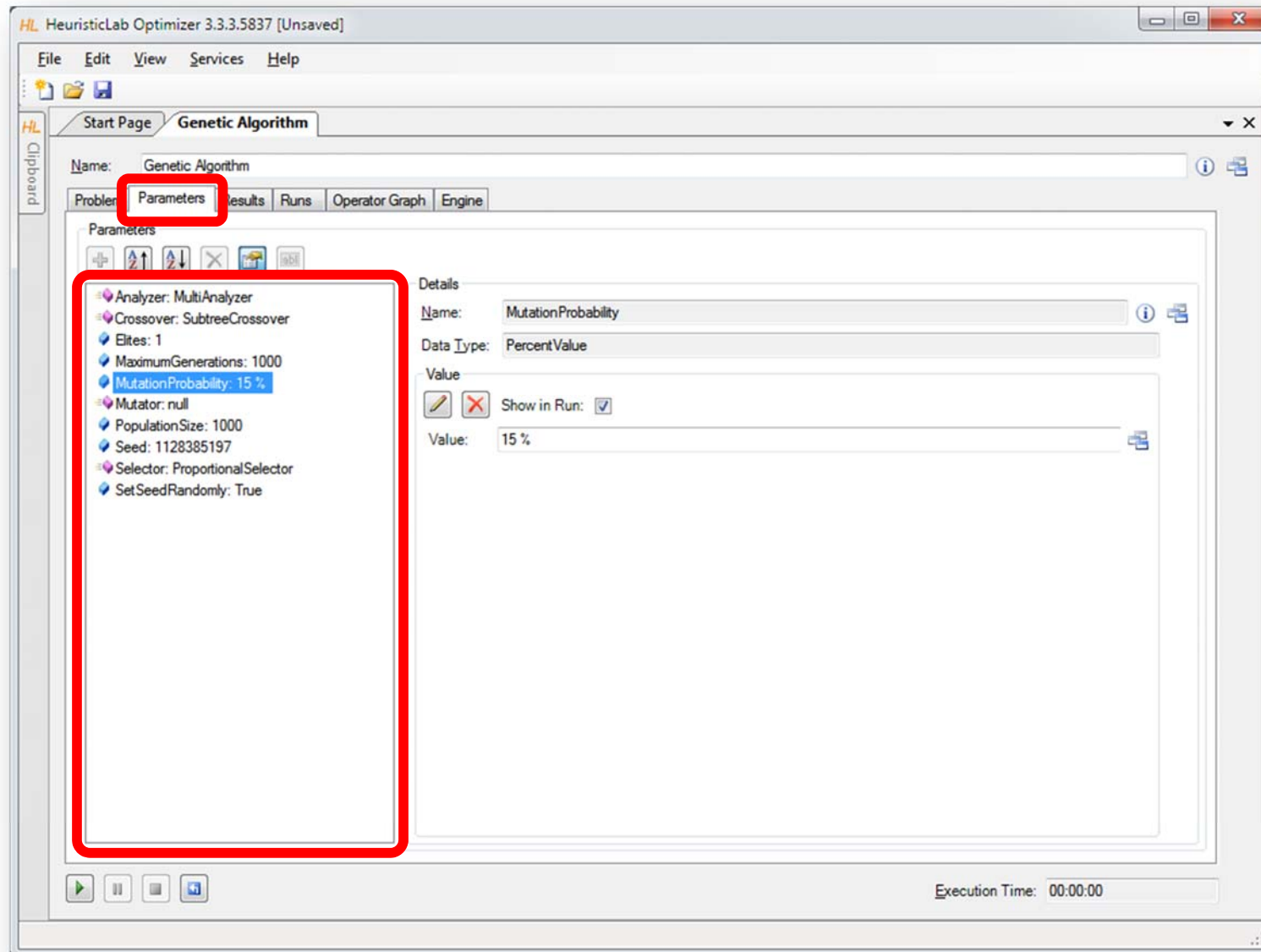
# Configure Function Set (Grammar)



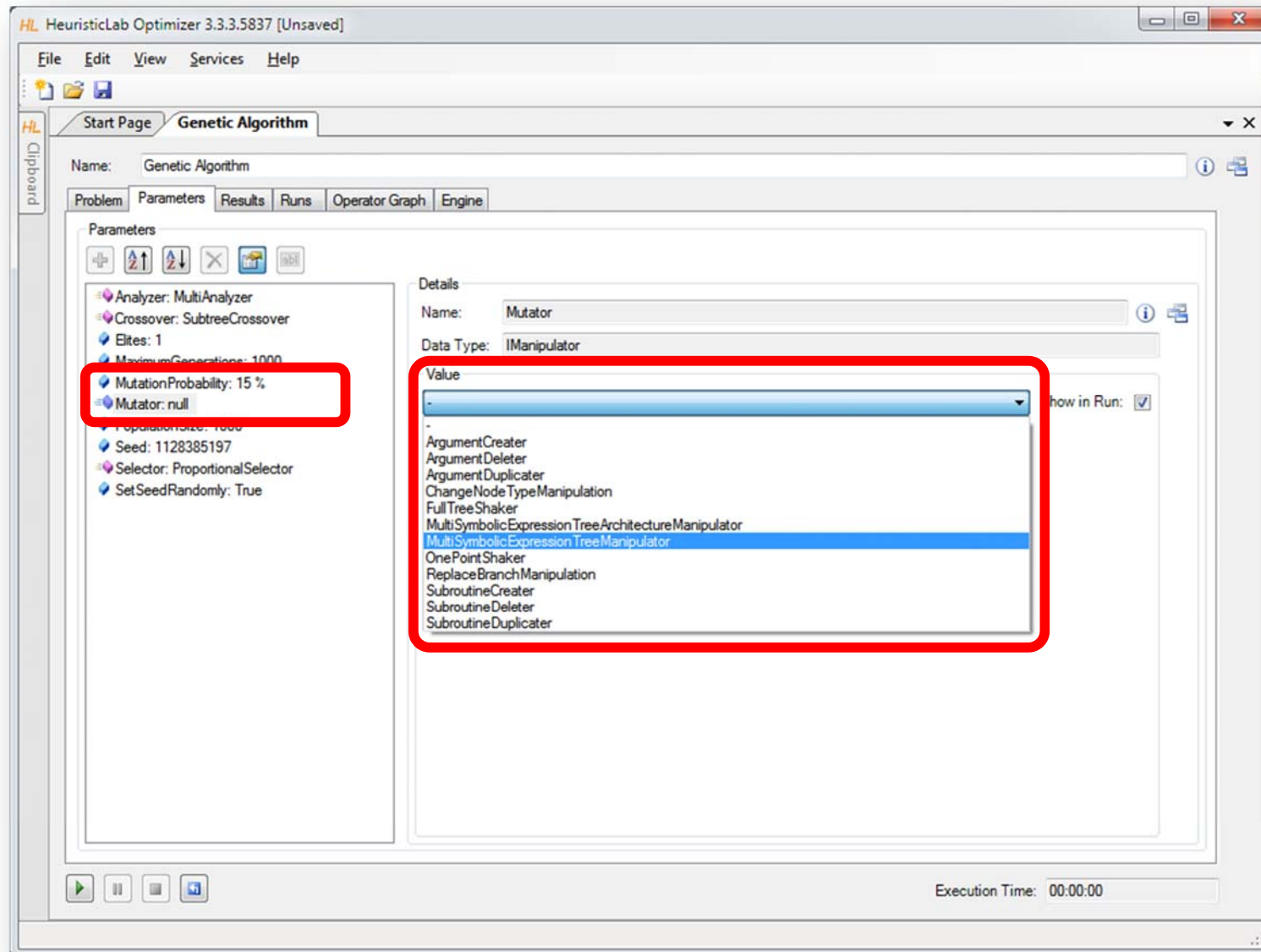
# Configure Function Set (Grammar)



