



# HeuristicLab

A Paradigm-Independent and Extensible  
Environment for Heuristic Optimization

## Optimizing External Applications with HeuristicLab

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**HEAL**

Heuristic and Evolutionary  
Algorithms Laboratory



**Heuristic  
Optimization in  
Production and  
Logistics**

# Instructor Biographies

- Andreas Beham
  - Research Associate (since 2007)
  - Team: Combinatorial and Simulation-based Optimization
  - Graduate of Johannes Kepler University
  - PhD in progress
  - Member of the HEAL research group
  - Architect of HeuristicLab
  - <http://heal.heuristiclab.com/team/beham>
  
- Michael Kommenda
  - Research Associate (since 2008)
  - Team: System Identification and Data Analysis
  - Graduate of University of Applied Sciences Upper Austria
  - PhD in progress
  - Member of the HEAL research group
  - Architect of HeuristicLab
  - <http://heal.heuristiclab.com/team/kommenda>



# Latest Version of this Tutorial



- An up-to-date version of this tutorial can be downloaded from the HeuristicLab website
  - <http://dev.heuristiclab.com/trac.fcgi/browser/misc/documentation/Tutorials>

# Agenda

- Objectives of the Tutorial
- Introduction
- Where to get HeuristicLab?
- Plugin Infrastructure
- Graphical User Interface
- Available Algorithms & Problems
  
- **Demonstration Part I: External Evaluation Problem**
- **Demonstration Part II: MATLAB and Scilab Parameter Optimization Problem**
- **Demonstration Part III: Programmable Problem**
  
- Some Additional Features
- Planned Features
- Team
- Suggested Readings
- Bibliography
- Questions & Answers

# Objectives of the Tutorial

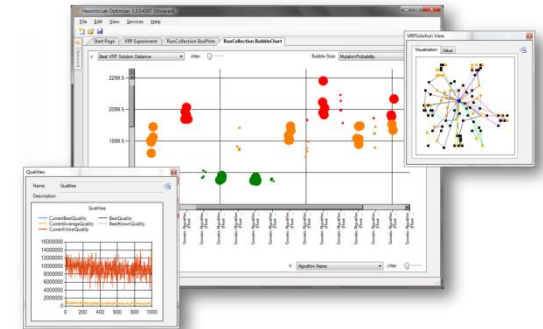


- Introduce general motivation and design principles of HeuristicLab
- Show where to get HeuristicLab
- Explain basic GUI usability concepts
- Demonstrate basic features
- Demonstrate optimization of parameters in external applications
- Demonstrate optimization of parameters in MATLAB and Scilab
- Demonstrate optimization of custom problem definitions
- Outline some additional features

# Introduction



- Motivation and Goals
  - graphical user interface
  - paradigm independence
  - multiple algorithms and problems
  - large scale experiments and analyses
  - parallelization
  - extensibility, flexibility and reusability
  - visual and interactive algorithm development
  - multiple layers of abstraction
- Facts
  - development of HeuristicLab started in 2002
  - based on Microsoft .NET and C#
  - used in research and education
  - second place at the *Microsoft Innovation Award 2009*
  - open source (GNU General Public License)
  - version 3.3.0 released on May 18th, 2010
  - latest version 3.3.15 “Berlin”
    - released on January 11th, 2018



# Where to get HeuristicLab?

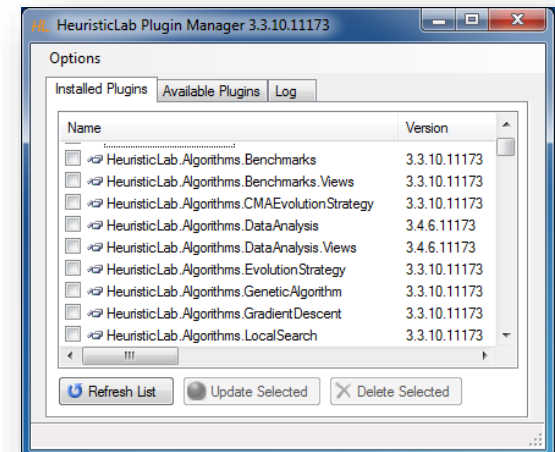
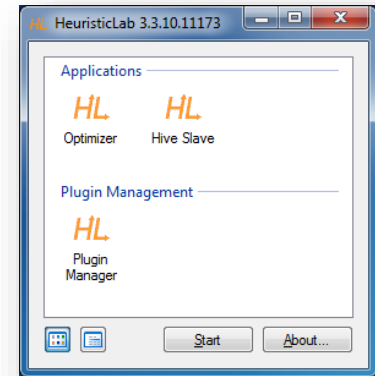


- Download binaries
  - deployed as ZIP archives
  - latest stable version 3.3.15 “Berlin”
    - released on January 11th, 2018
  - daily trunk builds
  - <http://dev.heuristiclab.com/download>
- Check out sources
  - SVN repository
  - HeuristicLab 3.3.15 tag
    - <https://src.heuristiclab.com/svn/core/tags/3.3.15>
  - Stable development version
    - <https://src.heuristiclab.com/svn/core/stable>
- License
  - GNU General Public License (Version 3)
- System requirements
  - Microsoft .NET Framework 4.5
  - enough RAM and CPU power ;-)

A screenshot of the HeuristicLab website. The page has a white background with a navigation bar at the top containing links for Home, News, Download, Features, Documentation, Support, and Search. Below the navigation bar is a main content area with a heading 'HeuristicLab' and a sub-heading 'A Paradigm-Independent and Extensible Environment for Heuristic Optimization'. The main content area contains a paragraph of text, a video player titled 'HeuristicLab Tour', a list of features, a download button for 'HeuristicLab 3.3', and a section for 'Research &amp; Publications'. The video player shows a screenshot of the HeuristicLab software interface with a play button in the center. The list of features includes Graphical User Interface, Algorithm Prototyping, Evolutionary Algorithms, Genetic Programming, Data Analysis, Simulation-based Optimization, Experiment Design and Analysis, and Plugin-based Architecture. The download button is orange and has a download icon. The 'Research &amp; Publications' section shows a group photo of people and a 'GPL Free Software' logo. The 'Join the discussion at the HeuristicLab group' section has an email input field and 'Subscribe' and 'Visit group' buttons. At the bottom of the page, there is a 'Thank you!' section with a 'ReSharper' logo and a 'Download in other formats' section with a 'Plain Text' link. The page footer includes the 'trac' logo and the text 'Powered by Trac 1.0.1 By Edgewall Software.' and 'Visit the Trac open source project at http://trac.edgewall.org/'.