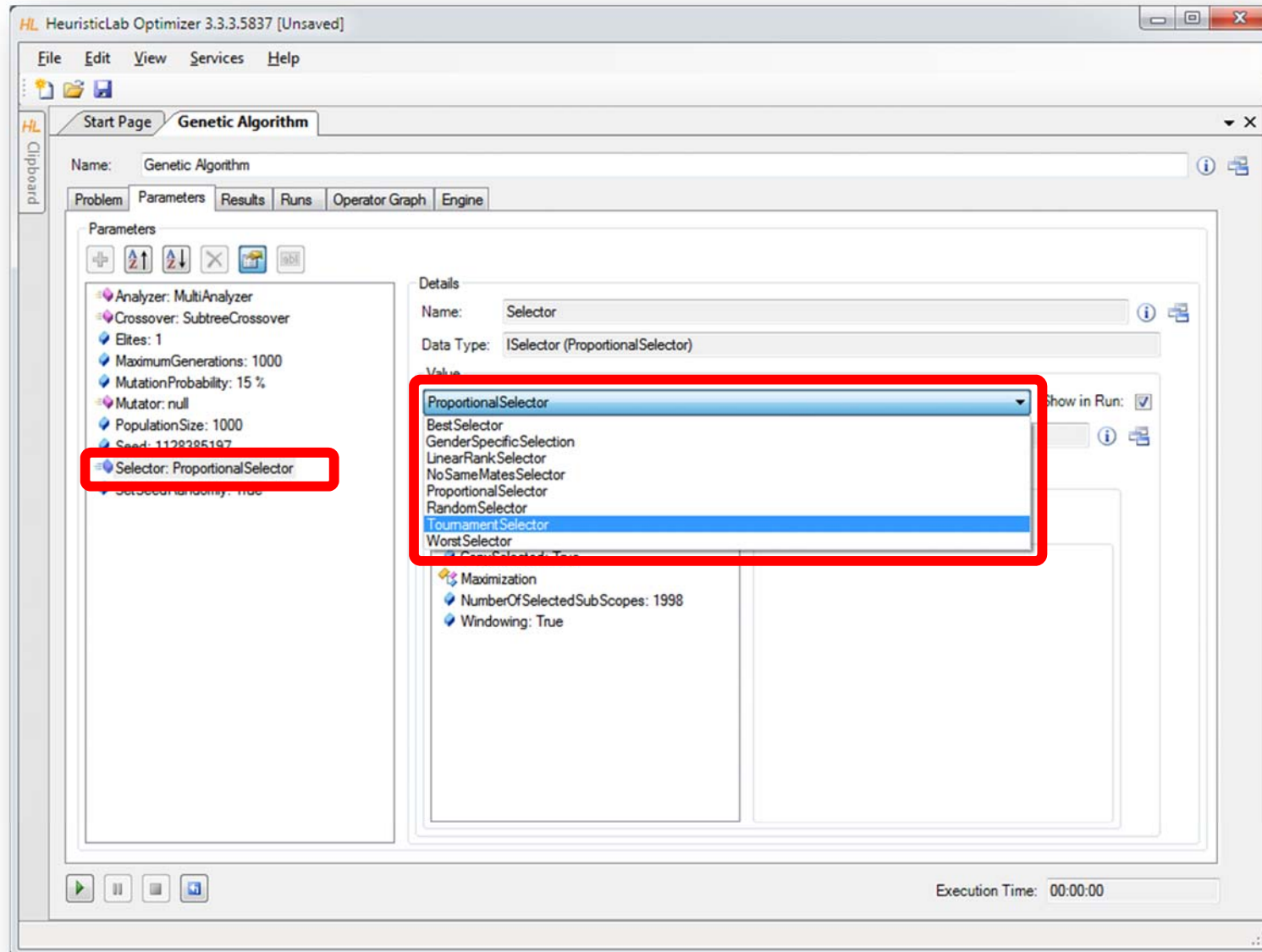
# Configure Algorithm Parameters



# Configure Mutation Operator

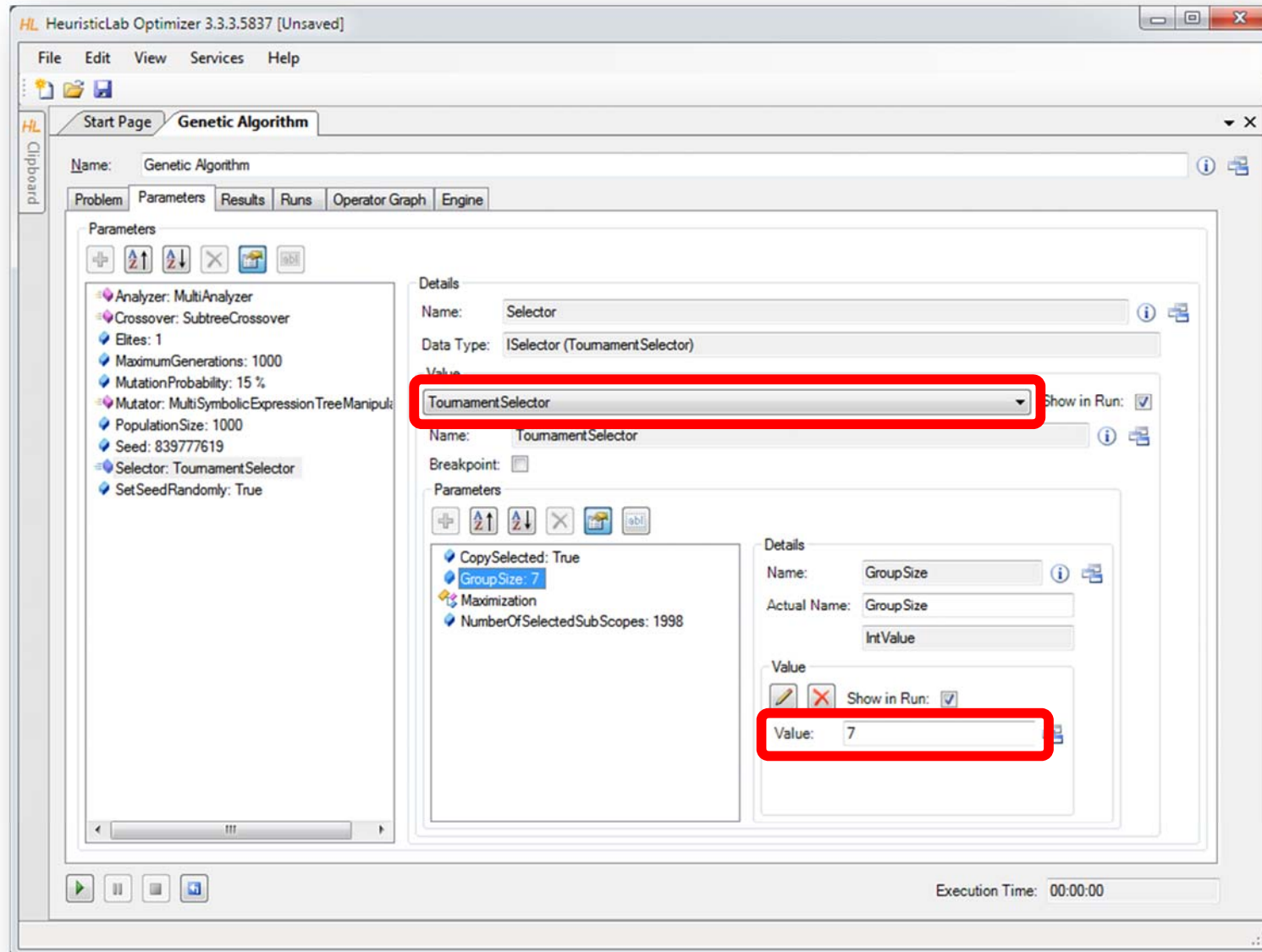


# Configure Selection Operator

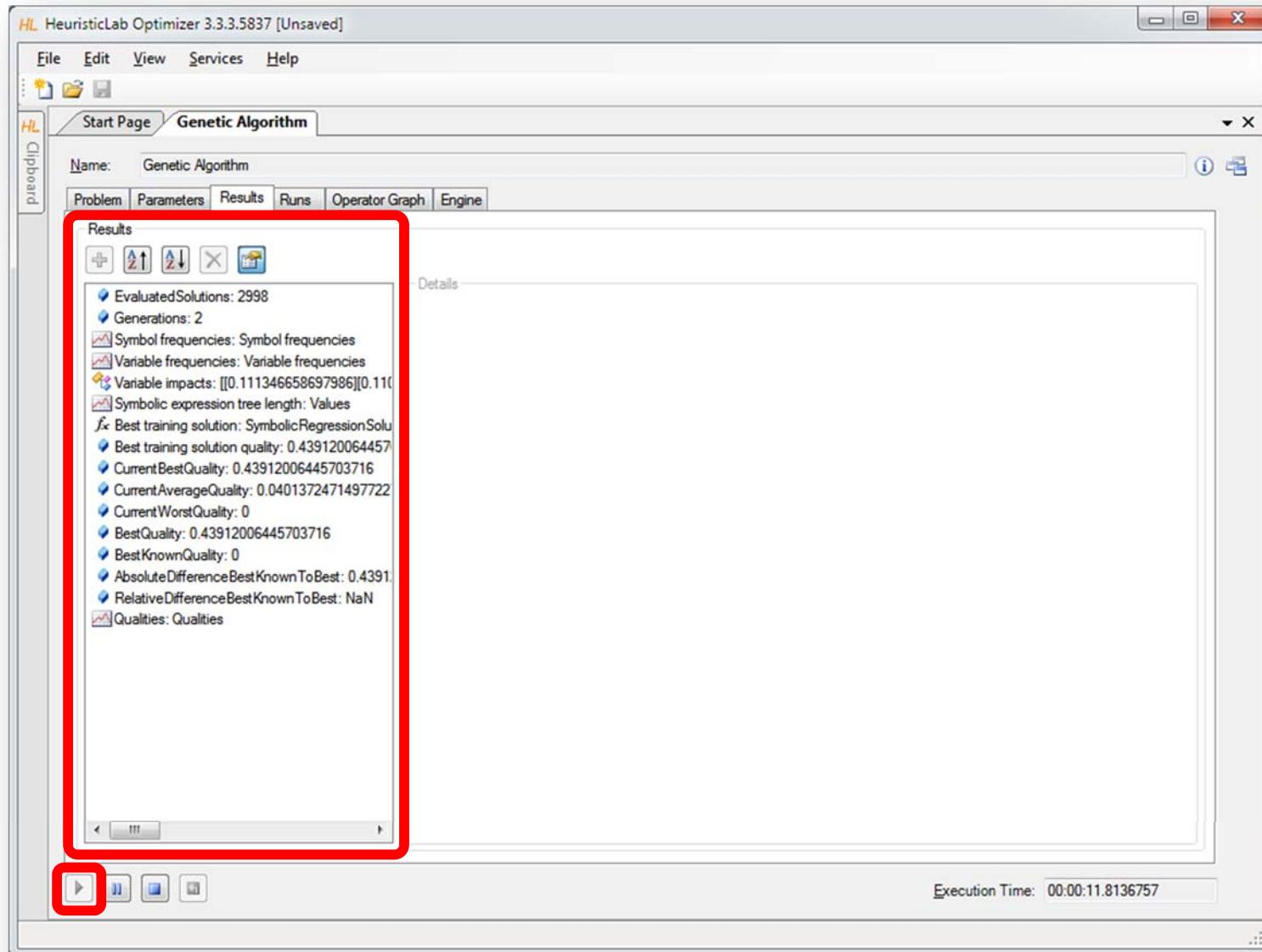




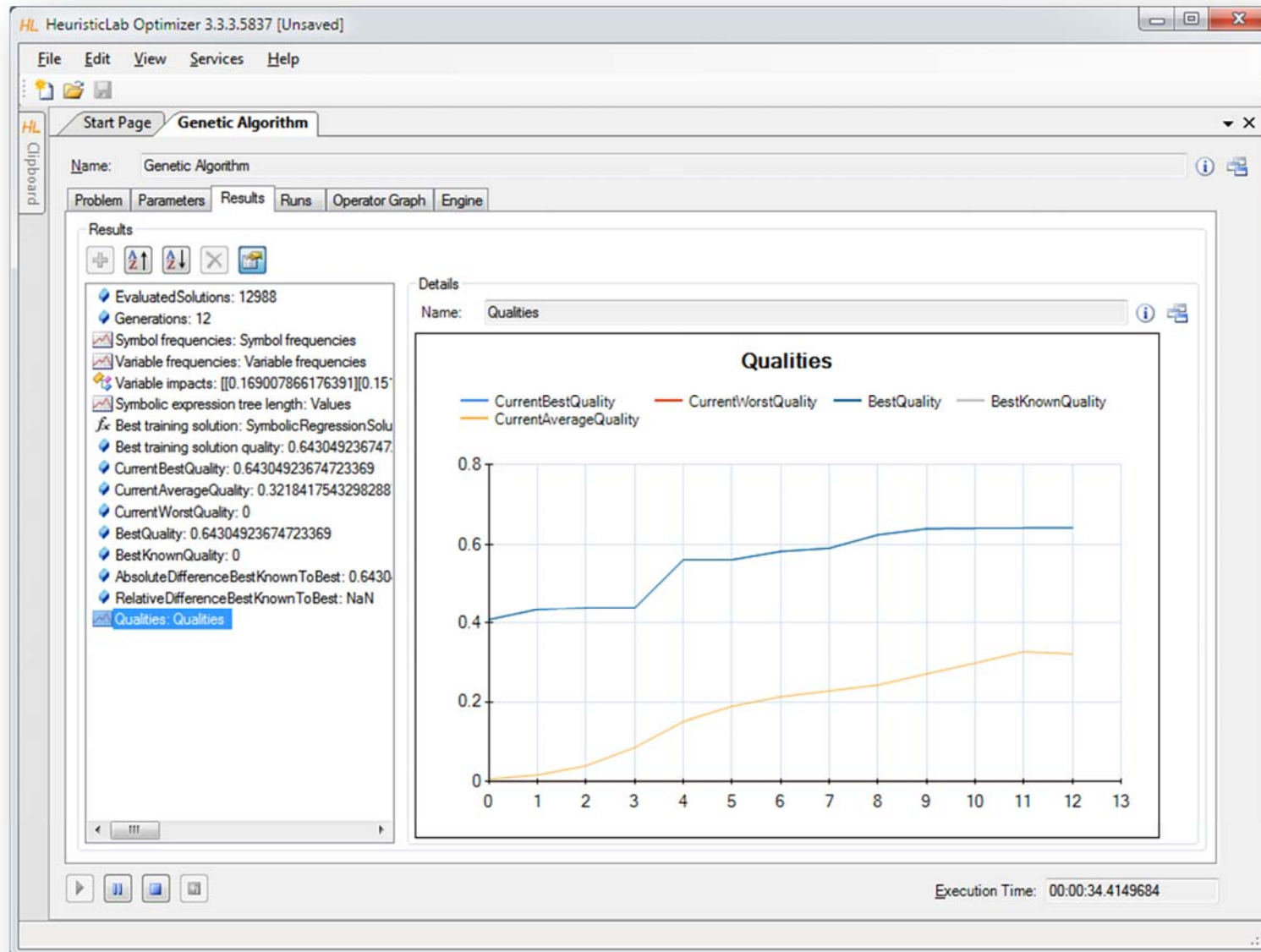
# Configure Tournament Group Size



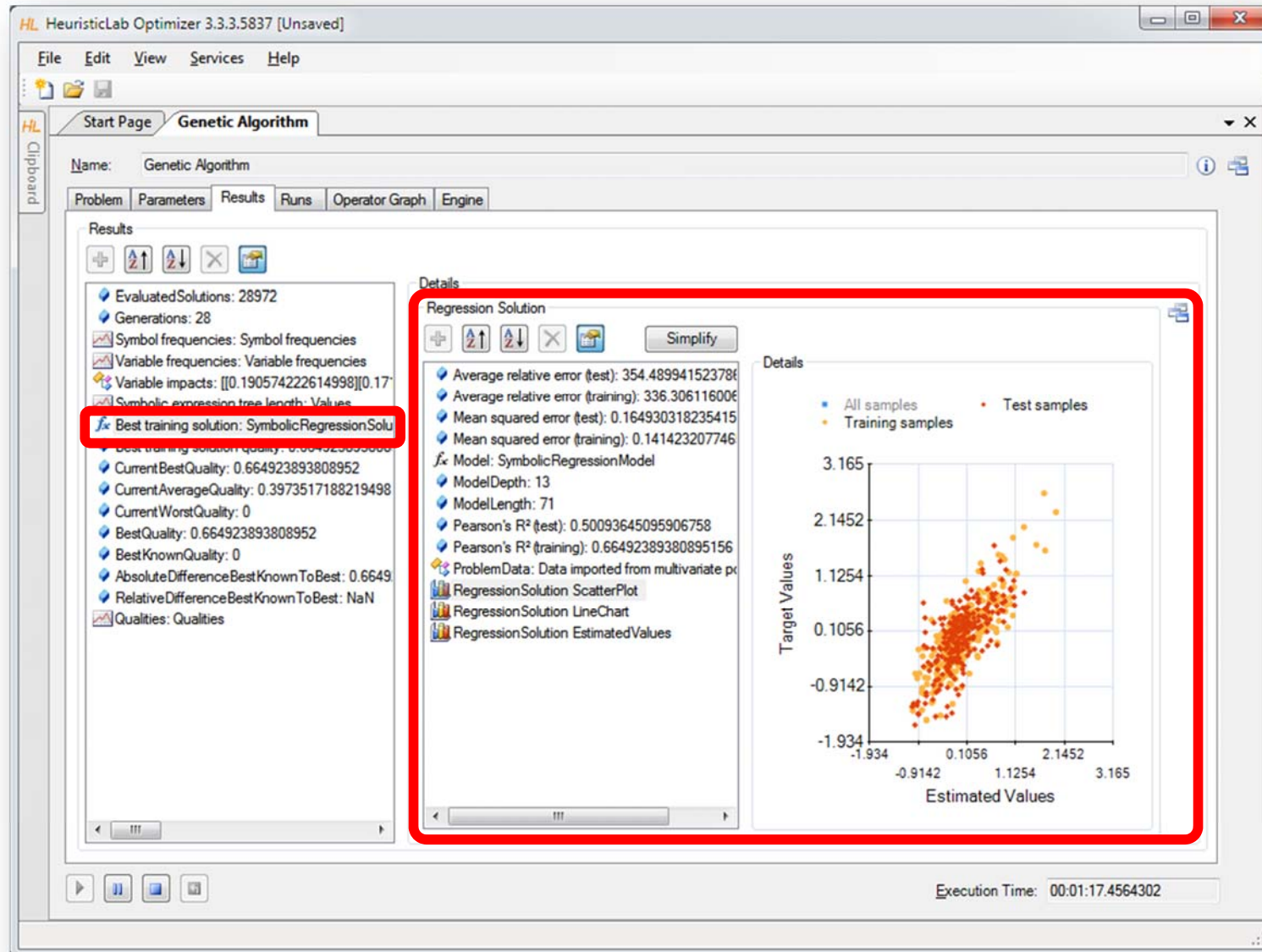
# Start Algorithm and Inspect Results



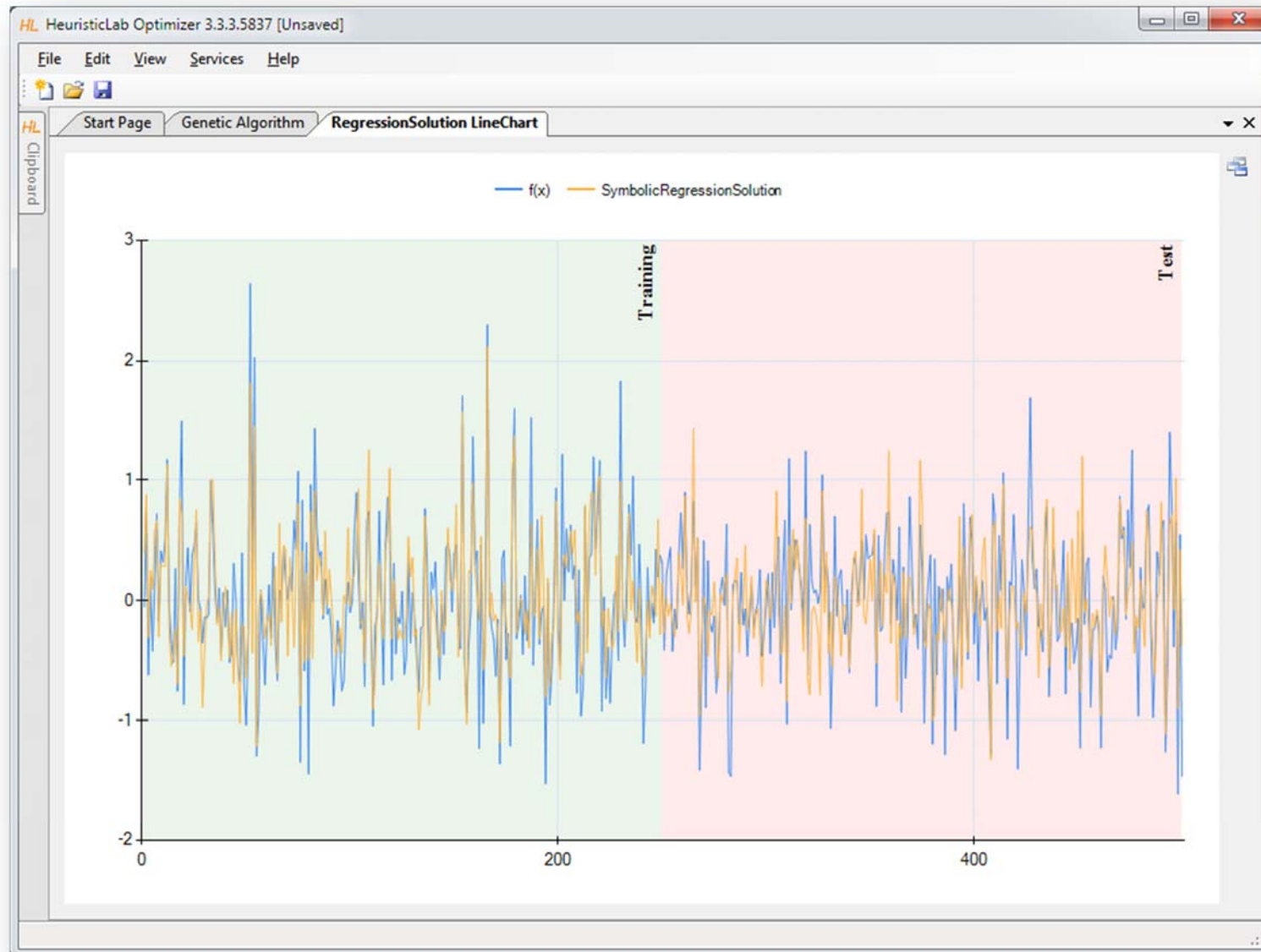
# Inspect Quality Chart



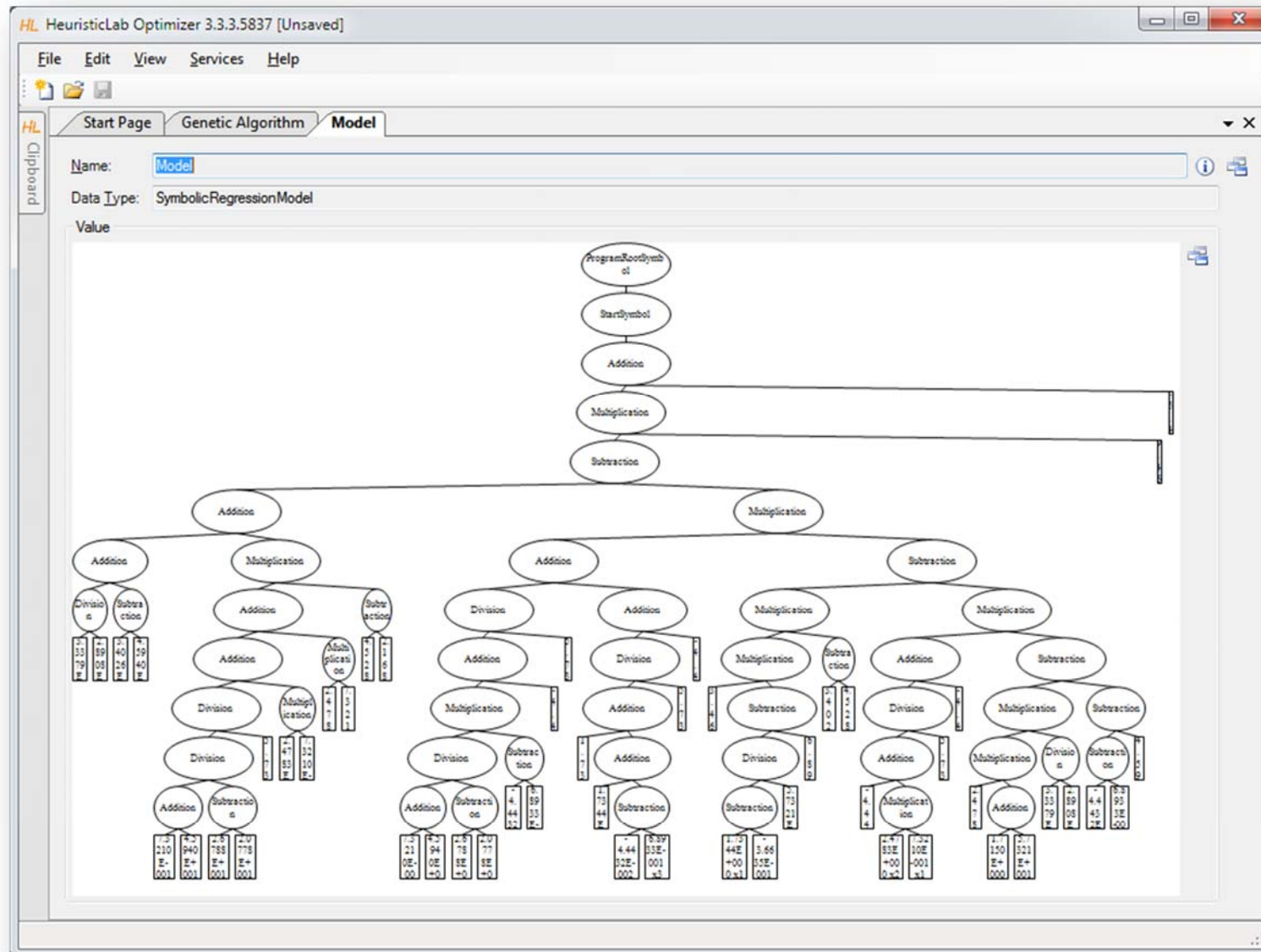
# Inspect Best Model on Training Partition



# Inspect Linechart of Best Model on Training Partition

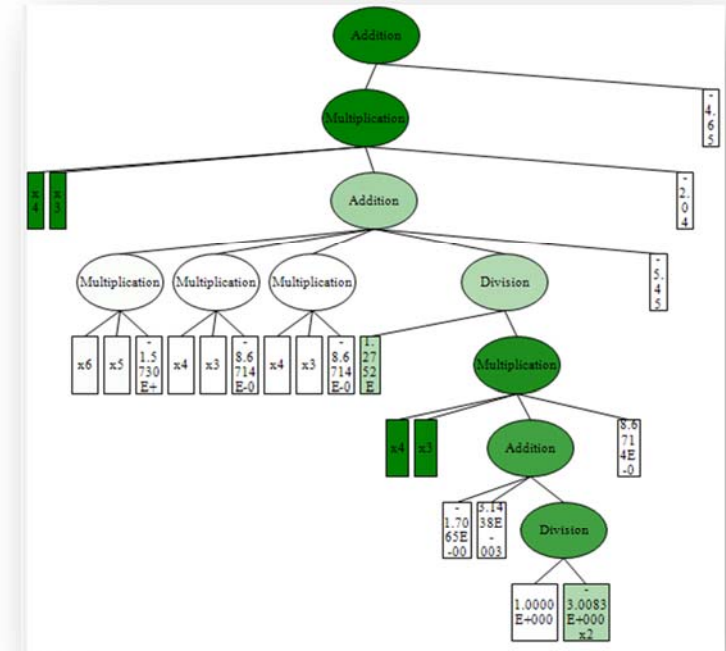


# Inspect Structure of Best Model on Training Partition



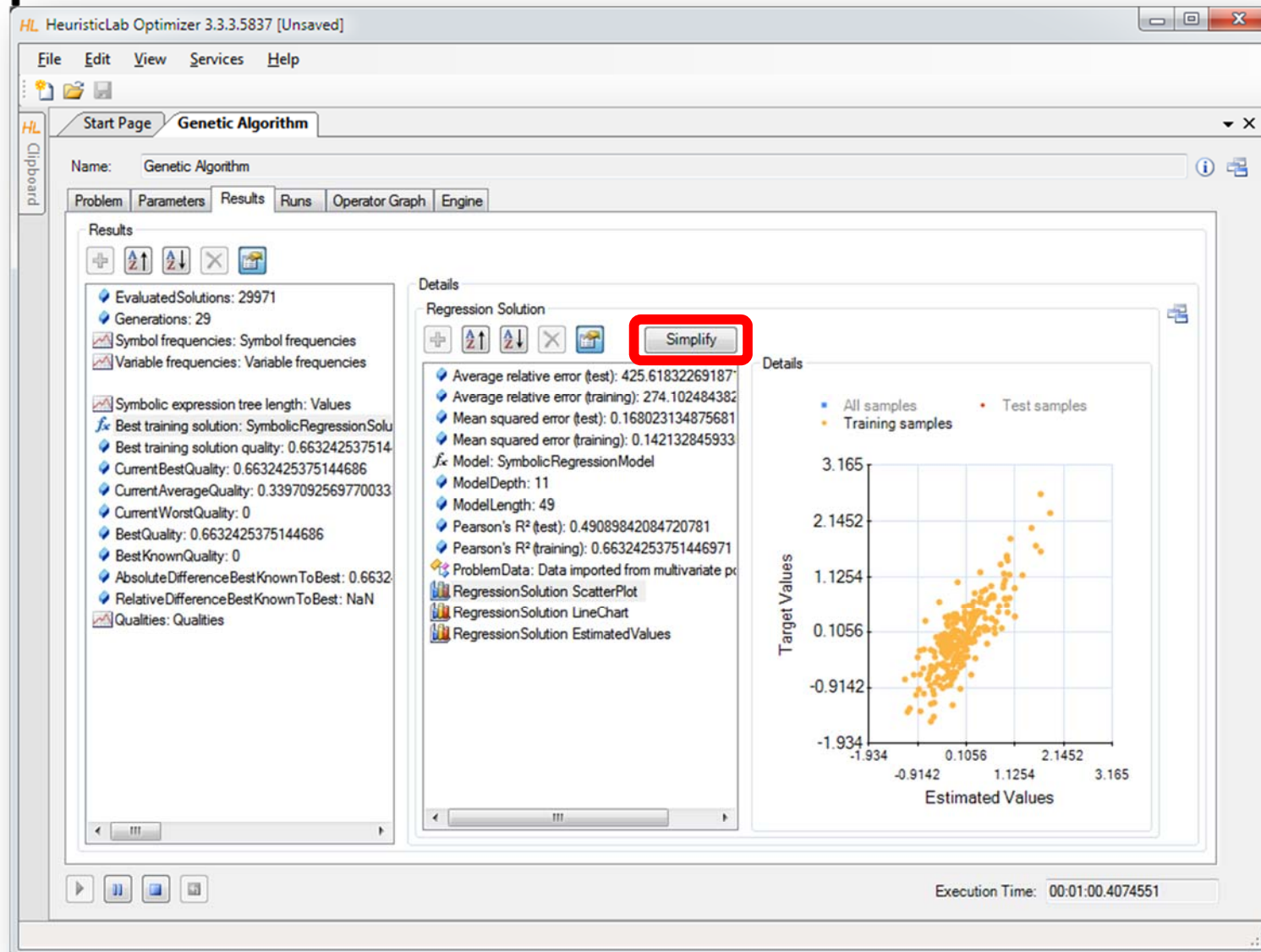
# Model Simplification and Export

- Demonstration
  - automatic simplification
  - visualization of node impacts
  - manual simplification
    - online update of results
  - model export
    - MATLAB
    - LaTeX



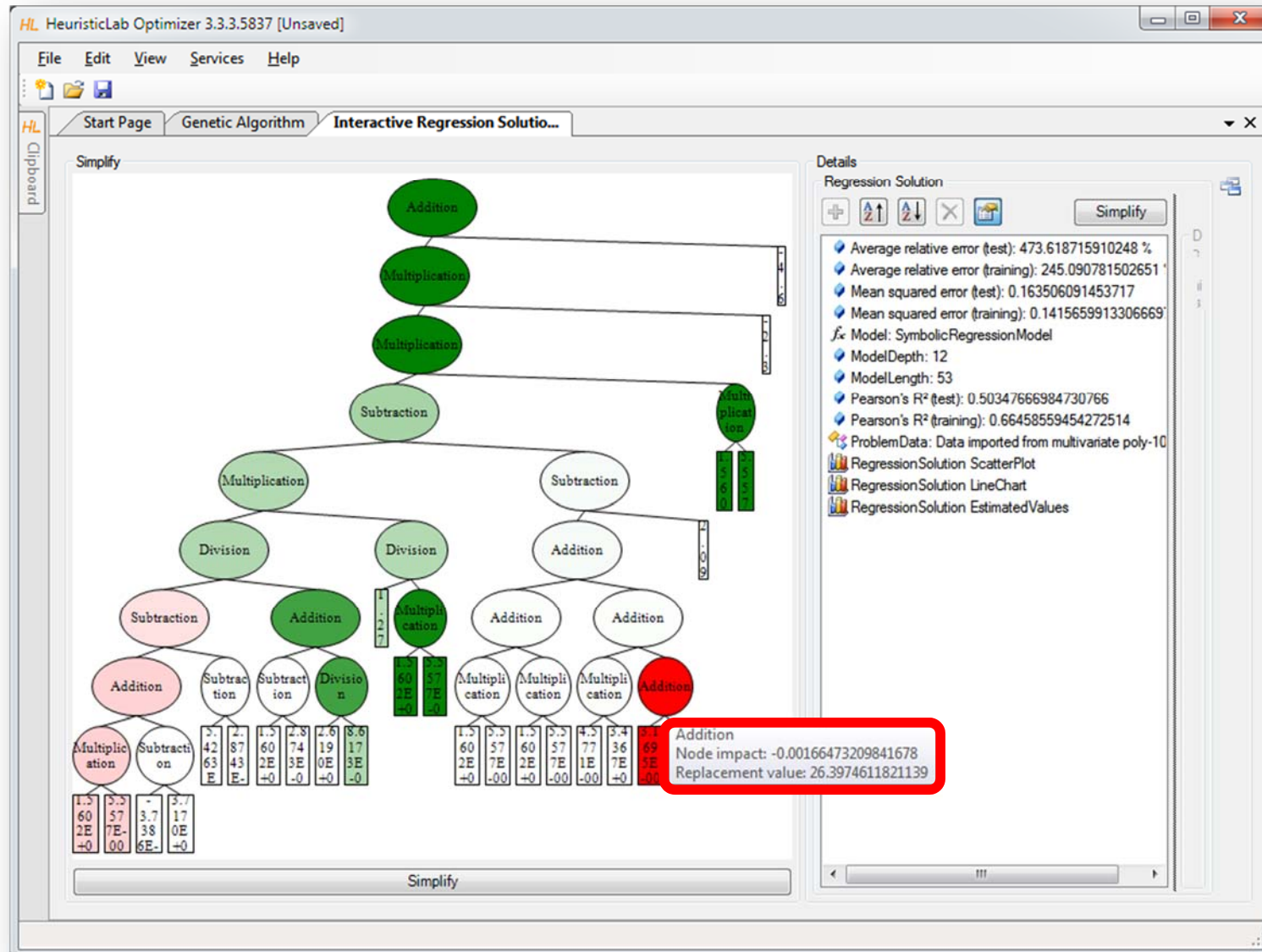
$$\begin{aligned}
 \text{Result} &= x_4(t) \cdot x_3(t) \cdot c_{20} & (13) \\
 &\cdot \left( x_6(t) \cdot x_5(t) \cdot c_4 + x_4(t) \cdot x_3(t) \cdot c_7 + x_4(t) \cdot x_3(t) \cdot c_{10} + \frac{c_{11} x_1(t)}{x_4(t) \cdot x_3(t) \cdot \left( c_{14} x_4(t) + c_{15} x_5(t) + \frac{1}{c_{17} x_2(t)} \right)} \cdot c_{18} + c_{19} \right) + c_{21} & (14)
 \end{aligned}$$

# Detailed Model Analysis and Simplification





# Symbolic Simplification and Node Impacts



The screenshot shows the HeuristicLab Optimizer interface with a symbolic regression tree. The tree consists of nodes representing mathematical operations: Addition, Multiplication, Subtraction, and Division. The nodes are color-coded: green for the root and its immediate children, light green for the next level, and pink for the bottom level. A red box highlights a specific node in the bottom right, showing its impact and replacement value.

**Node Impact Details:**

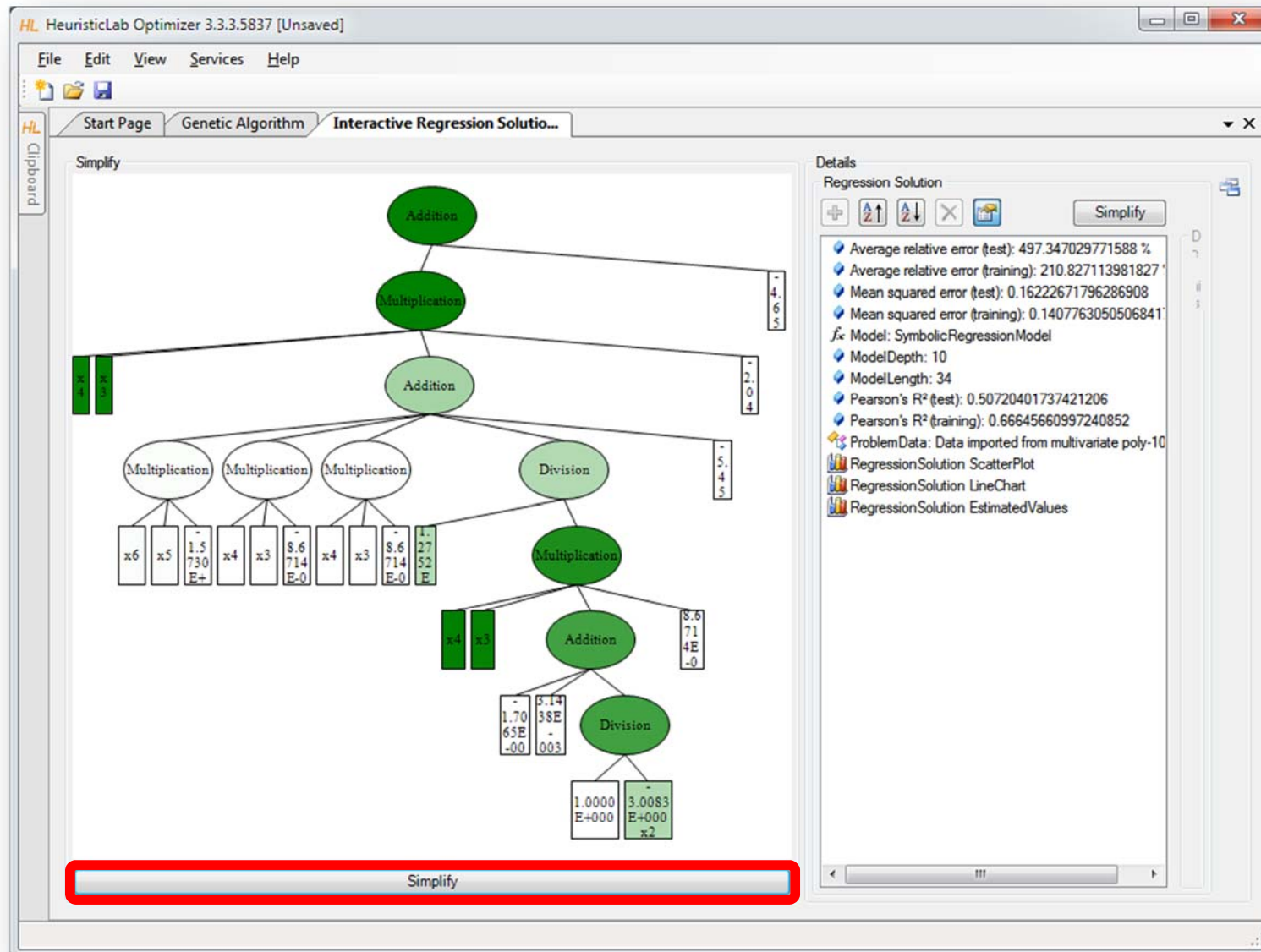
- Operation: Addition
- Node impact: -0.00166473209841678
- Replacement value: 26.3974611821139

**Regression Solution Details:**

- Average relative error (test): 473.618715910248 %
- Average relative error (training): 245.090781502651 %
- Mean squared error (test): 0.163506091453717
- Mean squared error (training): 0.1415659913306669
- Model: SymbolicRegressionModel
- ModelDepth: 12
- ModelLength: 53
- Pearson's R<sup>2</sup> (test): 0.50347666984730766
- Pearson's R<sup>2</sup> (training): 0.66458559454272514
- ProblemData: Data imported from multivariate poly-10
- RegressionSolution ScatterPlot
- RegressionSolution LineChart
- RegressionSolution EstimatedValues



# Automatic Symbolic Simplification



The screenshot displays the HeuristicLab Optimizer interface. The main window shows a symbolic regression tree under the 'Simplify' tab. The tree structure is as follows:

- Root: Addition (value: -4.65)
- Level 1: Multiplication (value: -2.04)
- Level 2: Addition (value: -5.45)
- Level 3: Multiplication (value: 8.6714E-0), Multiplication (value: 8.6714E-0), Multiplication (value: 1.2752E), and Division (value: 8.6714E-0)
- Level 4: Multiplication (value: 1.7065E-00), Multiplication (value: 1.5730E+), Multiplication (value: 1.0000E+000), and Division (value: 3.0083E+000)
- Level 5: Multiplication (value: 1.0000E+000), Multiplication (value: 1.5730E+), Multiplication (value: 1.2752E), and Division (value: 3.0083E+000)

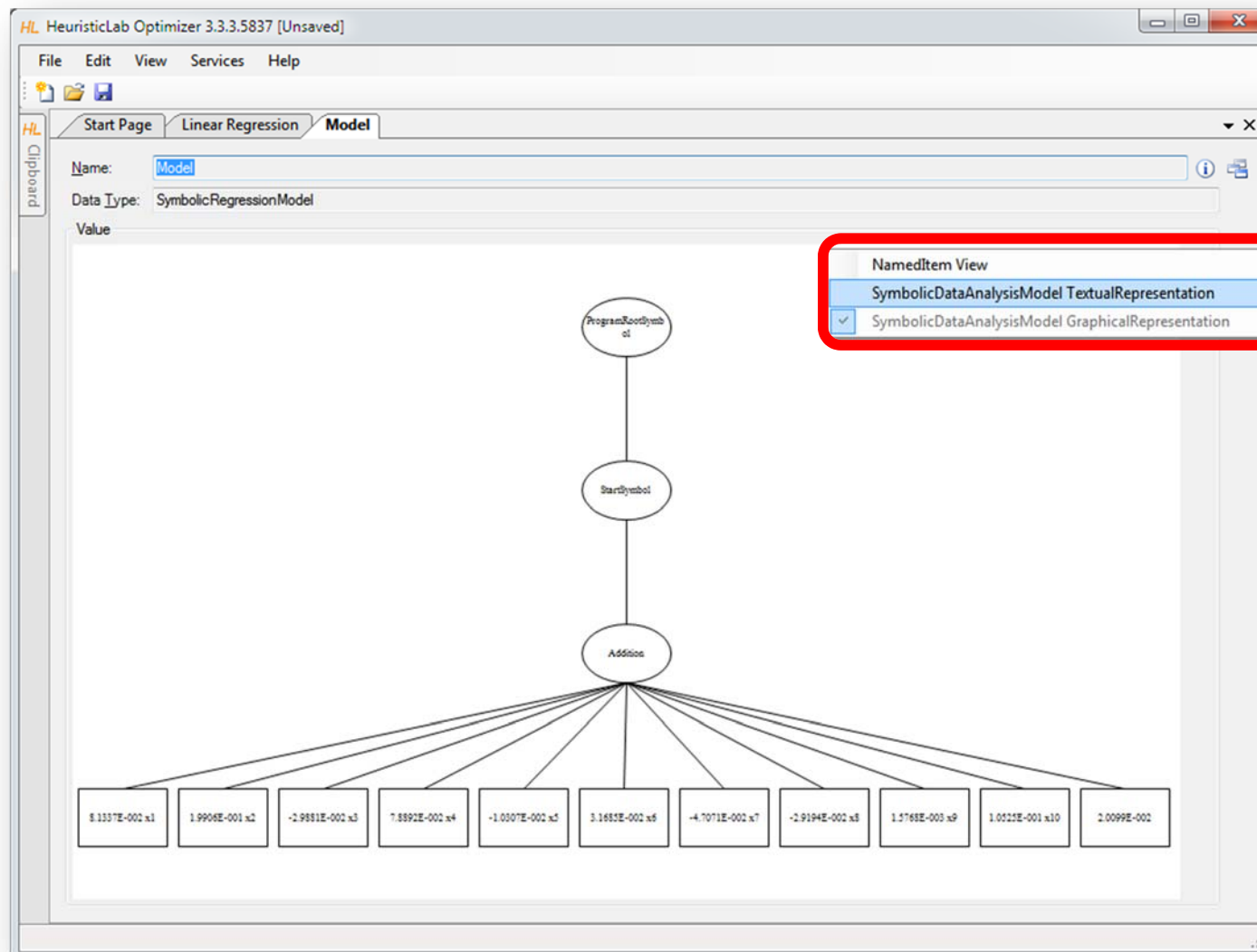
The 'Details' panel on the right provides the following information:

- Regression Solution
- Average relative error (test): 497.347029771588 %
- Average relative error (training): 210.827113981827 %
- Mean squared error (test): 0.16222671796286908
- Mean squared error (training): 0.1407763050506841
- Model: SymbolicRegressionModel
- ModelDepth: 10
- ModelLength: 34
- Pearson's R<sup>2</sup> (test): 0.50720401737421206
- Pearson's R<sup>2</sup> (training): 0.66645660997240852
- ProblemData: Data imported from multivariate poly-10
- RegressionSolution ScatterPlot
- RegressionSolution LineChart
- RegressionSolution EstimatedValues

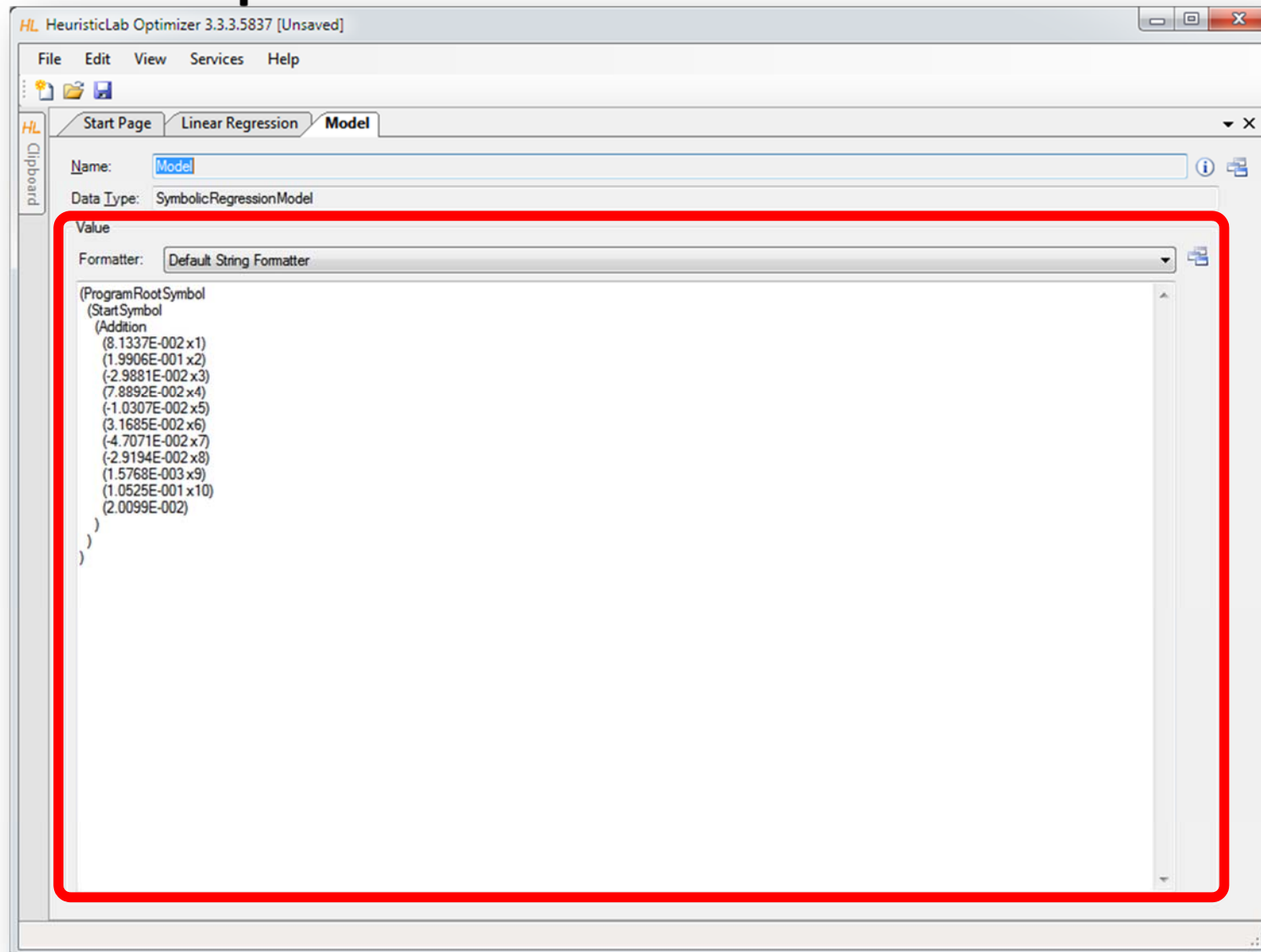
A red box highlights the 'Simplify' button at the bottom of the main window.

# Textual Representations Are Also Available

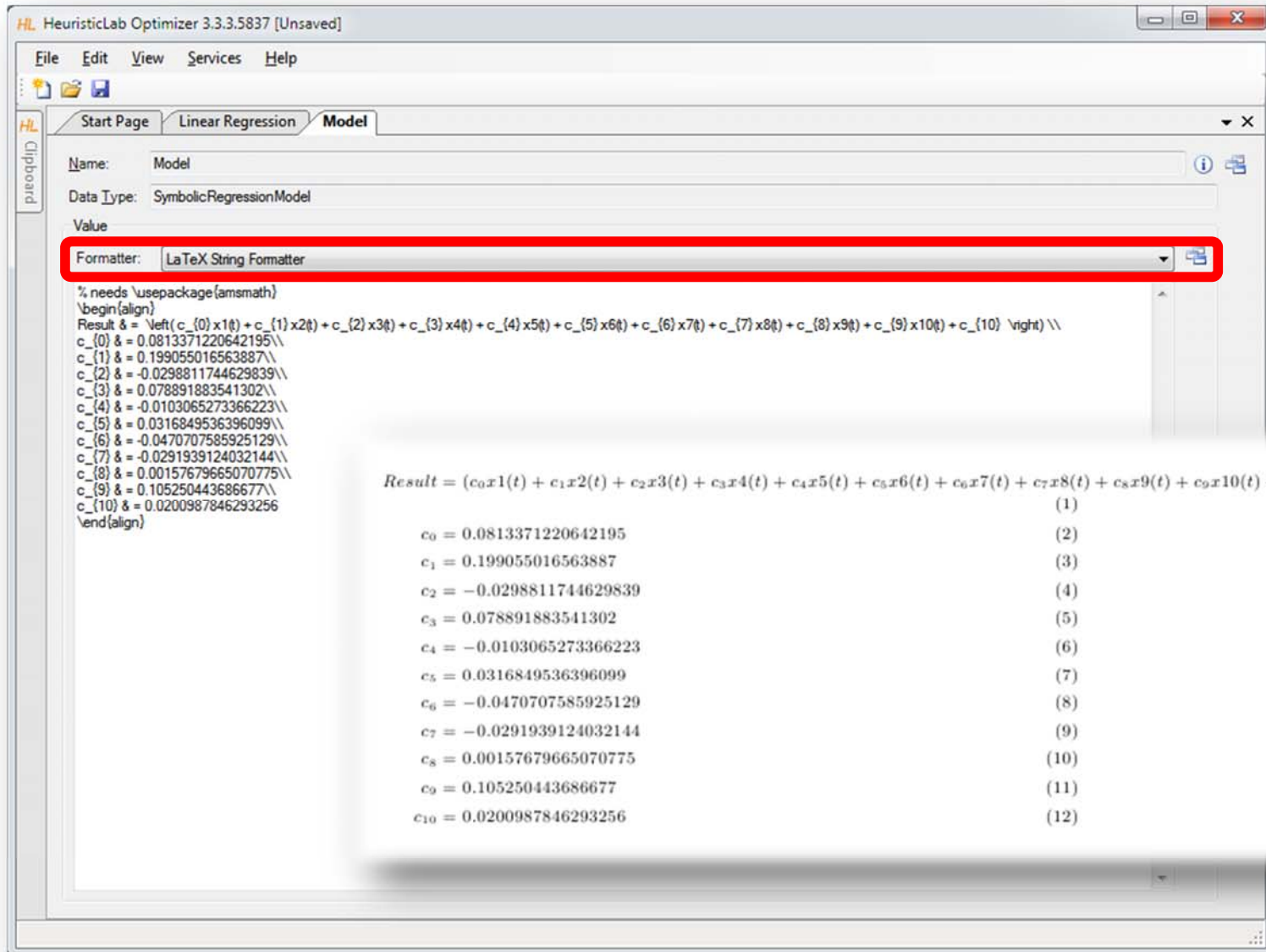
- Use *ViewHost* to switch to textual representation view.



# Default Textual Representation for Model Export



# Textual Representation for Export to LaTeX



HL HeuristicLab Optimizer 3.3.3.5837 [Unsaved]

File Edit View Services Help

Start Page Linear Regression Model

Name: Model

Data Type: SymbolicRegressionModel

Value

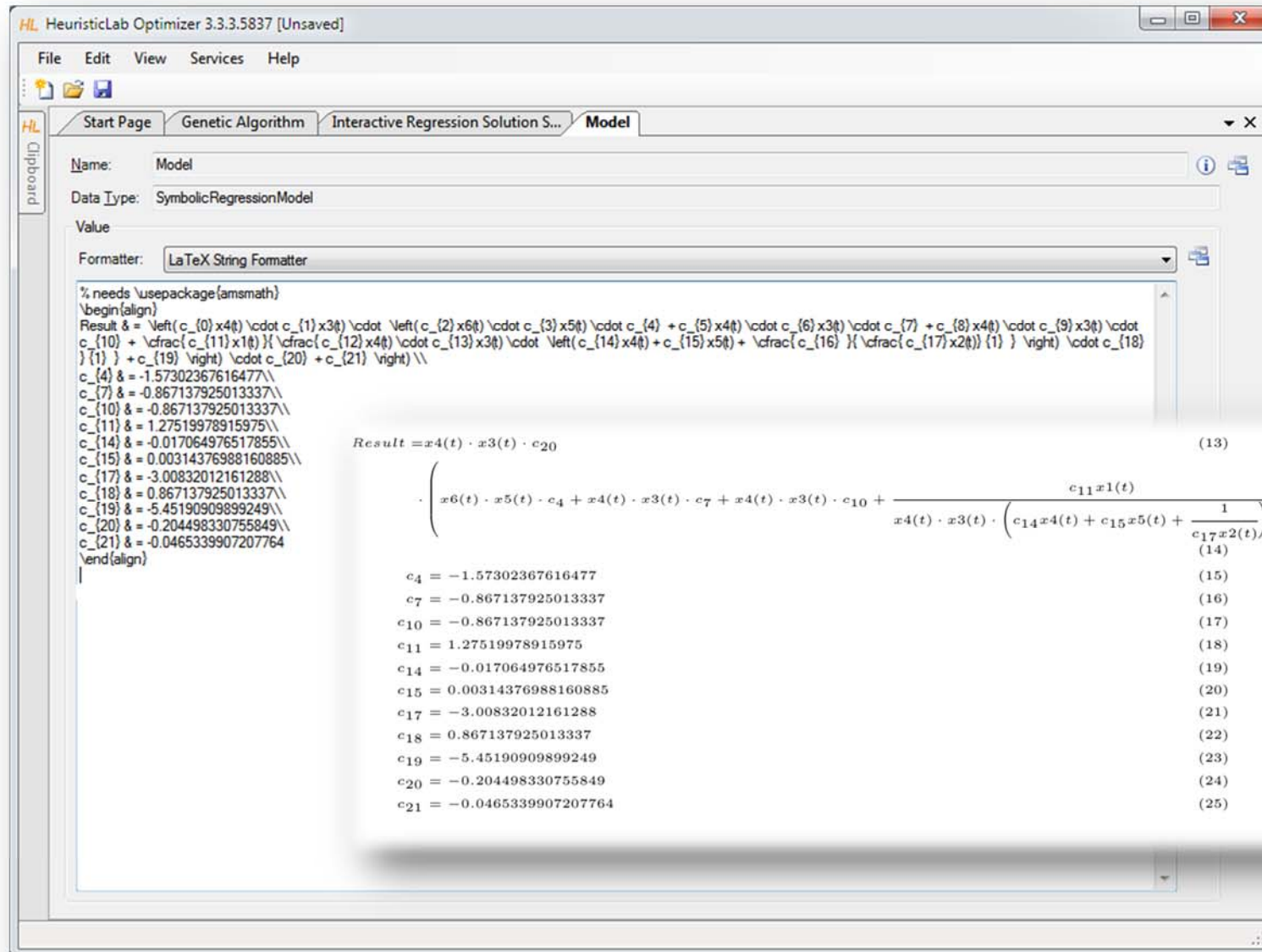
Formatter: LaTeX String Formatter

```
% needs \usepackage{amsmath}
\begin{align}
Result &= \left( c_0 x1(t) + c_1 x2(t) + c_2 x3(t) + c_3 x4(t) + c_4 x5(t) + c_5 x6(t) + c_6 x7(t) + c_7 x8(t) + c_8 x9(t) + c_9 x10(t) + c_{10} \right) \\
c_0 &= 0.0813371220642195 \\
c_1 &= 0.199055016563887 \\
c_2 &= -0.0298811744629839 \\
c_3 &= 0.078891883541302 \\
c_4 &= -0.0103065273366223 \\
c_5 &= 0.0316849536396099 \\
c_6 &= -0.0470707585925129 \\
c_7 &= -0.0291939124032144 \\
c_8 &= 0.00157679665070775 \\
c_9 &= 0.105250443686677 \\
c_{10} &= 0.0200987846293256
\end{align}
```

$$Result = (c_0 x1(t) + c_1 x2(t) + c_2 x3(t) + c_3 x4(t) + c_4 x5(t) + c_5 x6(t) + c_6 x7(t) + c_7 x8(t) + c_8 x9(t) + c_9 x10(t) + c_{10})$$

$c_0 = 0.0813371220642195$	(1)
$c_1 = 0.199055016563887$	(2)
$c_2 = -0.0298811744629839$	(3)
$c_3 = 0.078891883541302$	(4)
$c_4 = -0.0103065273366223$	(5)
$c_5 = 0.0316849536396099$	(6)
$c_6 = -0.0470707585925129$	(7)
$c_7 = -0.0291939124032144$	(8)
$c_8 = 0.00157679665070775$	(9)
$c_9 = 0.105250443686677$	(10)
$c_{10} = 0.0200987846293256$	(11)

# LaTeX Export



The screenshot shows the HeuristicLab Optimizer interface. The 'Model' tab is active, and the 'Value' section has 'LaTeX String Formatter' selected. The main window displays LaTeX code for a symbolic regression model. A preview window shows the rendered LaTeX expression and its corresponding numerical coefficients.