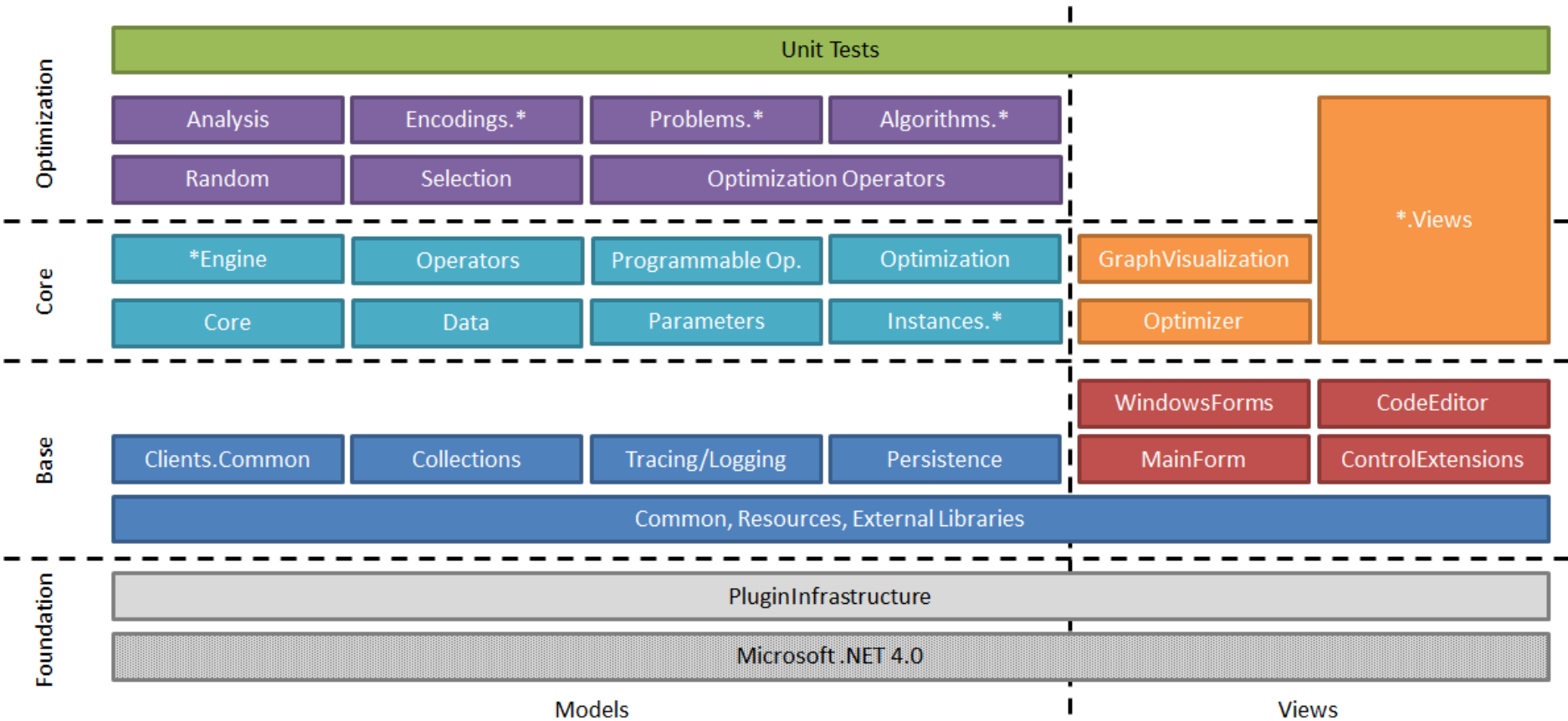
# Plugin Infrastructure

- HeuristicLab consists of many assemblies
  - 160+ plugins in HeuristicLab 3.3.15
  - plugins can be loaded or unloaded at runtime
  - plugins can be updated via internet
  - application plugins provide GUI frontends
- Extensibility
  - developing and deploying new plugins is easy
  - dependencies are explicitly defined, automatically checked and resolved
  - automatic discovery of interface implementations (service locator pattern)
- Plugin Manager
  - GUI to check, install, update or delete plugins





# Plugin Architecture

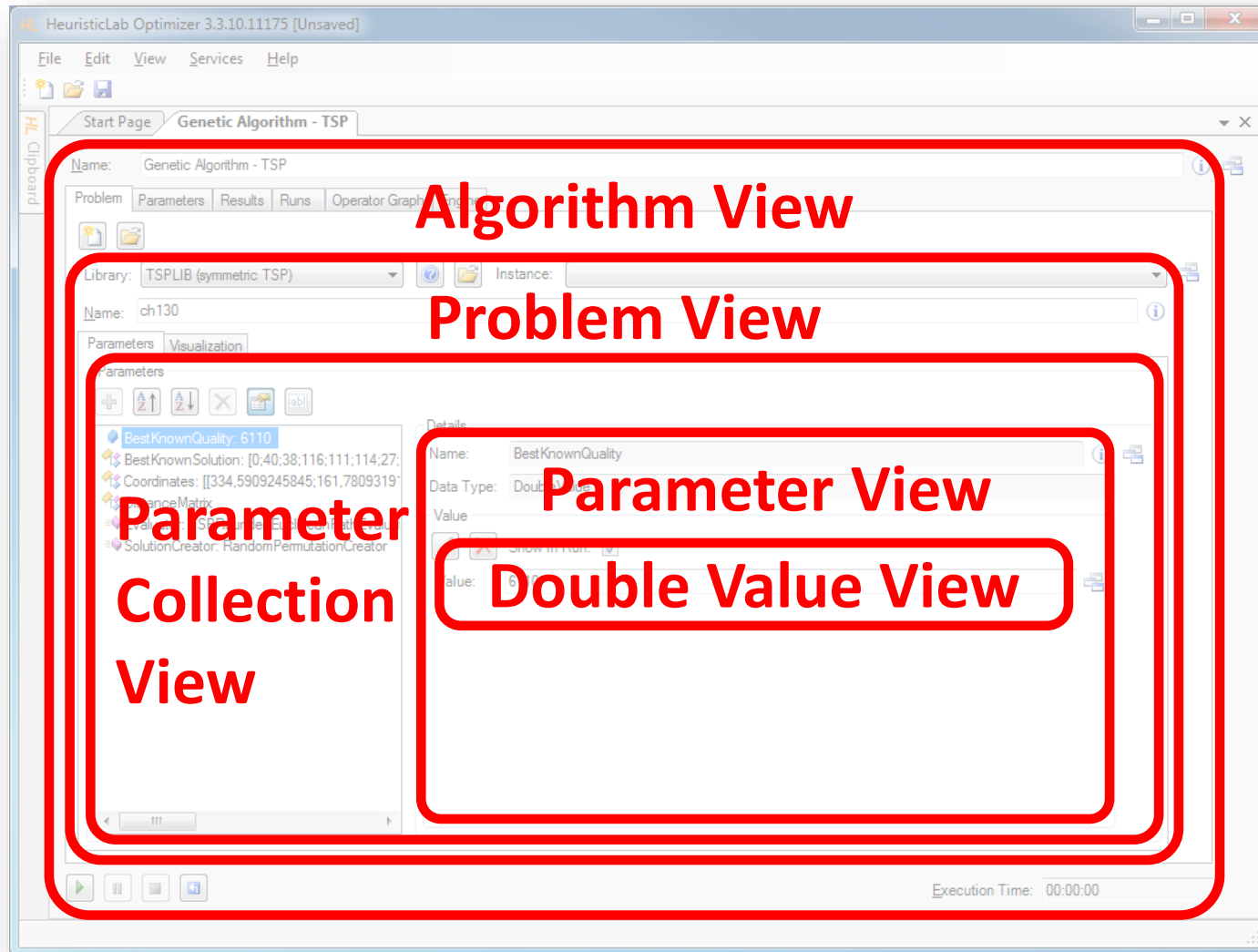


# Graphical User Interface



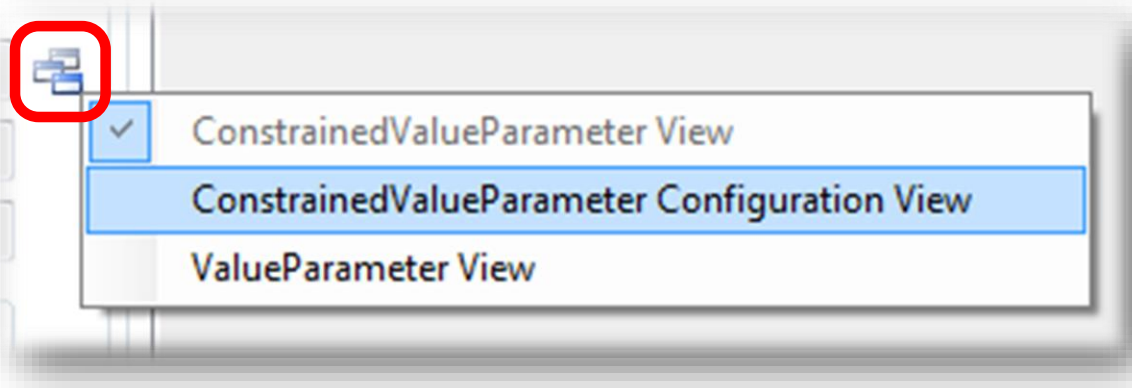
- HeuristicLab GUI is made up of views
  - views are visual representations of content objects
  - views are composed in the same way as their content
  - views and content objects are loosely coupled
  - multiple different views may exist for the same content
- Drag & Drop
  - views support drag & drop operations
  - content objects can be copied or moved (shift key)
  - enabled for collection items and content objects

# Graphical User Interface



# Graphical User Interface

- ViewHost
  - control which hosts views
  - right-click on windows icon to switch views
  - double-click on windows icon to open another view
  - drag & drop windows icon to copy contents



# Available Algorithms

## Population-based

- CMA-ES
- Evolution Strategy
- Genetic Algorithm
- Offspring Selection Genetic Algorithm (OSGA)
- Island Genetic Algorithm
- Island Offspring Selection Genetic Algorithm
- Parameter-less Population Pyramid (P3)
- SASEGASA
- Relevant Alleles Preserving GA (RAPGA)
- Age-Layered Population Structure (ALPS)
- Genetic Programming
- NSGA-II
- Scatter Search
- Particle Swarm Optimization

## Trajectory-based

- Local Search
- Tabu Search
- Robust Taboo Search
- Variable Neighborhood Search
- Simulated Annealing

## Data Analysis

- Linear Discriminant Analysis
- Linear Regression
- Multinomial Logit Classification
- k-Nearest Neighbor
- k-Means
- Neighbourhood Component Analysis (NCA)
- Artificial Neural Networks
- Random Forests
- Support Vector Machines
- Gaussian Processes
- Gradient Boosted Trees
- Gradient Boosted Regression
- Barnes-Hut t-SNE
- Kernel Ridge Regression
- Elastic-net Regression

## Additional Algorithms

- Performance Benchmarks
- Hungarian Algorithm
- Cross Validation
- LM-BFGS

# Available Problems

## Combinatorial Problems

- Test Problems (1-max, NK, HIFF, Deceptive Trap)
- Traveling Salesman
- Probabilistic Traveling Salesman
- Vehicle Routing (MDCVRPTW, PDPTW, ...)
- Knapsack
- Bin Packing
- Graph Coloring
- Job Shop Scheduling
- Linear Assignment
- Quadratic Assignment
- Orienteering