**LaTeX Code:**

```

% needs \usepackage{amsmath}
\begin{align}
Result &= \left( c_{0} x4(t) \cdot c_{1} x3(t) \cdot \left( c_{2} x6(t) \cdot c_{3} x5(t) \cdot c_{4} + c_{5} x4(t) \cdot c_{6} x3(t) \cdot c_{7} + c_{8} x4(t) \cdot c_{9} x3(t) \cdot c_{10} + \frac{c_{11} x1(t)}{\frac{c_{12} x4(t) \cdot c_{13} x3(t)}{\left( c_{14} x4(t) + c_{15} x5(t) + \frac{c_{16}}{\frac{c_{17} x2(t)}{1}} \right)} \right) \cdot c_{18} \right) \cdot c_{19} + c_{20} + c_{21} \\
c_{4} &= -1.57302367616477 \\
c_{7} &= -0.867137925013337 \\
c_{10} &= -0.867137925013337 \\
c_{11} &= 1.27519978915975 \\
c_{14} &= -0.017064976517855 \\
c_{15} &= 0.00314376988160885 \\
c_{17} &= -3.00832012161288 \\
c_{18} &= 0.867137925013337 \\
c_{19} &= -5.45190909899249 \\
c_{20} &= -0.204498330755849 \\
c_{21} &= -0.0465339907207764
\end{align}

```

**Mathematical Expression:**

$$Result = x4(t) \cdot x3(t) \cdot c_{20} \quad (13)$$

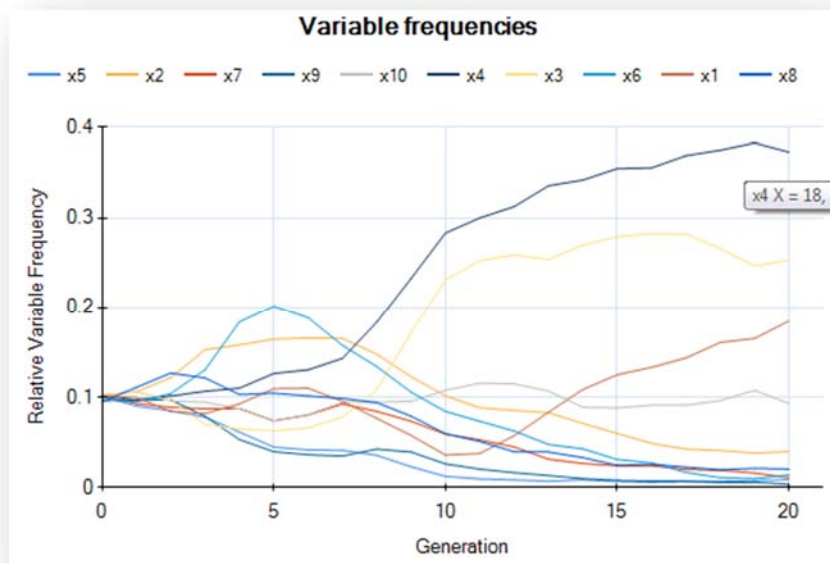
$$\cdot \left( x6(t) \cdot x5(t) \cdot c_4 + x4(t) \cdot x3(t) \cdot c_7 + x4(t) \cdot x3(t) \cdot c_{10} + \frac{c_{11} x1(t)}{x4(t) \cdot x3(t) \cdot \left( c_{14} x4(t) + c_{15} x5(t) + \frac{1}{c_{17} x2(t)} \right) \cdot c_{18}} + c_{19} \right) + c_{21}$$

**Coefficient List:**

- $c_4 = -1.57302367616477$  (15)
- $c_7 = -0.867137925013337$  (16)
- $c_{10} = -0.867137925013337$  (17)
- $c_{11} = 1.27519978915975$  (18)
- $c_{14} = -0.017064976517855$  (19)
- $c_{15} = 0.00314376988160885$  (20)
- $c_{17} = -3.00832012161288$  (21)
- $c_{18} = 0.867137925013337$  (22)
- $c_{19} = -5.45190909899249$  (23)
- $c_{20} = -0.204498330755849$  (24)
- $c_{21} = -0.0465339907207764$  (25)

# Variable Relevance Analysis

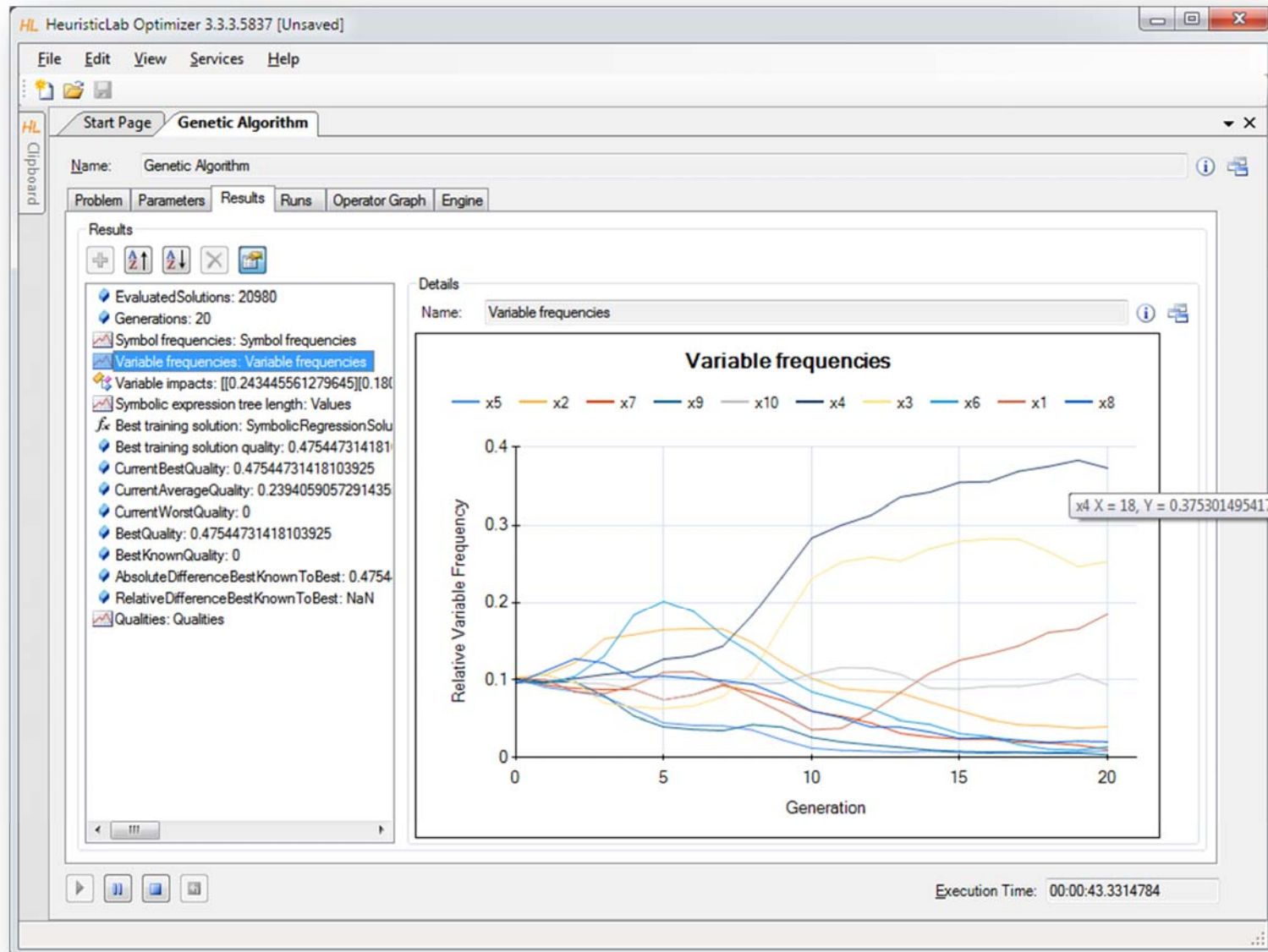
- Which variables are important to predict classes correctly?
- Demonstration
  - Variable frequency analyzer
  - symbol frequency analyzer
  - variable impacts



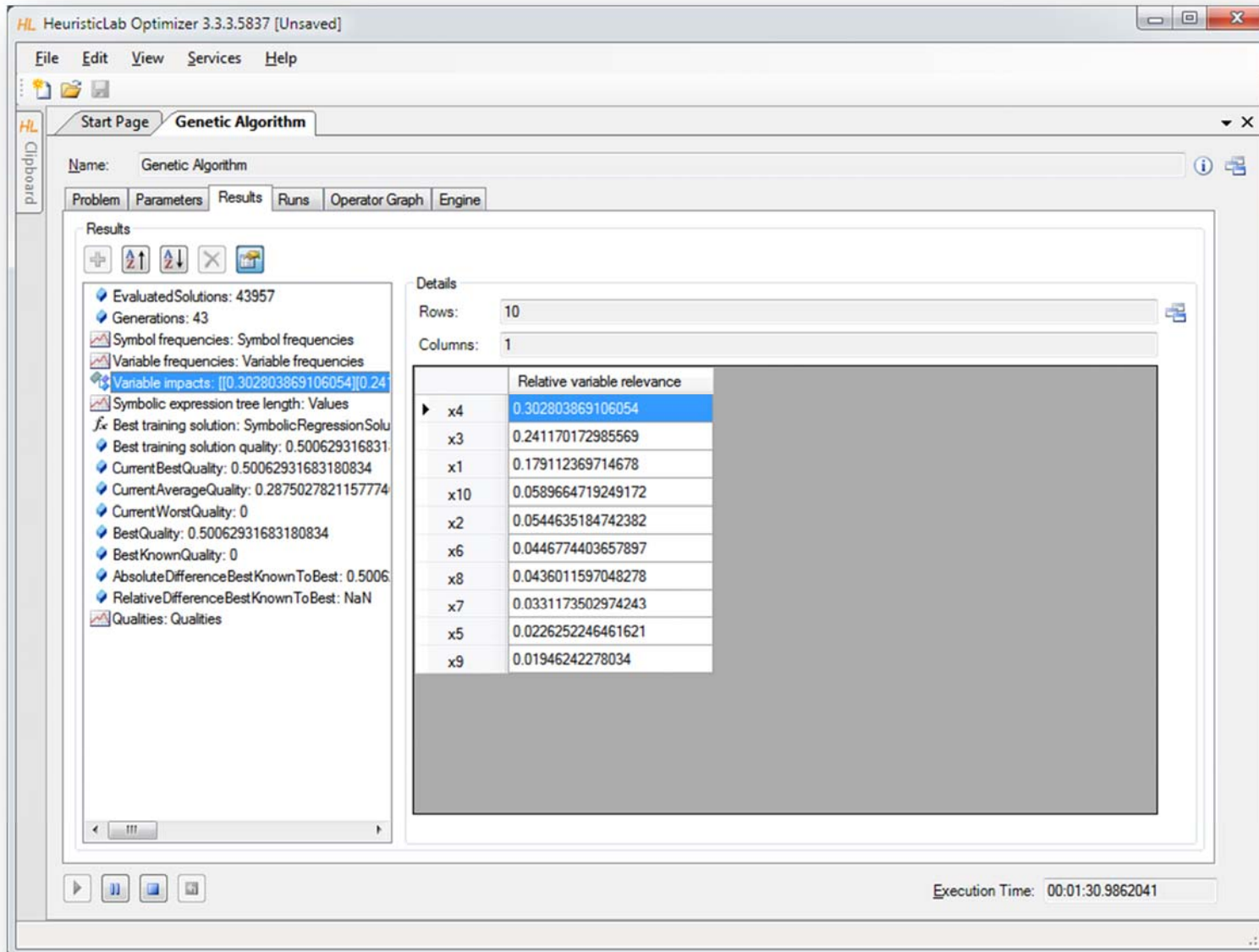
	Relative variable relevance
x4	0.302803869106054
x3	0.241170172985569
x1	0.179112369714678
x10	0.0589664719249172
x2	0.0544635184742382
x6	0.0446774403657897
x8	0.0436011597048278
x7	0.0331173502974243
x5	0.0226252246461621
x9	0.01946242278034



# Inspect Variable Frequency Chart



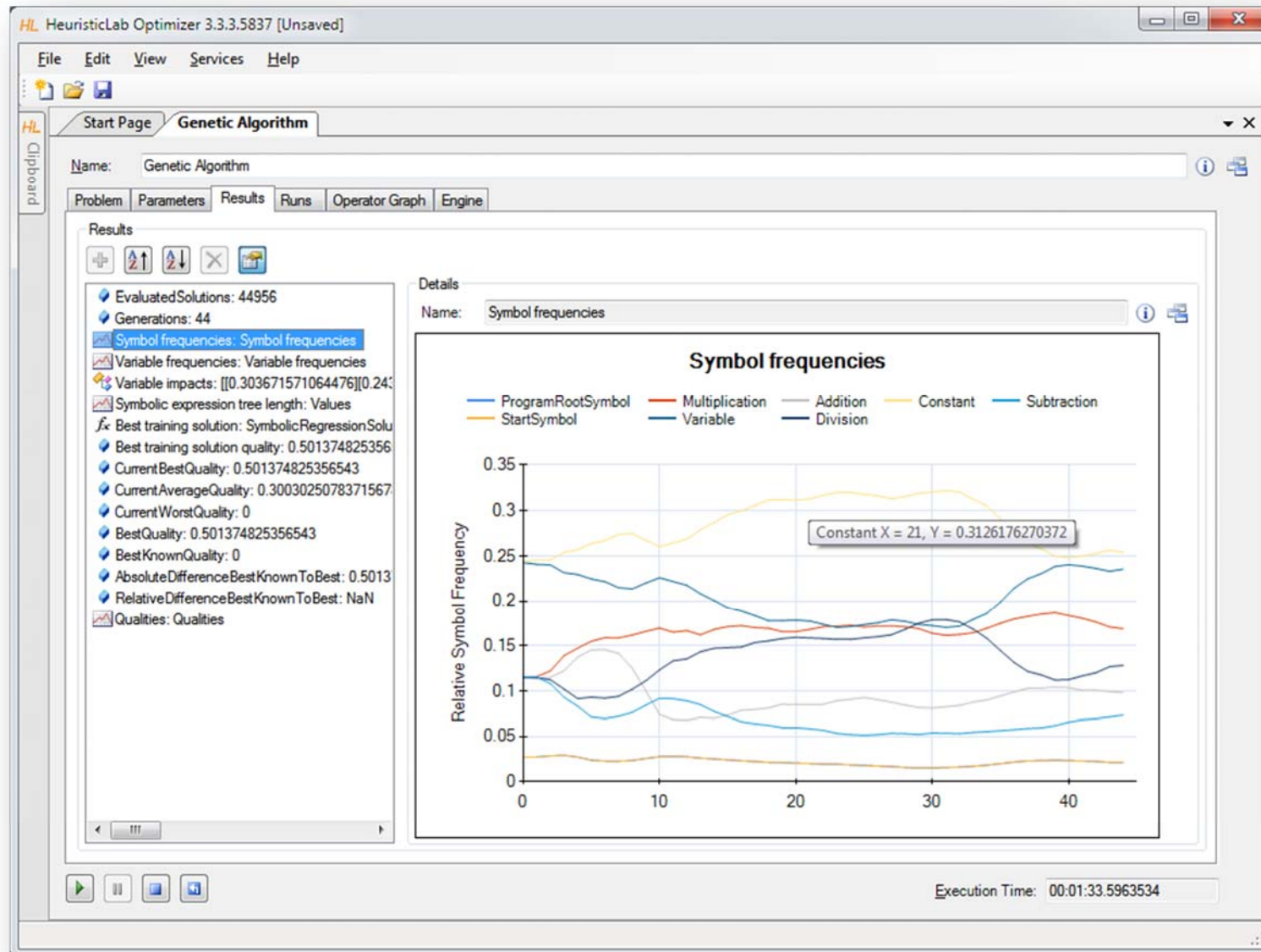
# Inspect Variable Impacts



The screenshot shows the HeuristicLab Optimizer interface. The 'Results' tab is active, displaying a list of results on the left and a 'Details' table on the right. The 'Variable impacts' result is selected, showing a list of variable impacts. The 'Details' table shows the relative variable relevance for each variable.

	Relative variable relevance
x4	0.302803869106054
x3	0.241170172985569
x1	0.179112369714678
x10	0.0589664719249172
x2	0.0544635184742382
x6	0.0446774403657897
x8	0.0436011597048278
x7	0.0331173502974243
x5	0.0226252246461621
x9	0.01946242278034

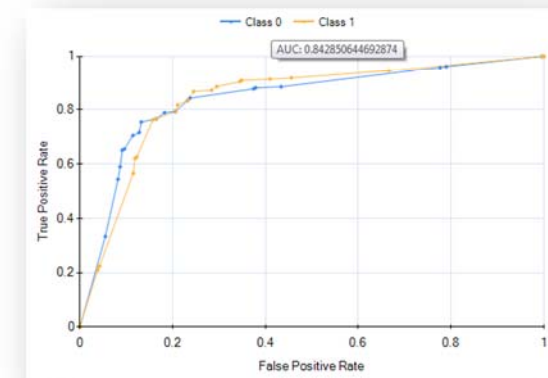
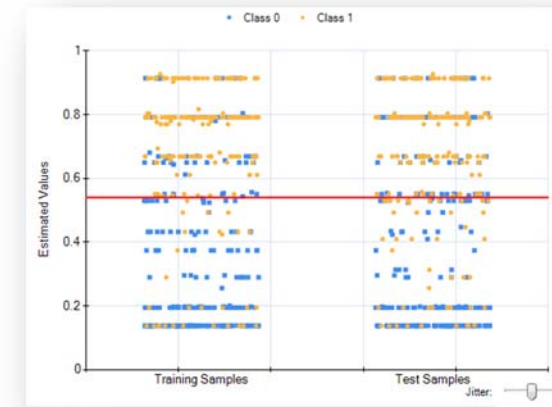
# Inspect Symbol Frequencies



# Classification with HeuristicLab



- Symbolic classification
  - evolve discriminating function using GP
  - find thresholds to assign classes
- Demonstration
  - real world medical application
  - model accuracy
  - visualization of model output
    - discriminating function output
    - ROC-curve
    - confusion matrix

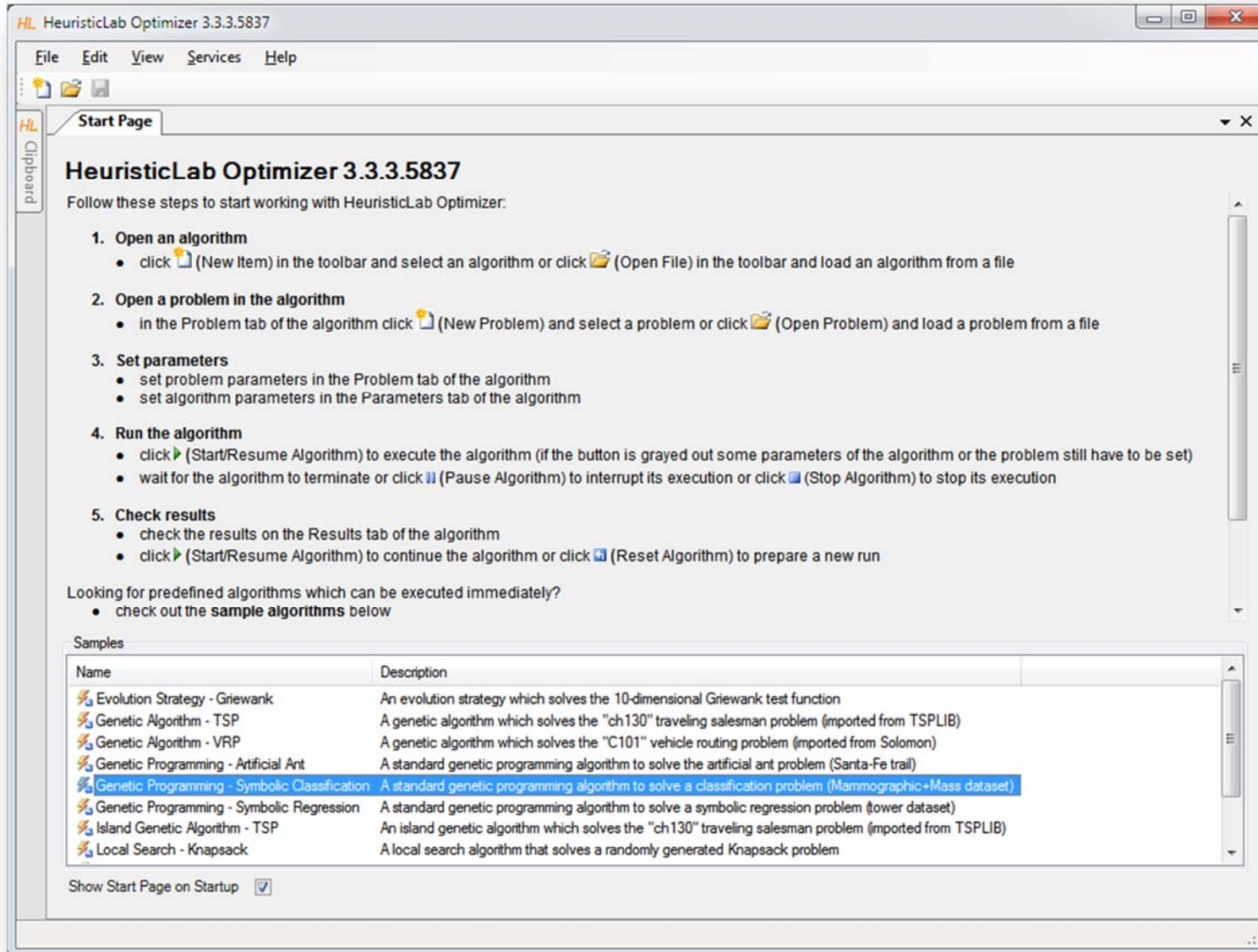


	Actual Class 0	Actual Class 1
Predicted Class 0	197	29
Predicted Class 1	64	190

# Case Study: Classification

- Real world medical dataset (*Mammographic Mass*) from UCI Machine Learning Repository
  - data from non-invasive mammography screening
  - variables:
    - patient age
    - visual features of inspected mass lesions: shape, margin, density
  - target variable: severity (malignant, benign)
  - download  
<http://dev.heuristiclab.com/AdditionalMaterial#GECCO2012>

# Open Sample



HL HeuristicLab Optimizer 3.3.3.5837

File Edit View Services Help

Start Page

## HeuristicLab Optimizer 3.3.3.5837

Follow these steps to start working with HeuristicLab Optimizer:

- 1. Open an algorithm**
  - click (New Item) in the toolbar and select an algorithm or click (Open File) in the toolbar and load an algorithm from a file
- 2. Open a problem in the algorithm**
  - in the Problem tab of the algorithm click (New Problem) and select a problem or click (Open Problem) and load a problem from a file
- 3. Set parameters**
  - set problem parameters in the Problem tab of the algorithm
  - set algorithm parameters in the Parameters tab of the algorithm
- 4. Run the algorithm**
  - click (Start/Resume Algorithm) to execute the algorithm (if the button is grayed out some parameters of the algorithm or the problem still have to be set)
  - wait for the algorithm to terminate or click (Pause Algorithm) to interrupt its execution or click (Stop Algorithm) to stop its execution
- 5. Check results**
  - check the results on the Results tab of the algorithm
  - click (Start/Resume Algorithm) to continue the algorithm or click (Reset Algorithm) to prepare a new run

Looking for predefined algorithms which can be executed immediately?

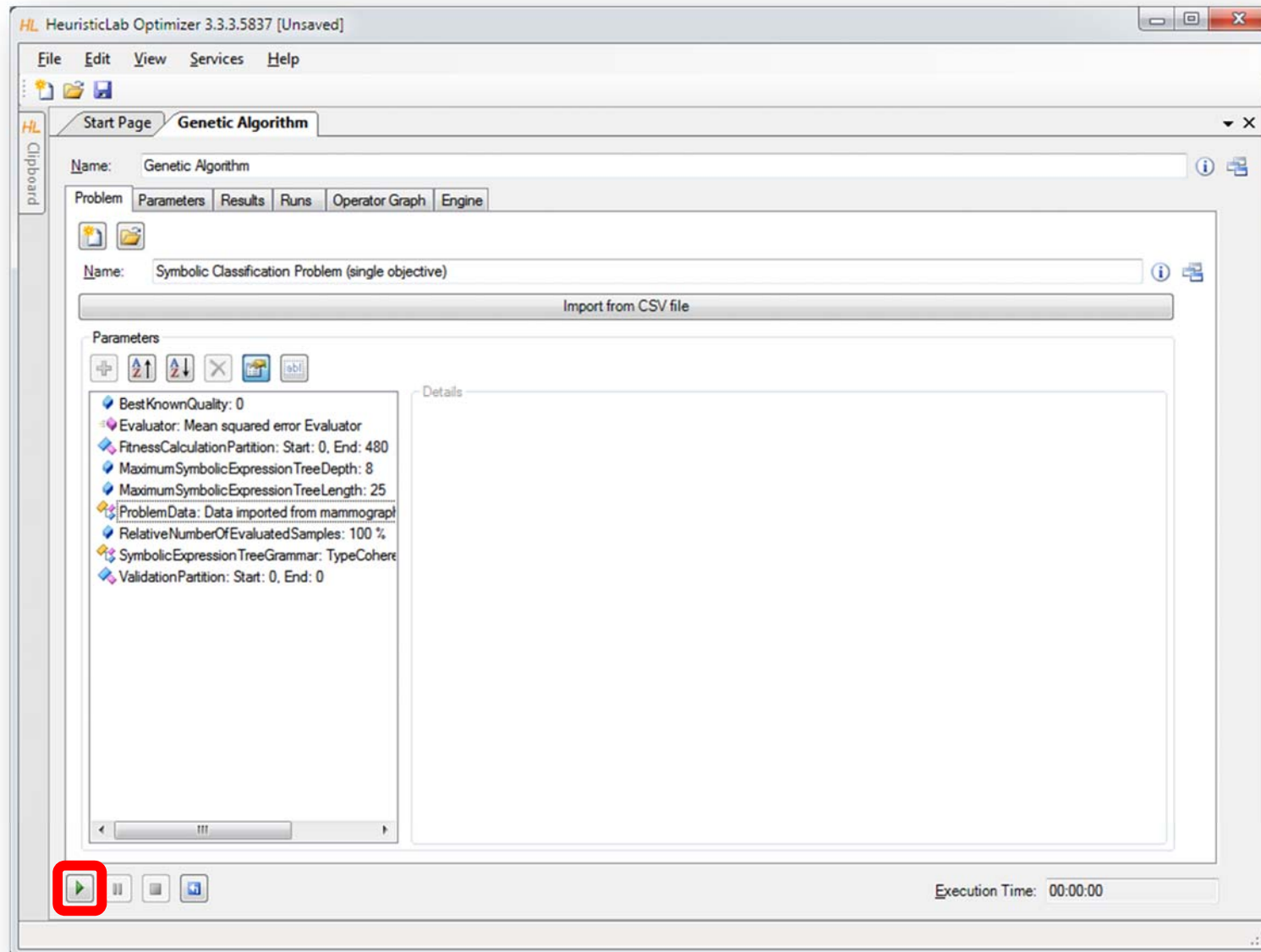
- check out the **sample algorithms** below

Samples

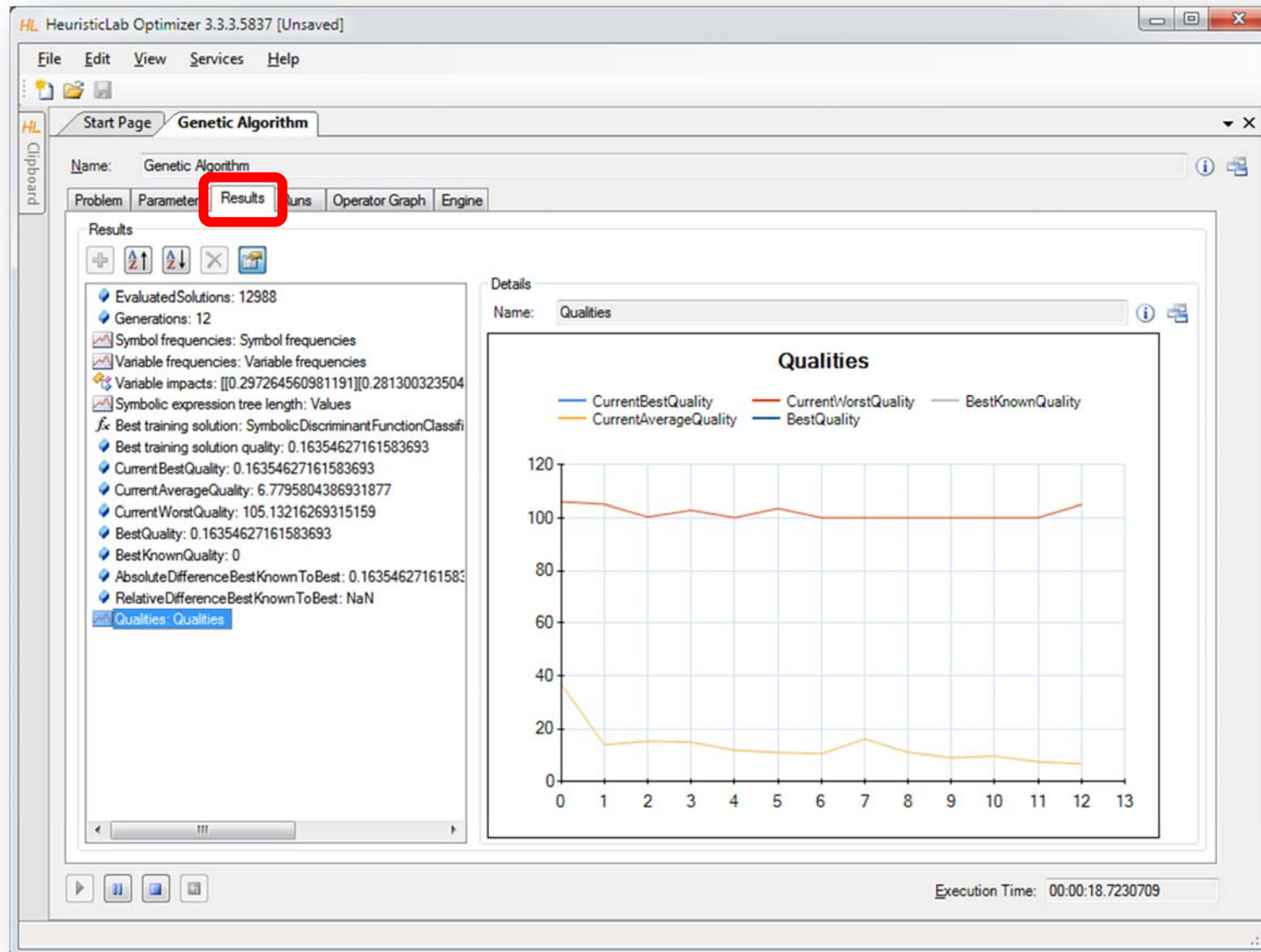
Name	Description
Evolution Strategy - Griewank	An evolution strategy which solves the 10-dimensional Griewank test function
Genetic Algorithm - TSP	A genetic algorithm which solves the "ch130" traveling salesman problem (imported from TSPLIB)
Genetic Algorithm - VRP	A genetic algorithm which solves the "C101" vehicle routing problem (imported from Solomon)
Genetic Programming - Artificial Ant	A standard genetic programming algorithm to solve the artificial ant problem (Santa-Fe trail)
Genetic Programming - Symbolic Classification	A standard genetic programming algorithm to solve a classification problem (Mammographic+Mass dataset)
Genetic Programming - Symbolic Regression	A standard genetic programming algorithm to solve a symbolic regression problem (tower dataset)
Island Genetic Algorithm - TSP	An island genetic algorithm which solves the "ch130" traveling salesman problem (imported from TSPLIB)
Local Search - Knapsack	A local search algorithm that solves a randomly generated Knapsack problem

Show Start Page on Startup

# Configure and Run Algorithm

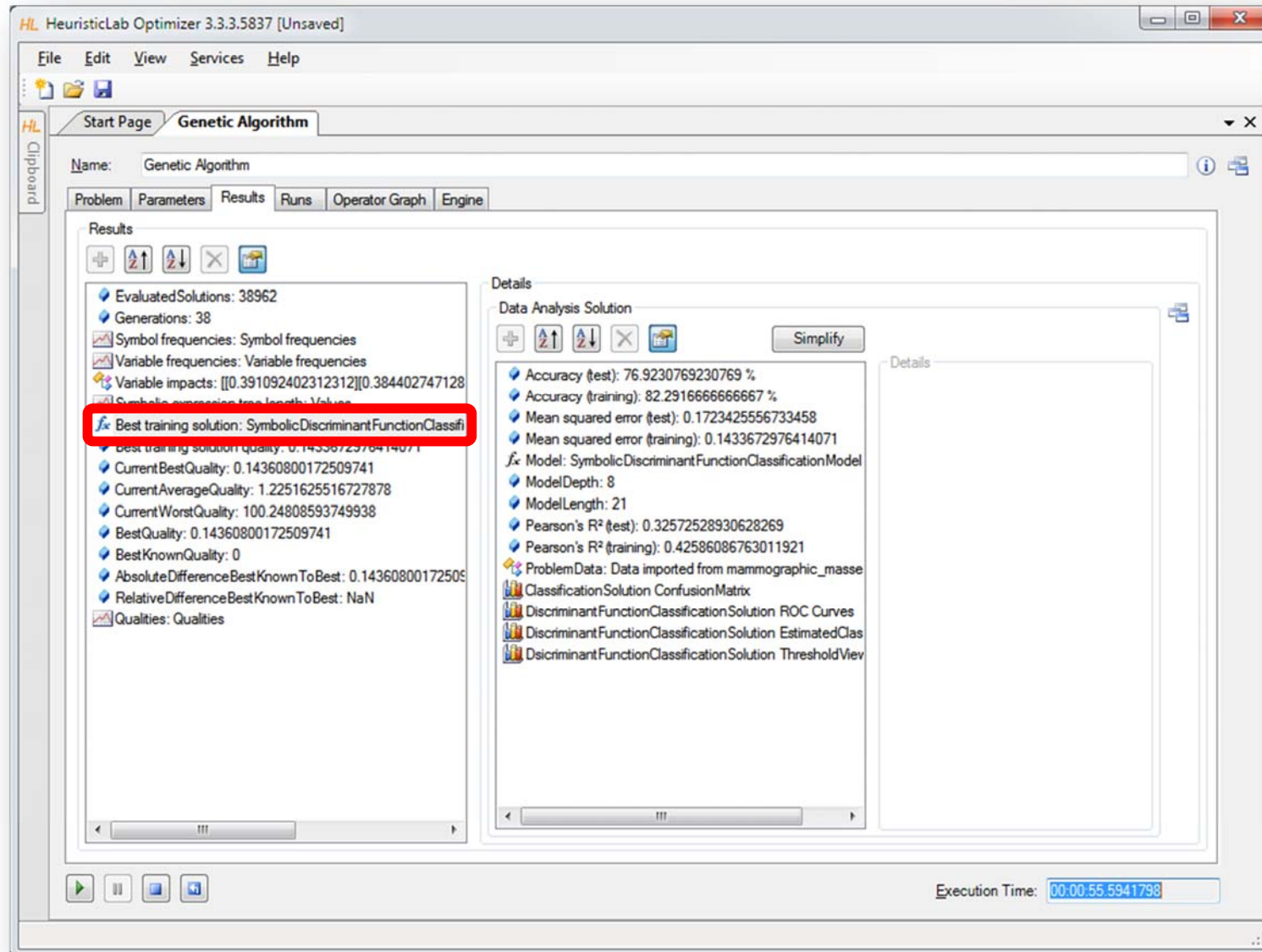


# Inspect Quality Linechart





# Inspect Best Training Solution



HL HeuristicLab Optimizer 3.3.3.5837 [Unsaved]

File Edit View Services Help

Clipboard

Start Page Genetic Algorithm

Name: Genetic Algorithm

Problem Parameters Results Runs Operator Graph Engine

Results

- EvaluatedSolutions: 38962
- Generations: 38
- Symbol frequencies: Symbol frequencies
- Variable frequencies: Variable frequencies
- Variable impacts: [[0.391092402312312][0.384402747128
- Symbolic expression tree length: Values
- Best training solution: SymbolicDiscriminantFunctionClassifi**
- Best training solution quality: 0.1433672976414071
- CurrentBestQuality: 0.14360800172509741
- CurrentAverageQuality: 1.2251625516727878
- CurrentWorstQuality: 100.24808593749938
- BestQuality: 0.14360800172509741
- BestKnownQuality: 0
- AbsoluteDifferenceBestKnownToBest: 0.14360800172509741
- RelativeDifferenceBestKnownToBest: NaN
- Qualities: Qualities