## Genetic Programming Problems

- Test Problems (Even Parity, MUX)
- Symbolic Classification
- Symbolic Regression
- Symbolic Time-Series Prognosis
- Artificial Ant
- Lawn Mower
- Robocode
- Grammatical Evolution

## Additional Problems

- Single-/Multi-Objective Test Functions
  - Ackley, Griewank, Rastrigin, Sphere, etc.
- Programmable Problem
- External Evaluation Problem (generic TCP/IP, Scilab, MATLAB)
- Regression, Classification, Clustering
- Trading

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# Demonstration Part I: External Evaluation Problem

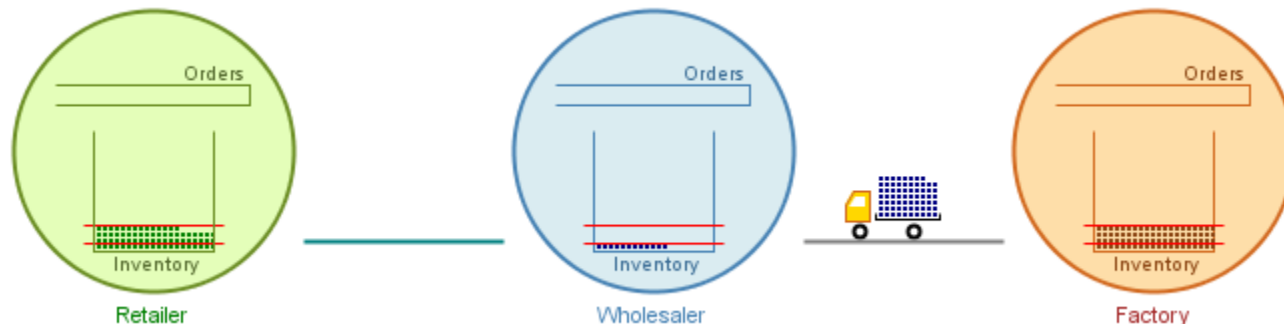


- Optimize parameters of an existing simulation model
- Implement necessary steps to talk with HeuristicLab



# Supply Chain Simulation

- $(s, S)$  Order Policy
  - 3 Echelons and 2 Parameters per Echelon
  - Minimize Inventory and Ordering Costs
  - Maintain a minimum service level
    - Bound on the waiting time due to „out of stock“ situations



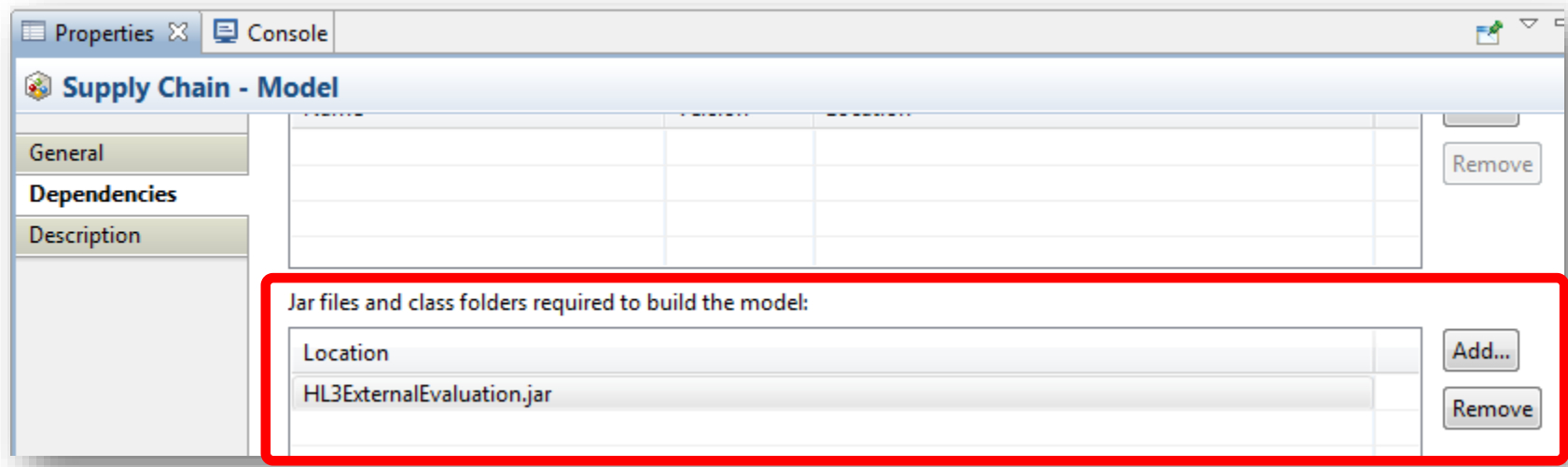
# Supply Chain Simulation



- Create a new simulation experiment for evaluating parameters from HeuristicLab
- Create the problem definition in HeuristicLab
- Optimize

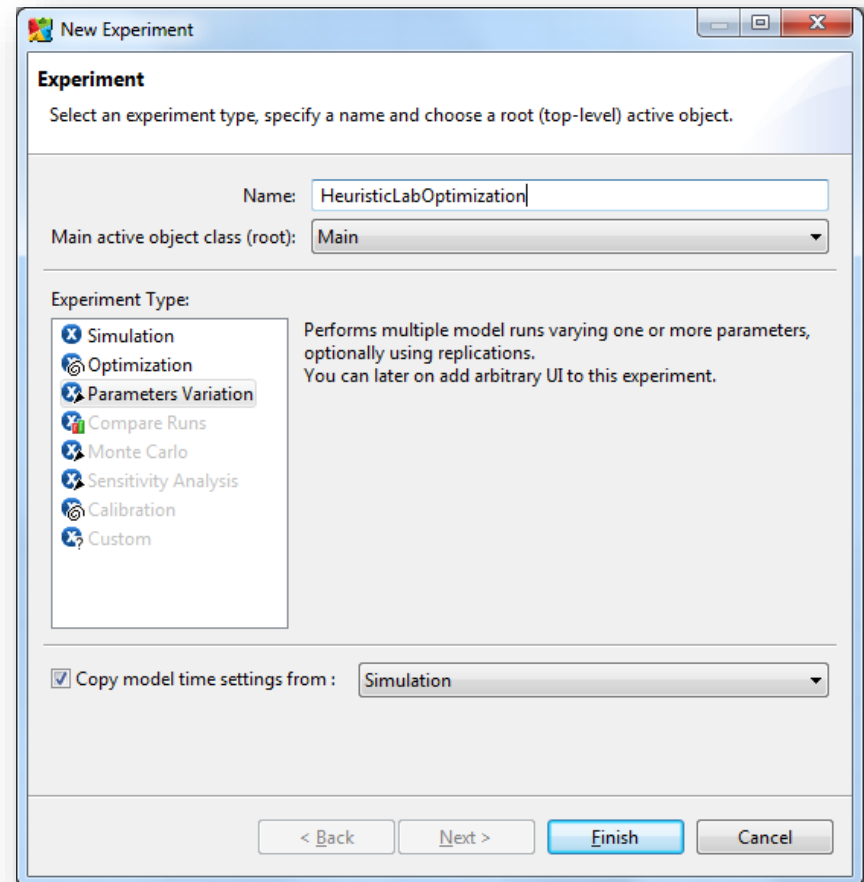
# Supply Chain Simulation

- Download communication helper library
  - <http://dev.heuristiclab.com/trac.fcgi/wiki/Documentation/Howto/OptimizeExternalApplications#no1>
- Add library as dependency to the model



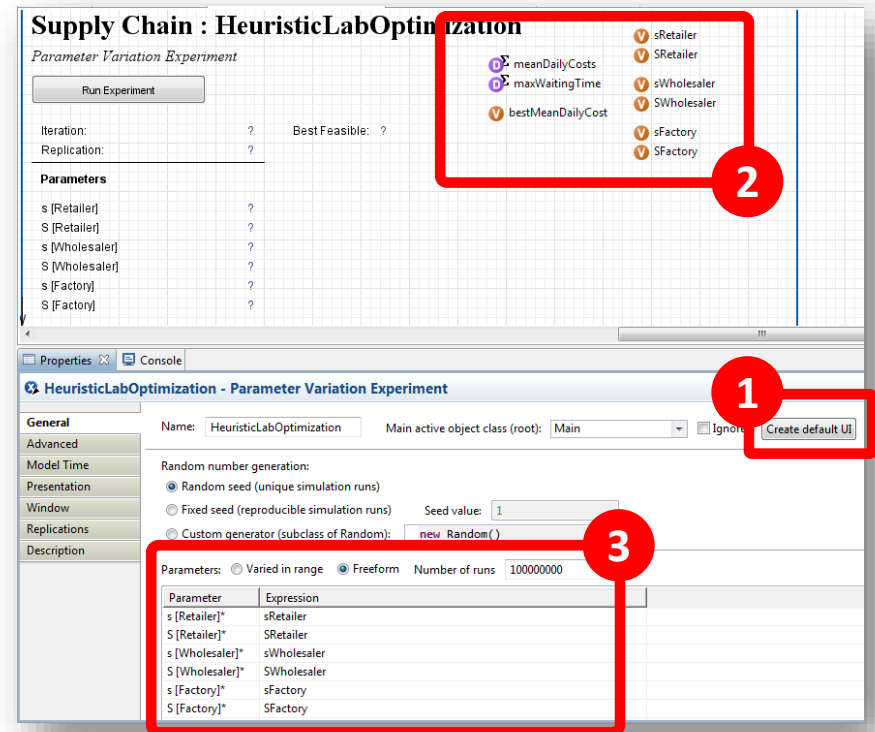
# Supply Chain Simulation

- The model is included as a sample in AnyLogic
- Open the model and create a new experiment of type „Parameters Variation“



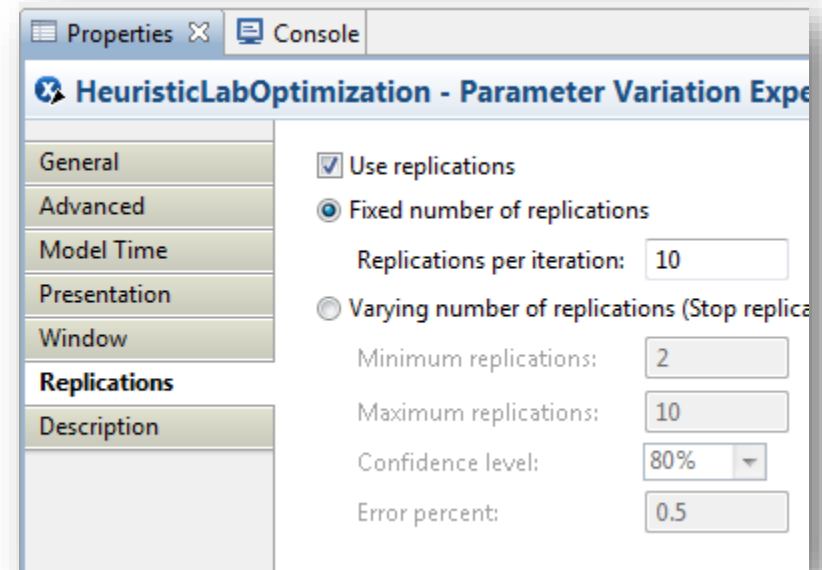
# Supply Chain Simulation

- Configure the experiment
  1. Create the default user interface by clicking the button
  2. Add one variable for each parameter and add statistics for collecting quality relevant information over multiple replications
  3. Select to vary parameters Freeform, use an arbitrary, but high number of runs and specify the variable that is assigned to each parameter
  4. Optional: remember the best identified solution so far



# Supply Chain Simulation

- Switch to the Replications tab
- Check the box „Use replications“
- Use a fixed number of 10 replications

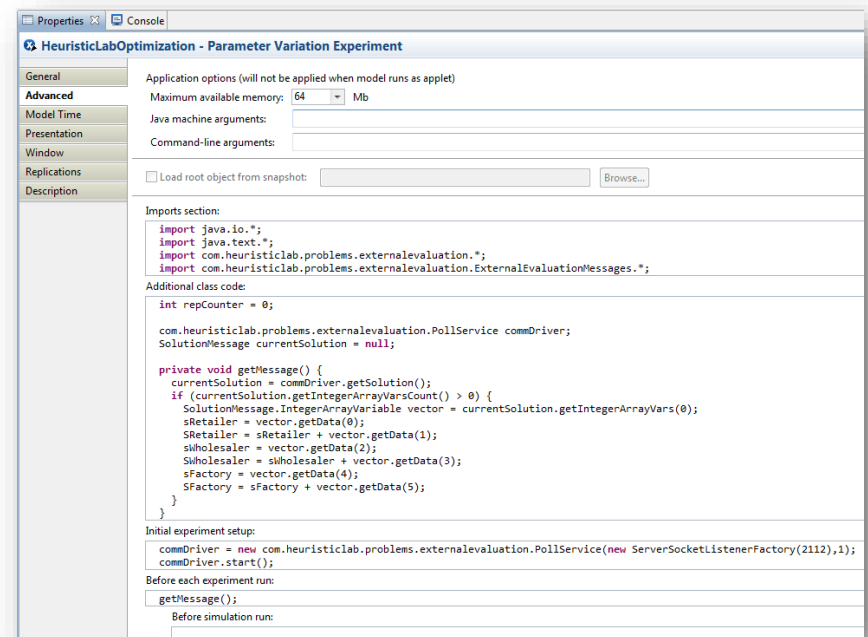


# Supply Chain Simulation

- How do parameter variation experiments work in AnyLogic?
- In an experiment run there are N iterations
- In each iteration R runs execute
  
- N = „Number of runs“ on the General tab
- R = „Replications per iteration“

# Supply Chain Simulation

- Switch to the Advanced tab, here we need to enter some code
  1. Initialize the communication
  2. Receive parameters from HeuristicLab
  3. Collect statistics after each run
  4. Send back the averaged results and continue with step 2



```
HeuristicLabOptimization - Parameter Variation Experiment

Application options (will not be applied when model runs as applet)
Maximum available memory: 64 Mb
Java machine arguments:
Command-line arguments:

Load root object from snapshot: Browse...

Imports section:
import java.io.*;
import java.text.*;
import com.heuristiclab.problems.externalevaluation.*;
import com.heuristiclab.problems.externalevaluation.ExternalEvaluationMessages.*;

Additional class code:
int repCounter = 0;

com.heuristiclab.problems.externalevaluation.PollService cmdDriver;
SolutionMessage currentSolution = null;

private void getMessage() {
    currentSolution = cmdDriver.getSolution();
    if (currentSolution.getIntegerArrayVarsCount() > 0) {
        SolutionMessage.IntegerArrayVariable vector = currentSolution.getIntegerArrayVars(0);
        sRetailer = vector.getData(0);
        sRetailer = sRetailer + vector.getData(1);
        sWholesaler = vector.getData(2);
        sWholesaler = sWholesaler + vector.getData(3);
        sFactory = vector.getData(4);
        sFactory = sFactory + vector.getData(5);
    }
}

Initial experiment setup:
cmdDriver = new com.heuristiclab.problems.externalevaluation.PollService(new ServerSocketListenerFactory(2112),1);
cmdDriver.start();

Before each experiment run:
getMessage();

Before simulation run:
```



# Supply Chain Simulation

- Imports section:

```
import java.io.*;
import java.text.*;
import com.heuristiclab.problems.externalevaluation.*;
import com.heuristiclab.problems.externalevaluation.ExternalEvaluationMessages.*;
```

- Additional class code:

```
com.heuristiclab.problems.externalevaluation.PollService commDriver;
SolutionMessage currentSolution = null;
```

```
private void getMessage() {
    currentSolution = commDriver.getSolution();
    if (currentSolution.getIntegerArrayVarsCount() > 0) {
        SolutionMessage.IntegerArrayVariable vector = currentSolution.getIntegerArrayVars(0);
        sRetailer = vector.getData(0);
        SRetailer = sRetailer + vector.getData(1);
        sWholesaler = vector.getData(2);
        SWholesaler = sWholesaler + vector.getData(3);
        sFactory = vector.getData(4);
        SFactory = sFactory + vector.getData(5);
    }
}
```

# Supply Chain Simulation

- Initial experiment setup:

```
commDriver = new com.heuristiclab.problems.externalevaluation.PollService(new  
ServerSocketListenerFactory(2112), 1);  
commDriver.start();
```

- Before each experiment run:

```
getMessage();
```

- After simulation run:

```
meanDailyCosts.add(root.meanDailyCost());  
maxWaitingTime.add(root.histWaitingTime.max());
```

# Supply Chain Simulation

- After iteration:

```
double fitness = 0;
Boolean isFeasible = maxWaitingTime.max() < 0.001;

if (isFeasible) {
    fitness = meanDailyCosts.mean();
    if (meanDailyCosts.mean() < bestMeanDailyCost)
        bestMeanDailyCost = meanDailyCosts.mean();
} else {
    fitness = 2000 + maxWaitingTime.max();
}

try {
    commDriver.sendQuality(currentSolution, fitness);
} catch (IOException e) { /* handle error */ }

meanDailyCosts.reset();
maxWaitingTime.reset();

getMessage();
```