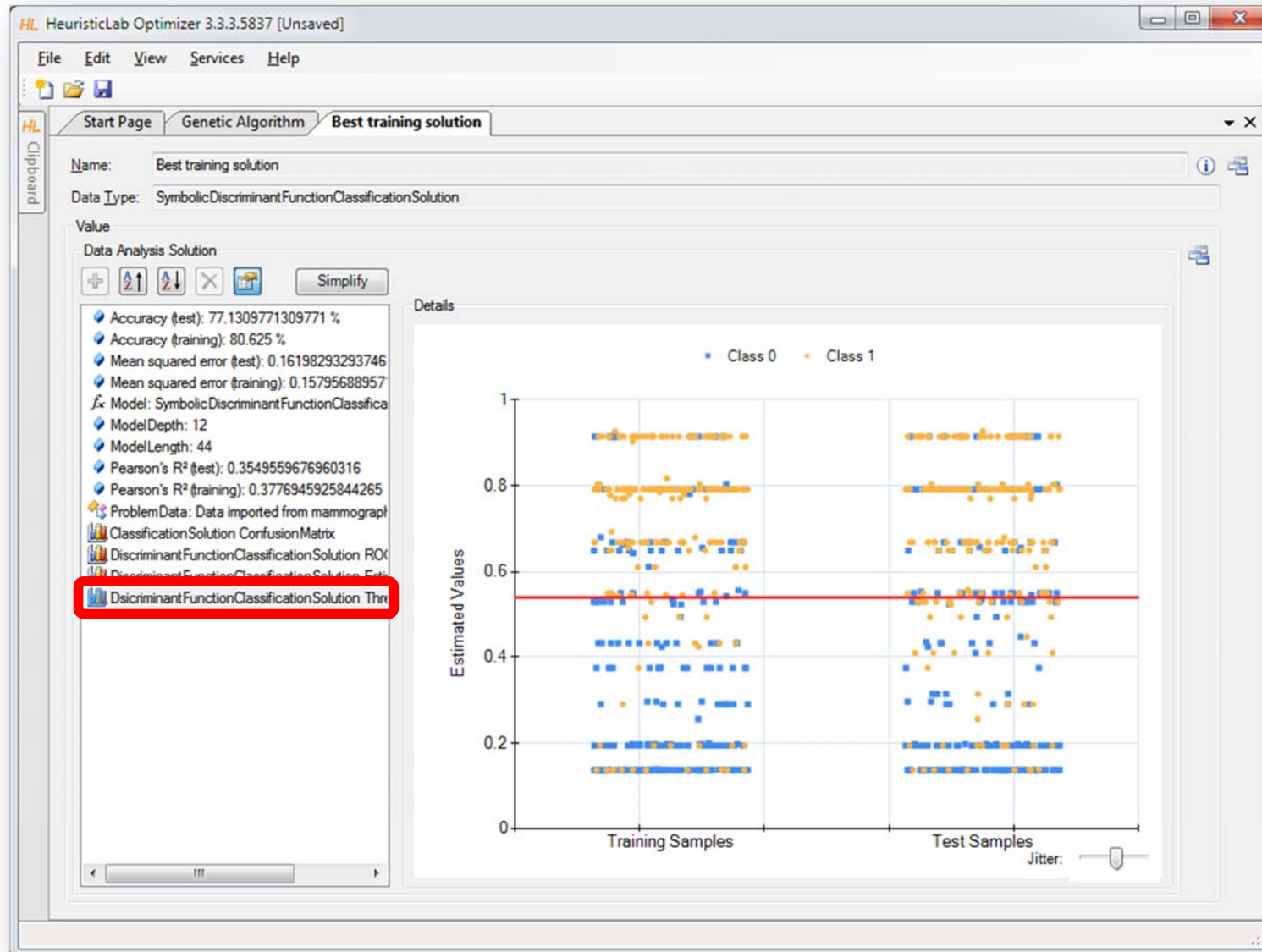
Details

Data Analysis Solution

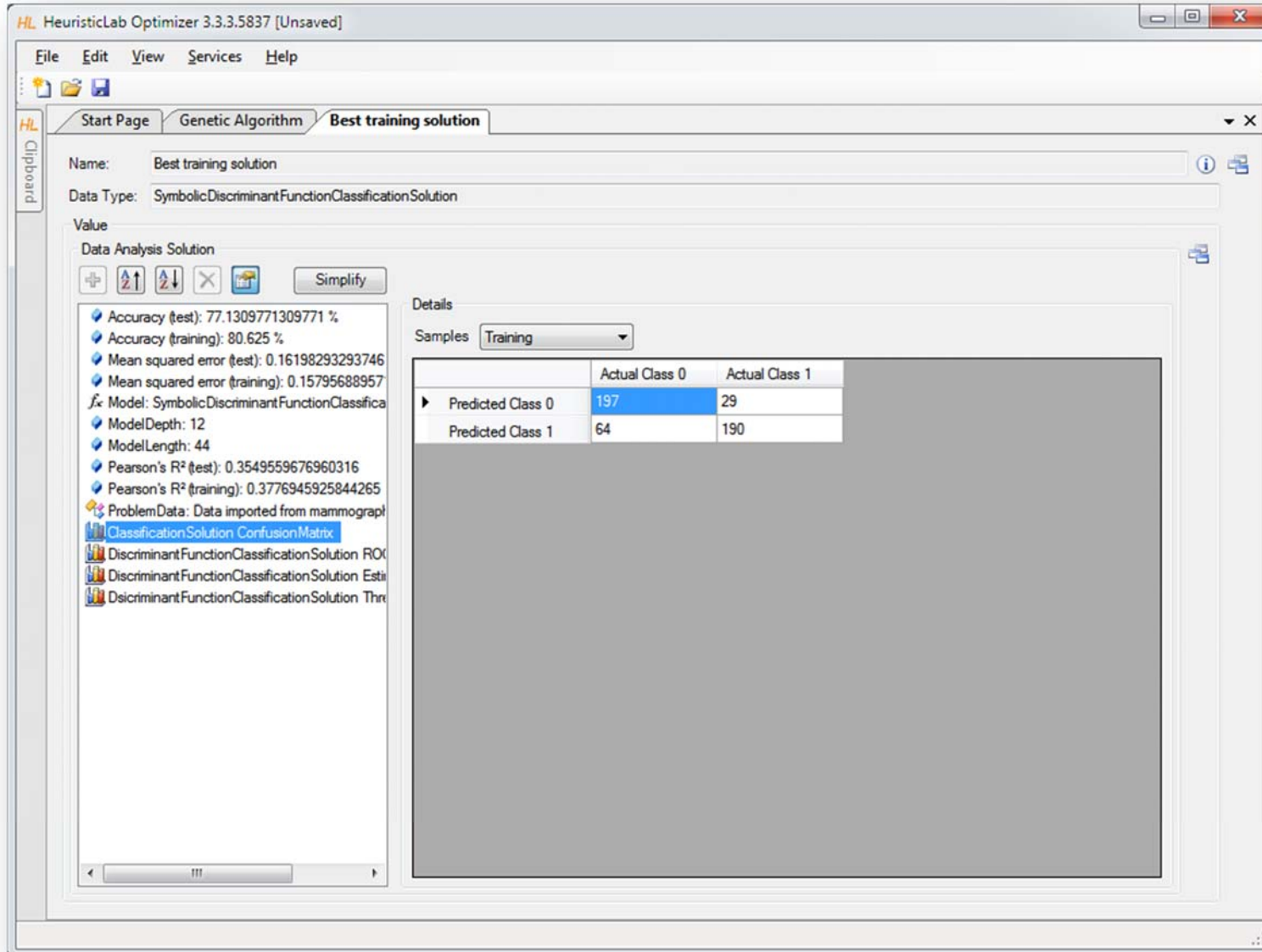
- Accuracy (test): 76.9230769230769 %
- Accuracy (training): 82.2916666666667 %
- Mean squared error (test): 0.1723425556733458
- Mean squared error (training): 0.1433672976414071
- Model: SymbolicDiscriminantFunctionClassificationModel
- ModelDepth: 8
- ModelLength: 21
- Pearson's R<sup>2</sup> (test): 0.32572528930628269
- Pearson's R<sup>2</sup> (training): 0.42586086763011921
- ProblemData: Data imported from mammographic\_masse
- ClassificationSolution ConfusionMatrix
- DiscriminantFunctionClassificationSolution ROC Curves
- DiscriminantFunctionClassificationSolution EstimatedClas
- DiscriminantFunctionClassificationSolution ThresholdView

Execution Time: 00:00:55.5941798

# Inspect Model Output and Thresholds



# Inspect Confusion Matrix



The screenshot shows the HeuristicLab Optimizer interface. The main window displays the 'Best training solution' for a Symbolic Discriminant Function Classification Solution. The 'Value' section shows various performance metrics, including accuracy and mean squared error. The 'Details' section shows a confusion matrix for the training samples.

Value

Data Analysis Solution

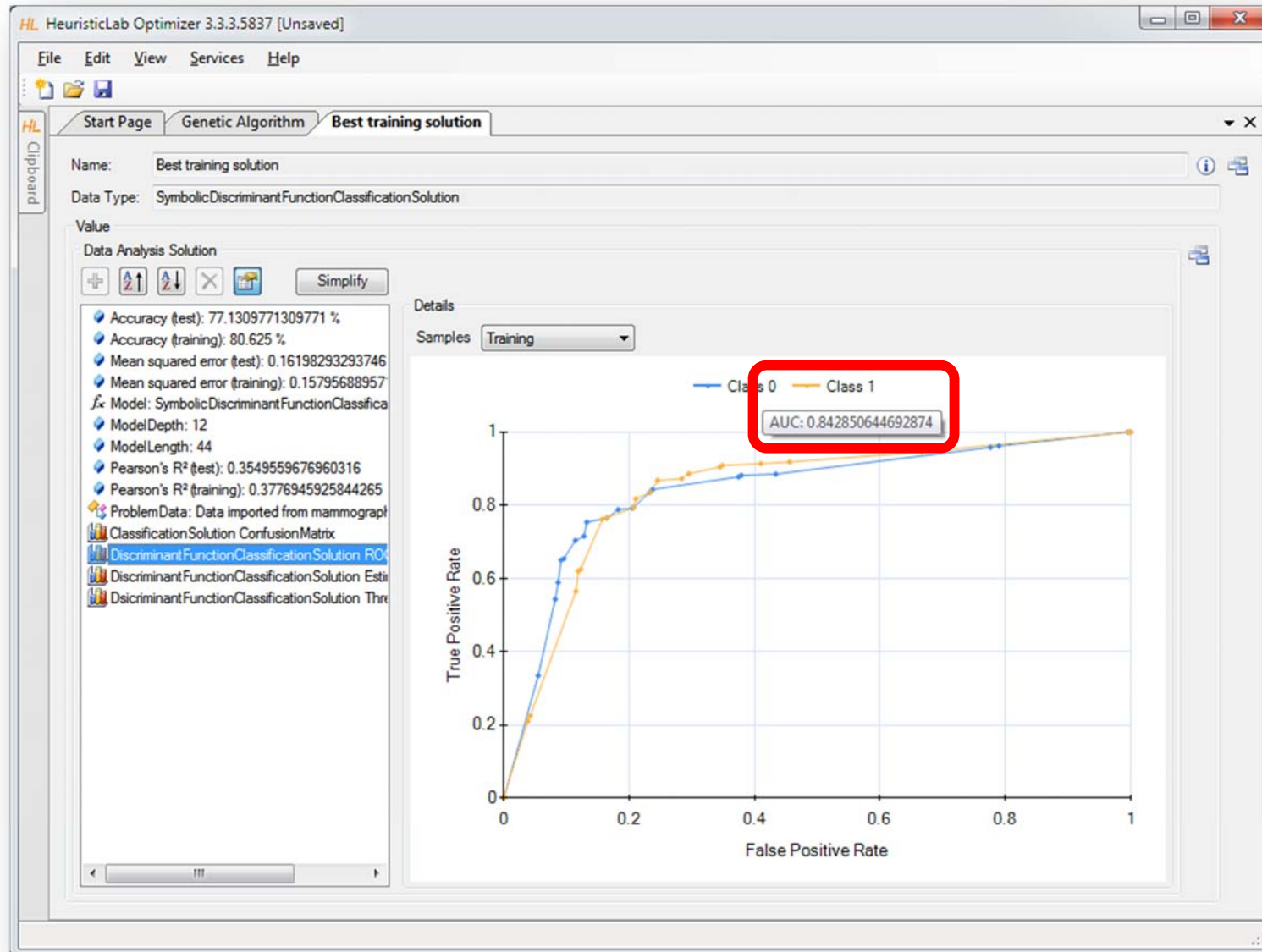
Accuracy (test): 77.1309771309771 %  
Accuracy (training): 80.625 %  
Mean squared error (test): 0.16198293293746  
Mean squared error (training): 0.15795688957  
Model: SymbolicDiscriminantFunctionClassifica  
ModelDepth: 12  
ModelLength: 44  
Pearson's R<sup>2</sup> (test): 0.3549559676960316  
Pearson's R<sup>2</sup> (training): 0.3776945925844265  
ProblemData: Data imported from mammograph  
ClassificationSolution ConfusionMatrix  
DiscriminantFunctionClassificationSolution ROC  
DiscriminantFunctionClassificationSolution Esti  
DiscriminantFunctionClassificationSolution Thr

Details

Samples Training

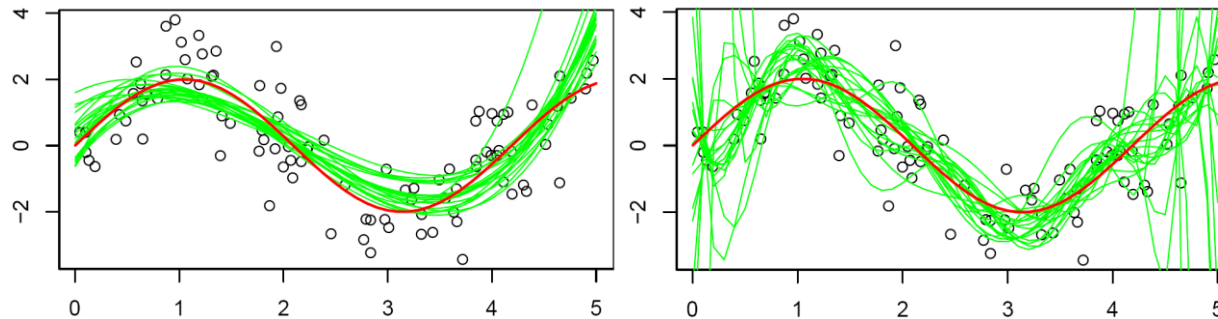
	Actual Class 0	Actual Class 1
Predicted Class 0	197	29
Predicted Class 1	64	190

# Inspect ROC Curve



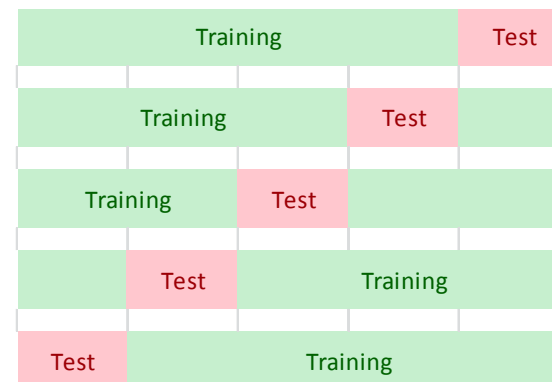
# Validation of Results

- Overfitting = memorizing data



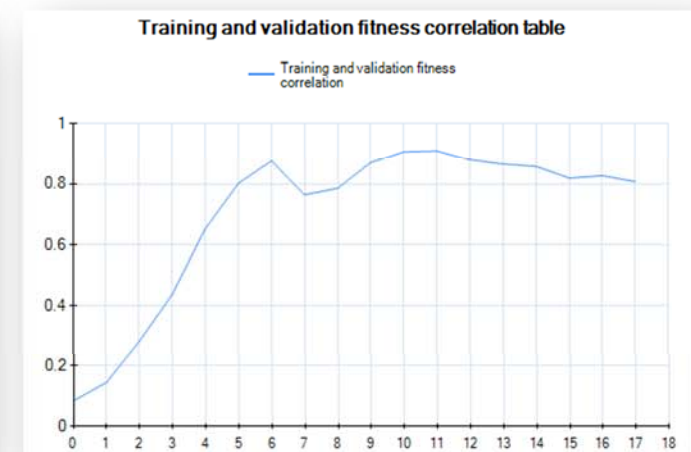
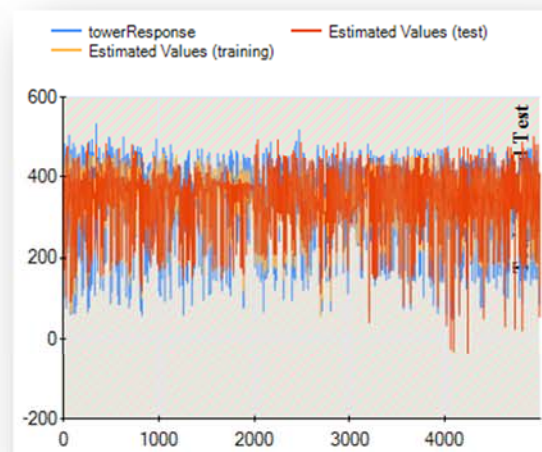
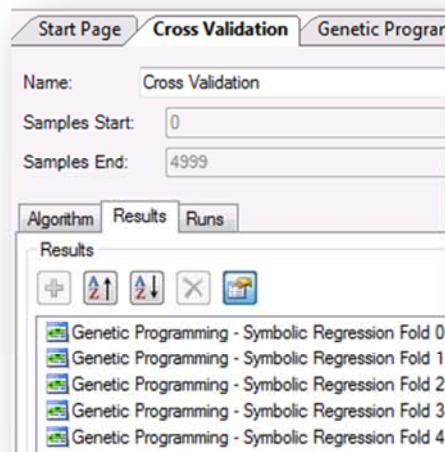
- Strategies to reduce overfitting