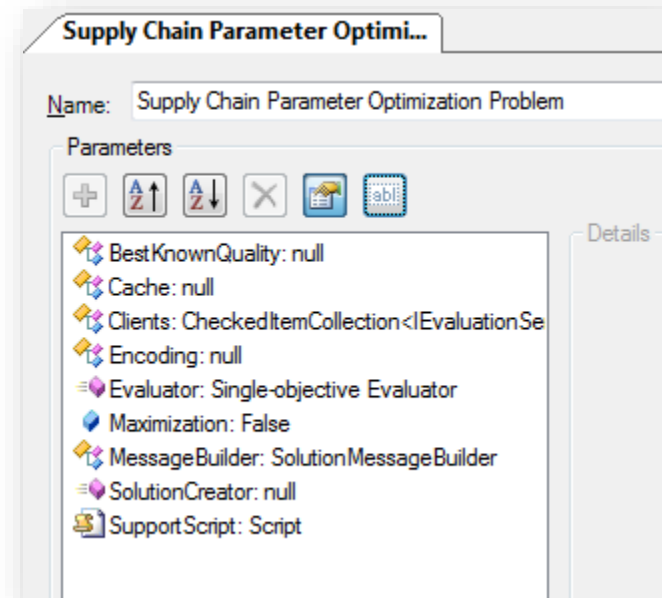
# Supply Chain Simulation



- Create a new simulation experiment for evaluating parameters from HeuristicLab
- Create the problem definition in HeuristicLab
- Optimize

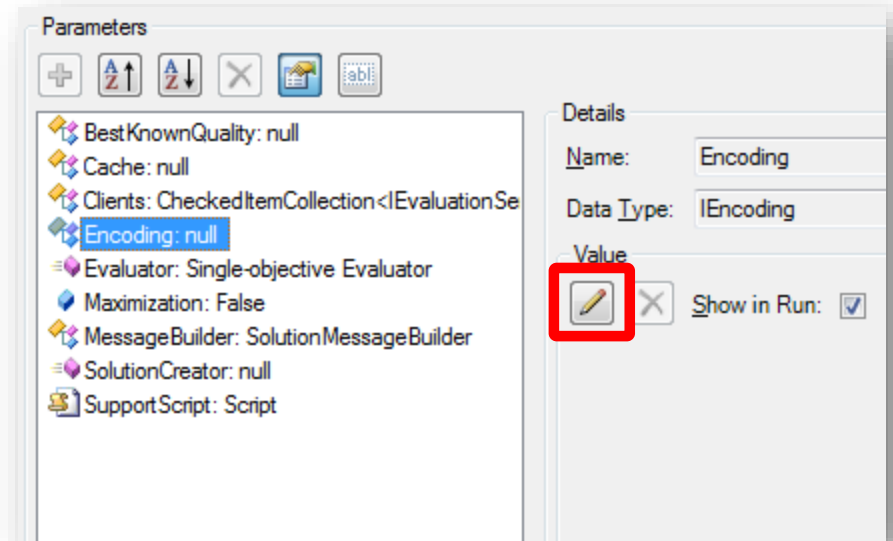
# Supply Chain Simulation

- **Cache:** optional parameter that caches solutions and their corresponding quality
- **Clients:** the simulation model instances that can evaluate parameters
- **Encoding:** The encoding that describes a solution, e.g. a vector of integer values
- **Evaluator:** The operator that will extract the parameters and transmit them to the model
- **Maximization:** Whether the returned fitness is to be minimized or maximized
- **SolutionCreator:** The operator that will construct the initial solutions
- **SupportScript:** Additional code for analyzing solution candidates as well as ability to define a neighborhood function



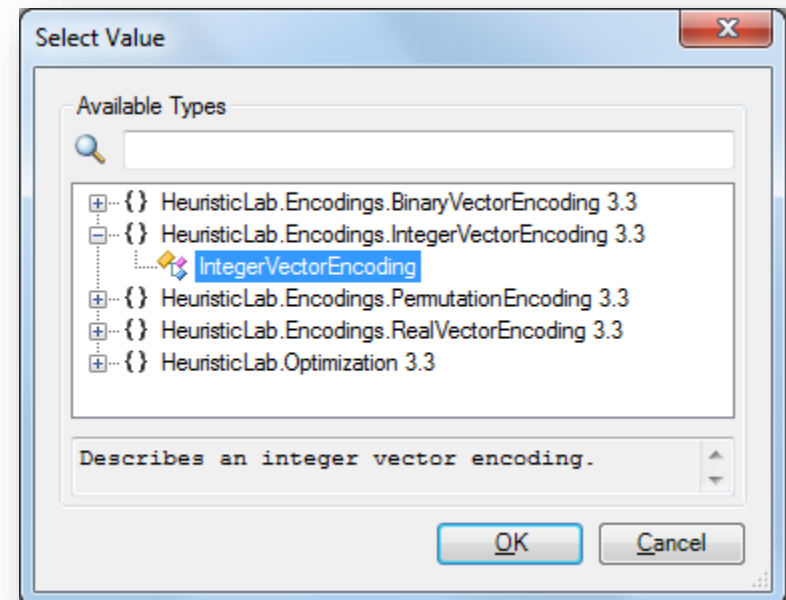
# Supply Chain Simulation

- Click on the Encoding parameter
- Click on the pencil icon to choose an encoding



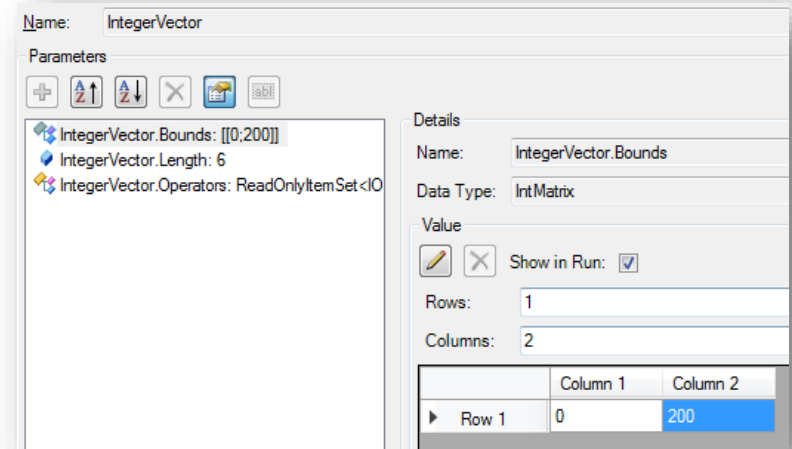
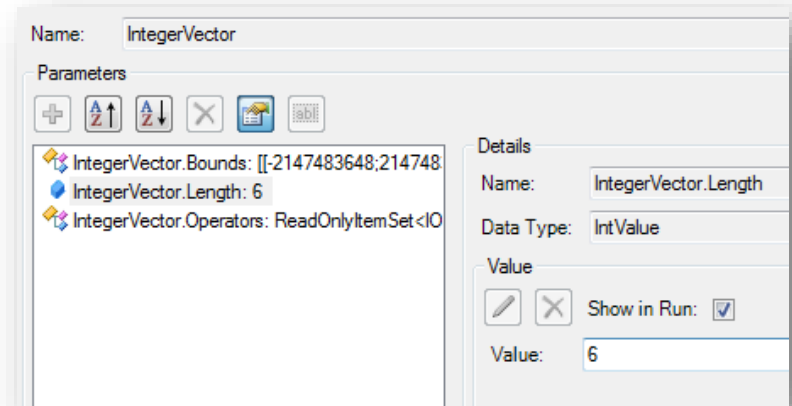
# Supply Chain Simulation

- Select the *IntegerVectorEncoding* from the list of available types
- Click OK



# Supply Chain Simulation

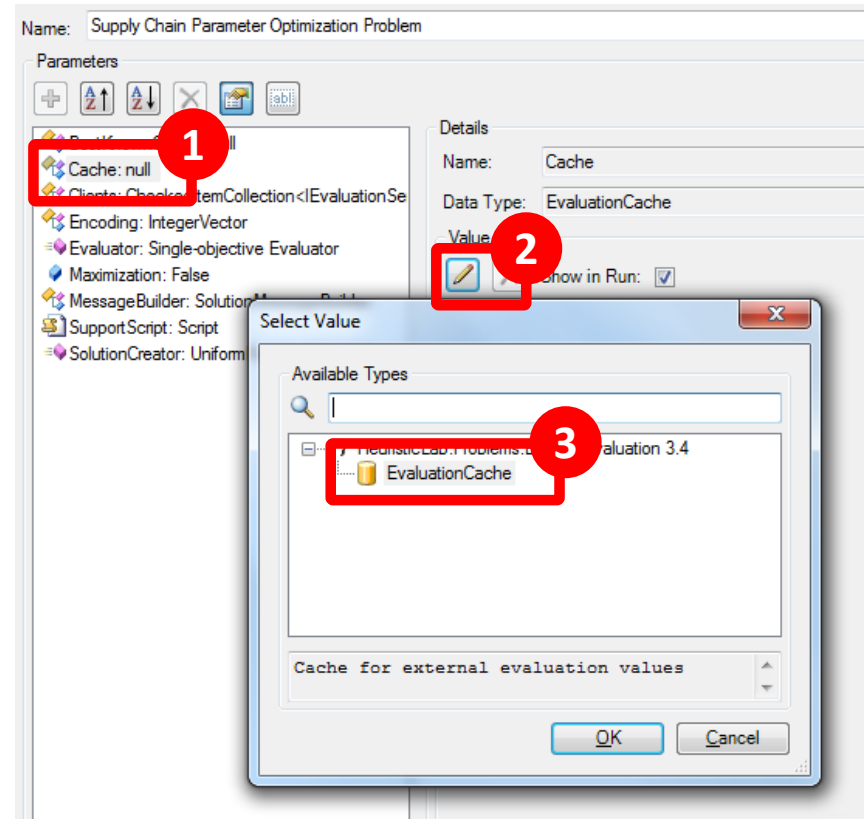
- Adjust the parameters of the Encoding
  - Change the Length to 6
  - Change the Bounds to be 0 and 200 for all 6 dimensions
- The columns in the bounds specify lower and upper bound for each dimension respectively
  - If you have less rows in the bounds than dimensions in the vector, the bounds will be cycled





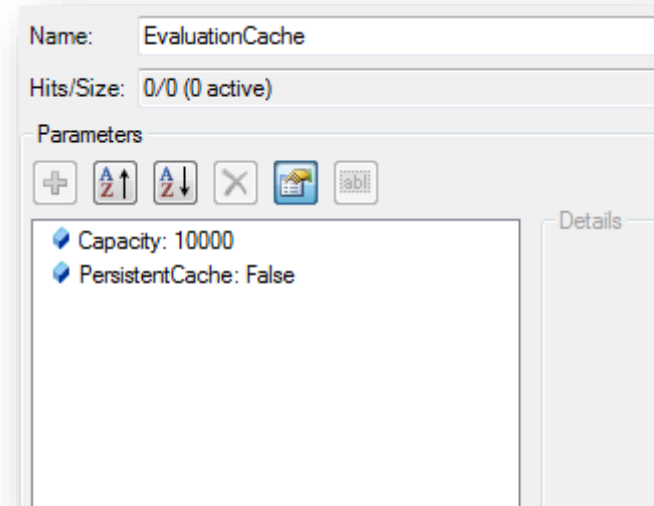
# Supply Chain Simulation

- Click on the Cache parameter
- Click on the pencil icon to assign a value
  - A dialog will pop up
- In the dialog select the EvaluationCache
- Click Ok



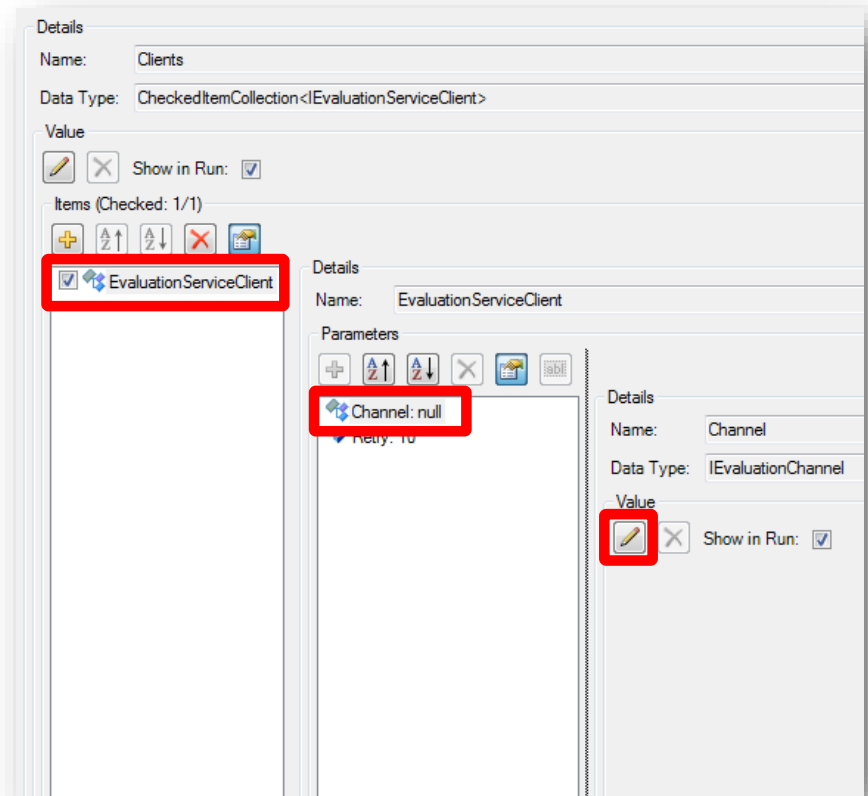
# Supply Chain Simulation

- The cache will store the solution message and the returned quality
- New solution messages will be compared against those already inside the cache
- The capacity of the cache can be adjusted
- PersistentCache determines if the cache should be stored when the problem or algorithm is saved



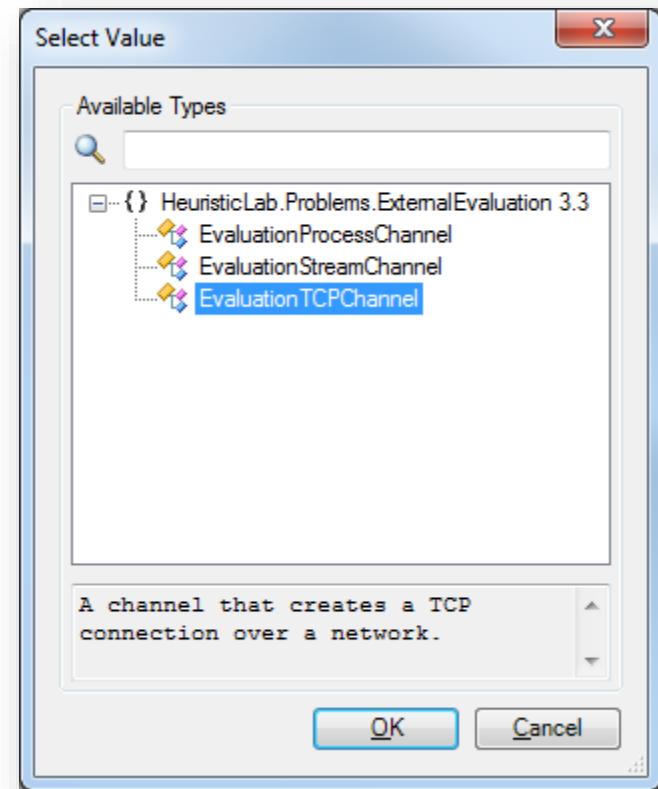
# Supply Chain Simulation

- Now set up the client machine that runs the simulation model
- Click on the Client parameter
- Click on EvaluationServiceClient
- Click on the Channel parameter
- Click the pencil icon to set a new channel



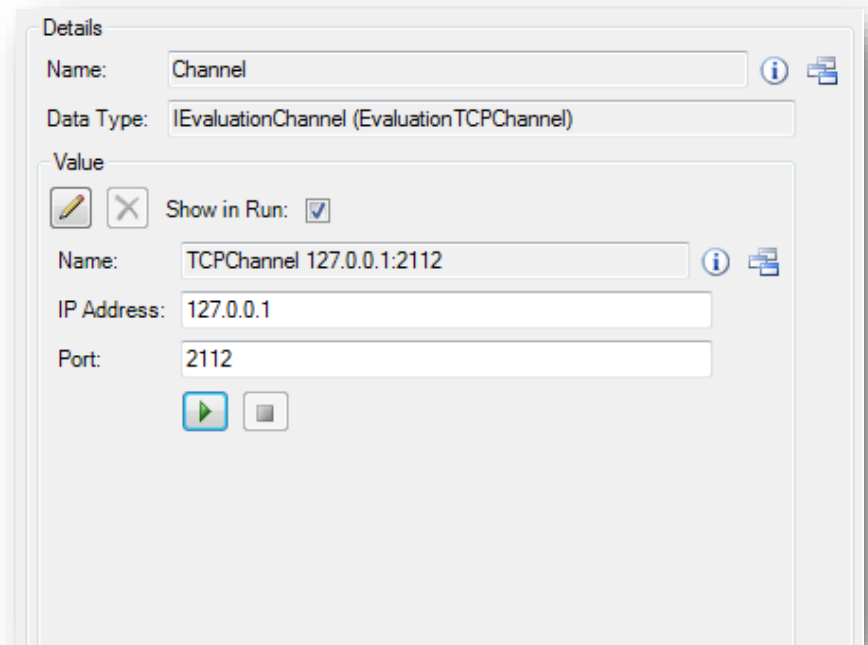
# Supply Chain Simulation

- Select the EvaluationTCPChannel for communicating over a TCP/IP connection
- Click OK