- validation partition
- cross-validation

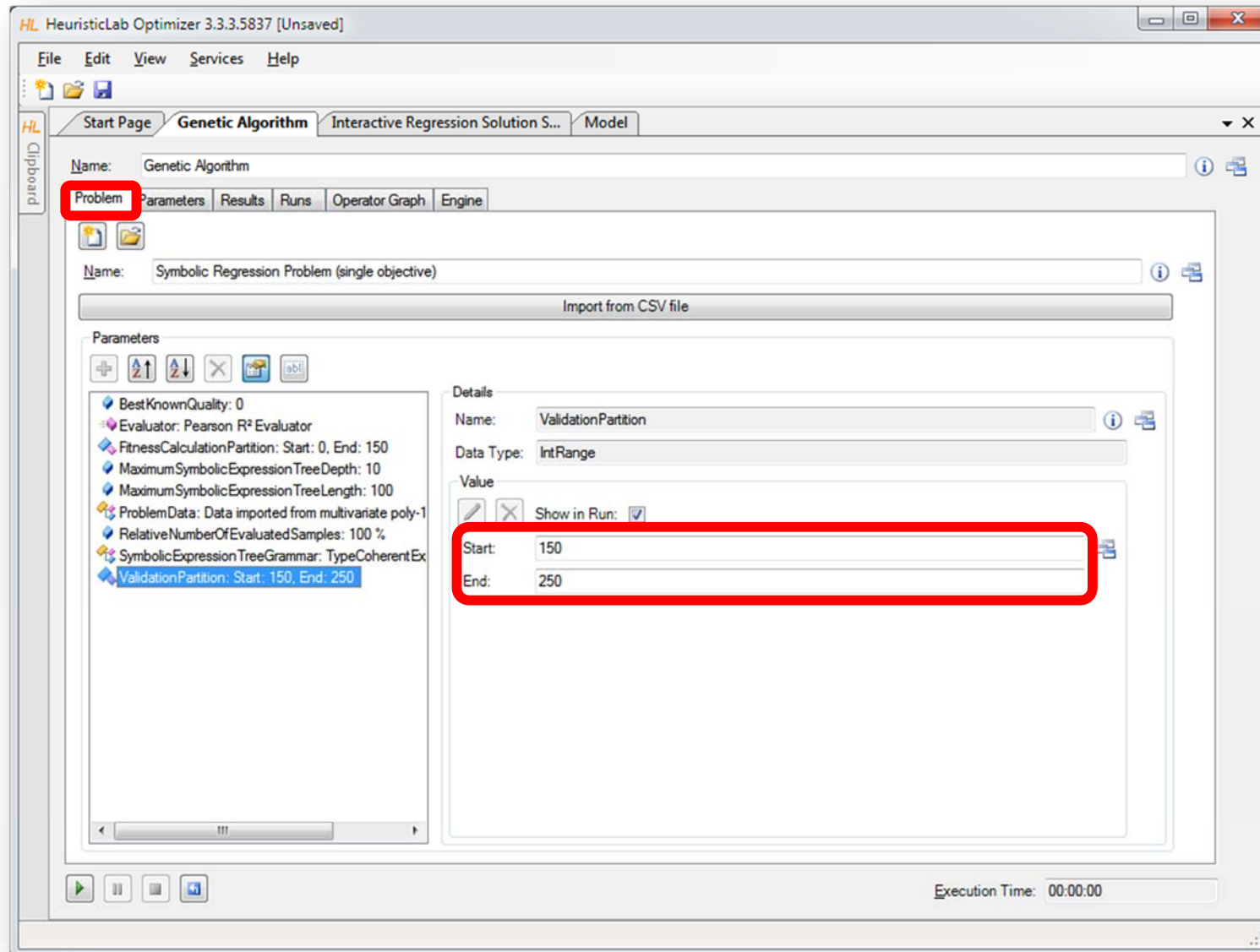


# Validation of Results

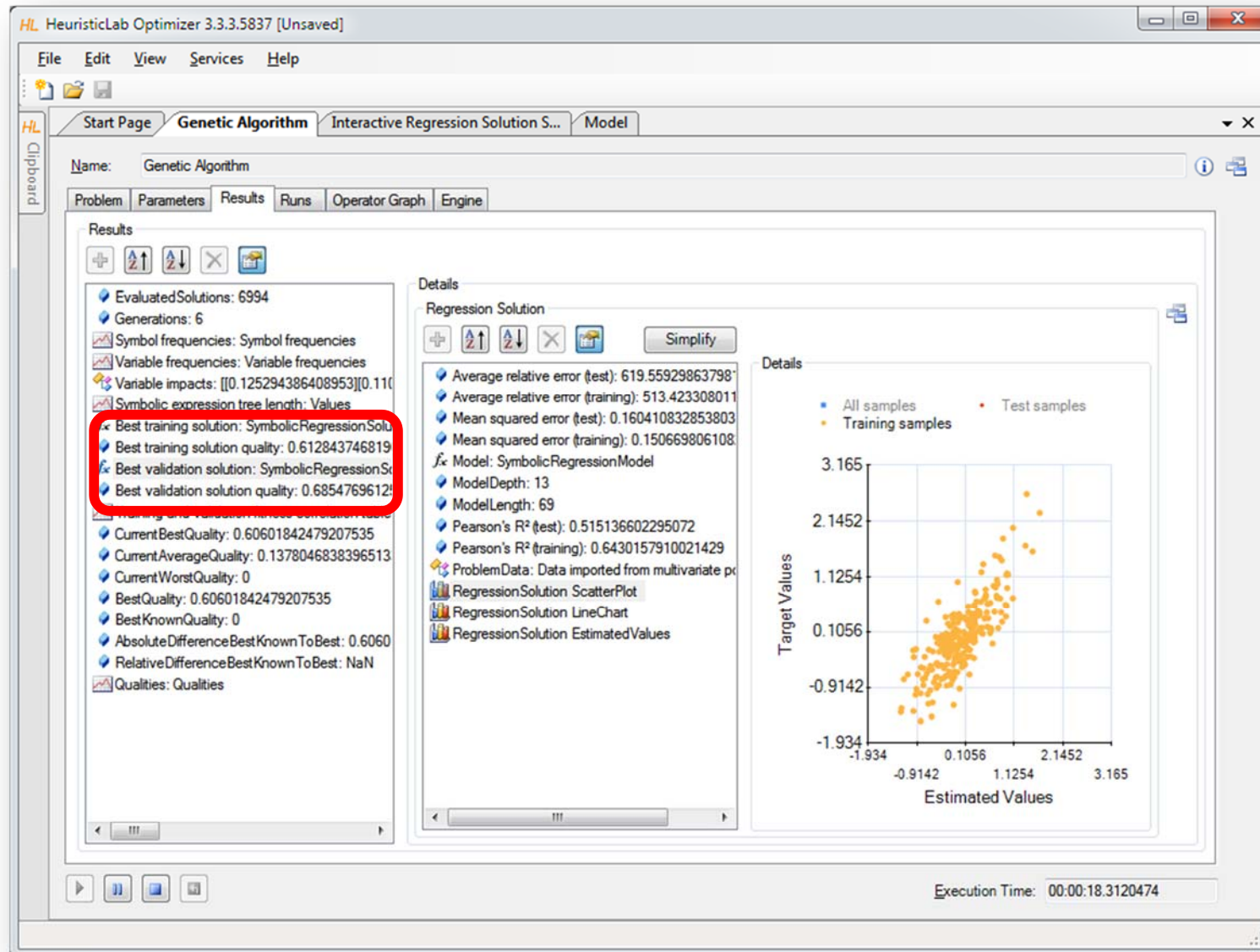
- Demonstration
  - Configuration of a validation set
  - Inspection of best solution on validation set
  - Analysis of training- and validation fitness correlation
  - Cross-validation
    - Configuration
    - Analysis of results



# Configuration of Validation Partition

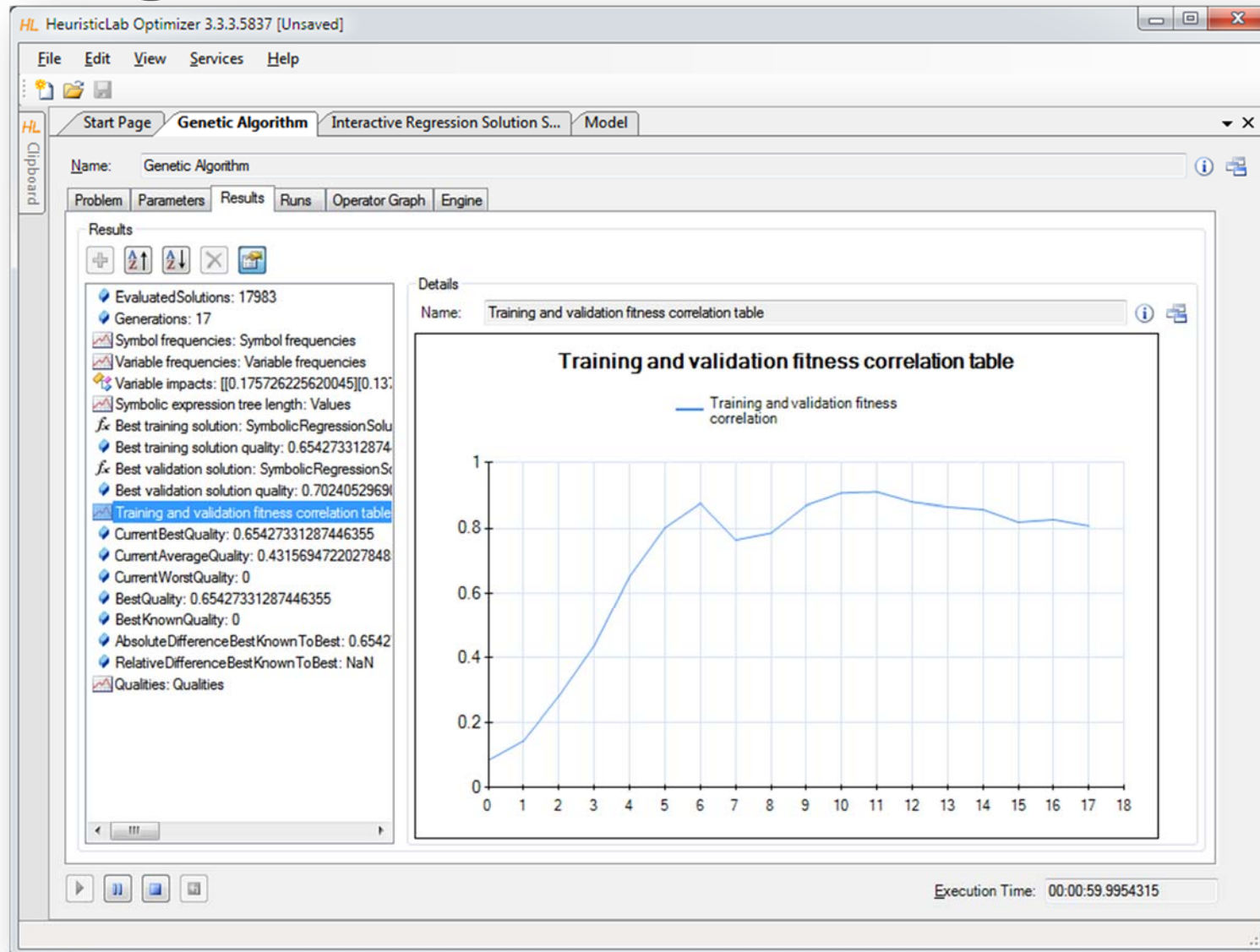


# Inspect Best Model on Validation Partition





# Inspect Linechart of Correlation of Training and Validation Fitness



# Agenda



- Objectives of the Tutorial
- Introduction
- Where to get HeuristicLab?
- Plugin Infrastructure
- Graphical User Interface
- Available Algorithms & Problems
  
- **Demonstration Part I: Working with HeuristicLab**
- **Demonstration Part II: Data-based Modeling**
  
- Some Additional Features
- Planned Features
- Team
- Suggested Readings
- Bibliography
- Questions & Answers

# Some Additional Features



- HeuristicLab Hive
  - parallel and distributed execution of algorithms and experiments on many computers in a network
- Optimization Knowledge Base (OKB)
  - database to store algorithms, problems, parameters and results
  - open to the public
  - open for other frameworks
  - analyze and store characteristics of problem instances and problem classes
- External solution evaluation and simulation-based optimization
  - interface to couple HeuristicLab with other applications (MATLAB, AnyLogic, ...)
  - supports different protocols (command line parameters, TCP, ...)
- Parameter grid tests and meta-optimization
  - automatically create experiments to test large ranges of parameters
  - apply heuristic optimization algorithms to find optimal parameter settings for heuristic optimization algorithms



# Planned Features

- Algorithms & Problems
  - steady-state genetic algorithm
  - unified tabu search for vehicle routing
  - scatter search
  - ...
- Cloud Computing
  - port HeuristicLab Hive to Windows Azure
- Linux
  - port HeuristicLab to run on Mono and Linux machines
- Have a look at the HeuristicLab roadmap
  - <http://dev.heuristiclab.com/trac/hl/core/roadmap>
- Any other ideas, requests or recommendations?
  - join our HeuristicLab Google group [heuristiclab@googlegroups.com](http://heuristiclab@googlegroups.com) or
  - write an e-mail to [support@heuristiclab.com](mailto:support@heuristiclab.com)

# HeuristicLab Team



Heuristic and Evolutionary Algorithms Laboratory (HEAL)  
School of Informatics, Communications and Media  
University of Applied Sciences Upper Austria

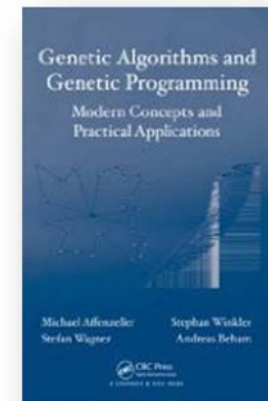
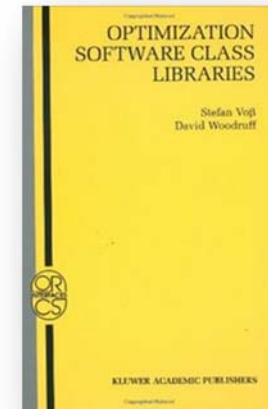
Softwarepark 11  
A-4232 Hagenberg  
AUSTRIA

WWW: <http://heal.heuristiclab.com>



# Suggested Readings

- S. Voß, D. Woodruff (Edts.)  
**Optimization Software Class Libraries**  
Kluwer Academic Publishers, 2002
- M. Affenzeller, S. Winkler, S. Wagner, A. Beham  
**Genetic Algorithms and Genetic Programming  
Modern Concepts and Practical Applications**  
CRC Press, 2009



# Bibliography



- S. Wagner, M. Affenzeller  
**HeuristicLab: A generic and extensible optimization environment**  
Adaptive and Natural Computing Algorithms, pp. 538-541  
Springer, 2005
- S. Wagner, S. Winkler, R. Braune, G. Kronberger, A. Beham, M. Affenzeller  
**Benefits of plugin-based heuristic optimization software systems**  
Computer Aided Systems Theory - EUROCAST 2007, Lecture Notes in Computer Science, vol. 4739, pp. 747-754  
Springer, 2007
- S. Wagner, G. Kronberger, A. Beham, S. Winkler, M. Affenzeller  
**Modeling of heuristic optimization algorithms**  
Proceedings of the 20th European Modeling and Simulation Symposium, pp. 106-111  
DIPTeM University of Genova, 2008
- S. Wagner, G. Kronberger, A. Beham, S. Winkler, M. Affenzeller  
**Model driven rapid prototyping of heuristic optimization algorithms**  
Computer Aided Systems Theory - EUROCAST 2009, Lecture Notes in Computer Science, vol. 5717, pp. 729-736  
Springer, 2009
- S. Wagner  
**Heuristic optimization software systems - Modeling of heuristic optimization algorithms in the HeuristicLab software environment**  
Ph.D. thesis, Johannes Kepler University Linz, Austria, 2009.
- S. Wagner, A. Beham, G. Kronberger, M. Kommenda, E. Pitzer, M. Kofler, S. Vonolfen, S. Winkler, V. Dorfer, M. Affenzeller  
**HeuristicLab 3.3: A unified approach to metaheuristic optimization**  
Actas del séptimo congreso español sobre Metaheurísticas, Algoritmos Evolutivos y Bioinspirados (MAEB'2010), 2010
- Detailed list of all publications of the HEAL research group: <http://research.fh-ooe.at/de/orgunit/detail/356#showpublications>

# Questions & Answers



<http://dev.heuristiclab.com>

[heuristiclab@googlegroups.com](mailto:heuristiclab@googlegroups.com)