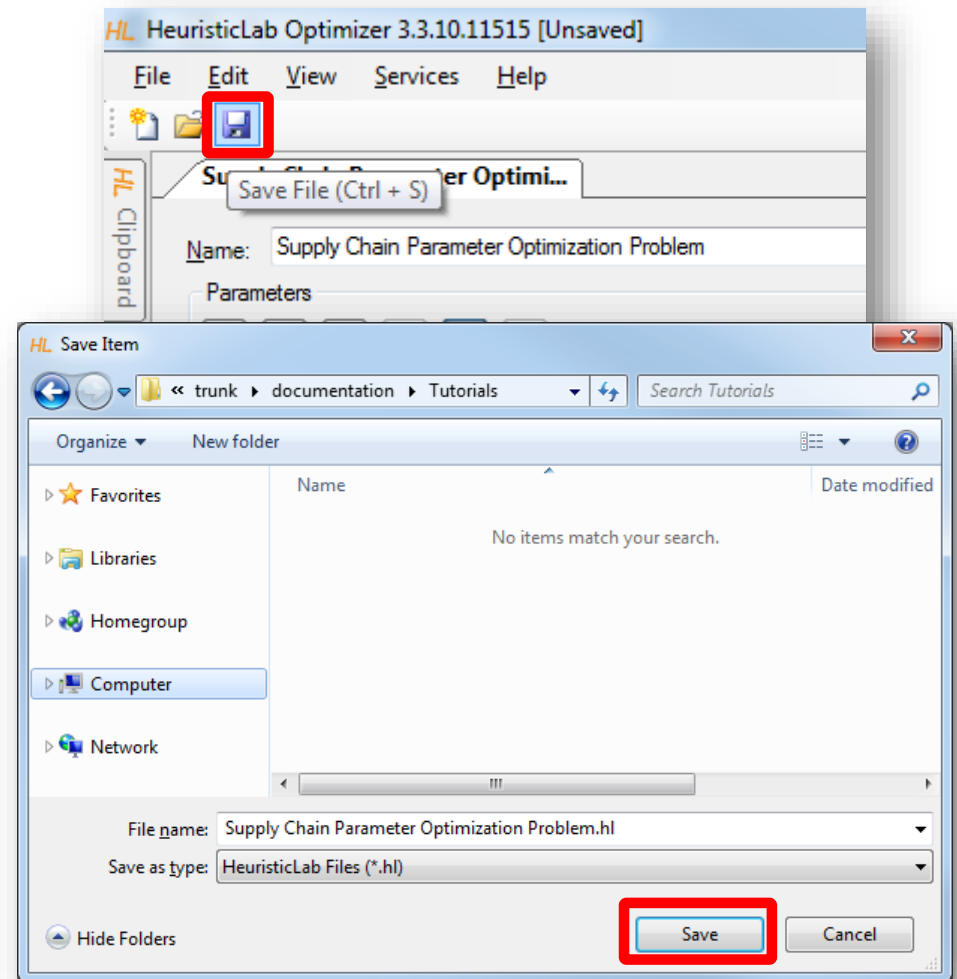
# Supply Chain Simulation

- Enter the IP address of the machine that the models runs on, use 127.0.0.1 if the model runs on the same machine
- We configured our model to listen on port 2112 so we enter this information as Port



# Supply Chain Simulation

- The problem is now configured
- Click the save button to store the external problem definition into a file



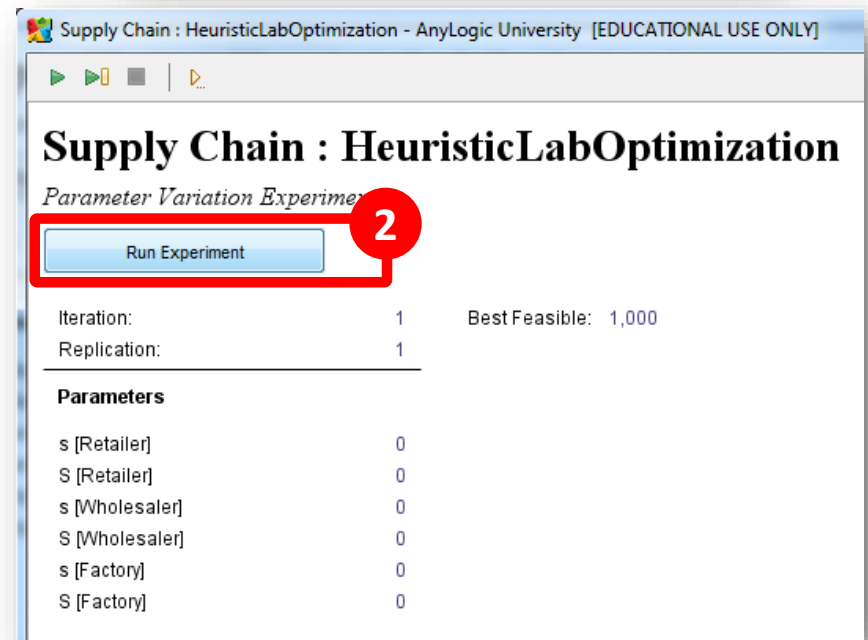
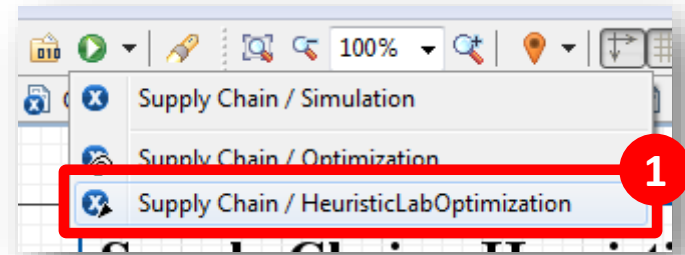
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- Create a new simulation experiment for evaluating parameters from HeuristicLab
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# Supply Chain Simulation

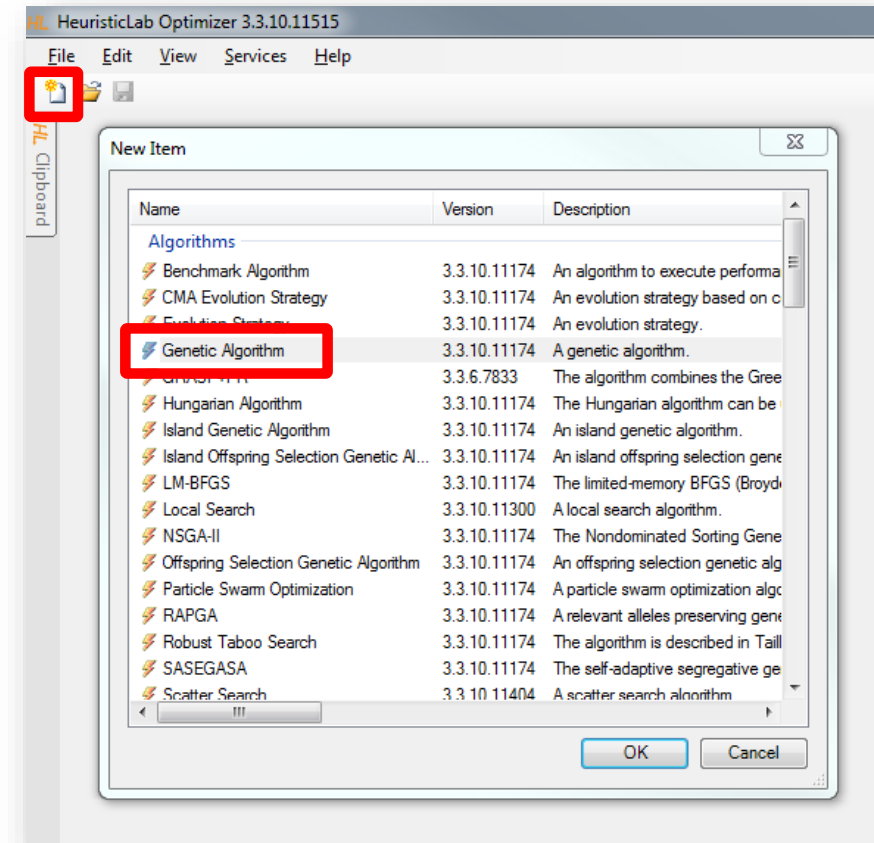
- In AnyLogic click the arrow next to the green play button and select our newly created experiment
- Click to run the experiment at which point the model will wait to receive a solution message





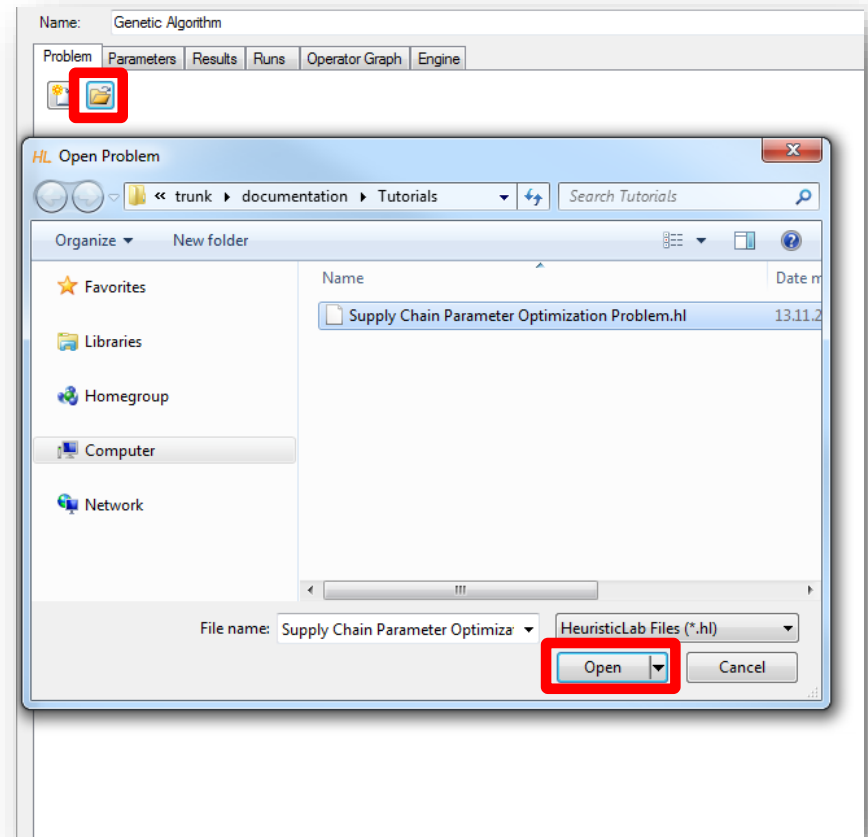
# Supply Chain Simulation

- In HeuristicLab click on the „New Item“ button to open the list of creatable items
- Select the Genetic Algorithm entry
- Click OK



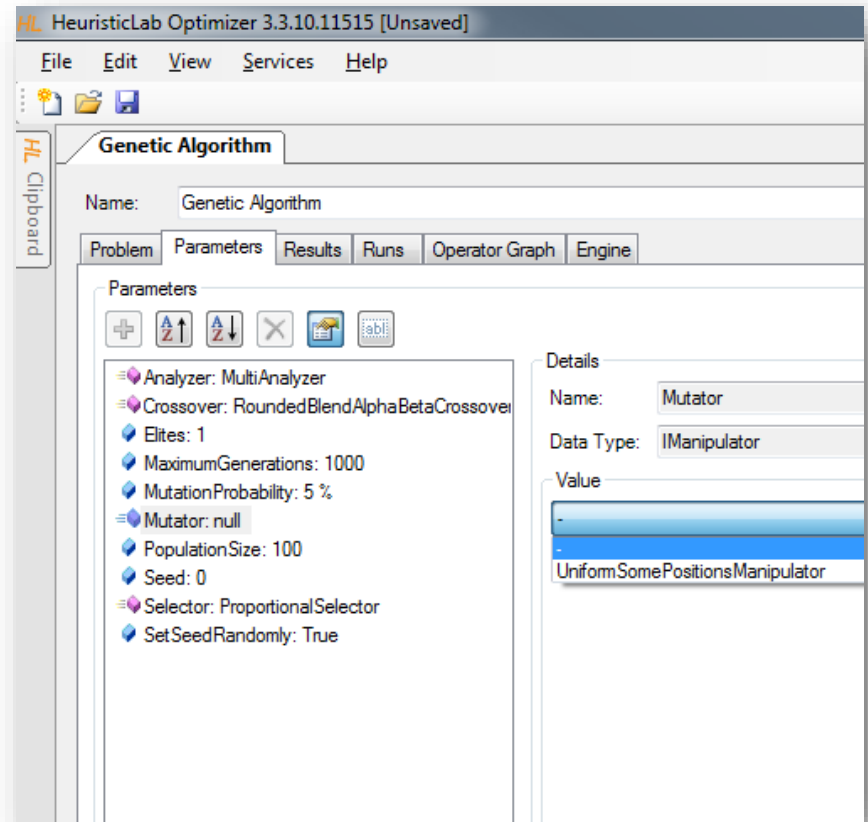
# Supply Chain Simulation

- Click on the Open button and select the previously saved problem definition
- Click Open in the dialog

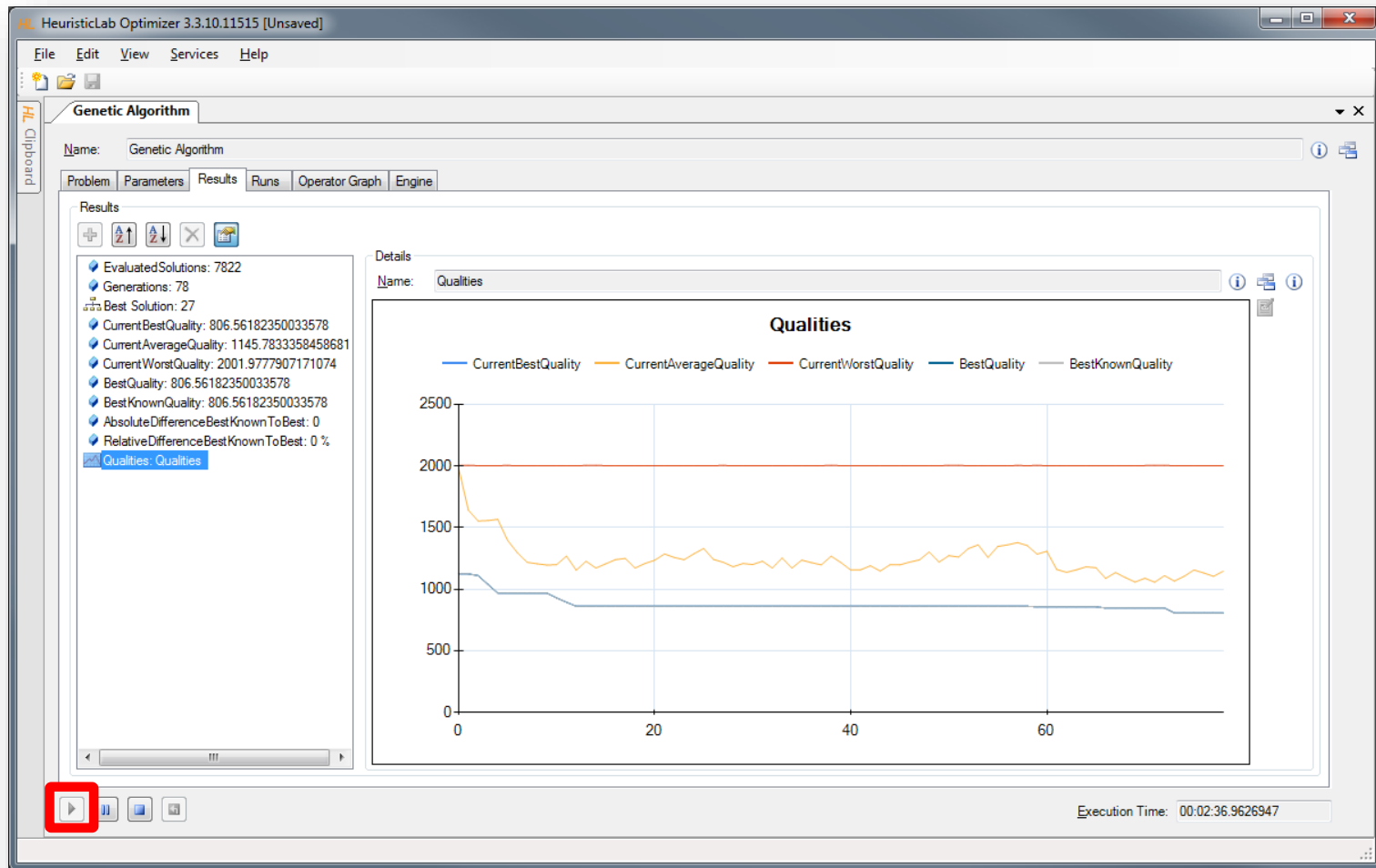


# Supply Chain Simulation

- Click on the Mutator parameter
- Select the manipulator that we have added to the operators list in one of the previous steps
- Switch to the Results tab and hit the play button at the bottom



# Supply Chain Simulation



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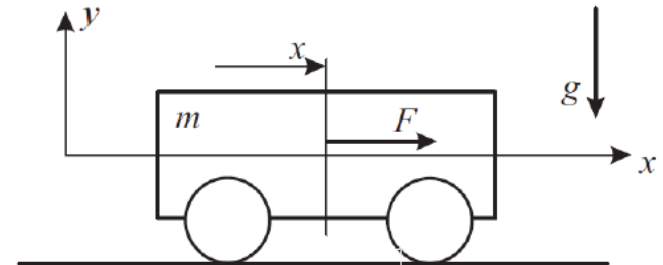
# Demonstration Part II: Parameter Optimization Problem



- Parameter Optimization of Differential Equation Systems (Scilab)

# Electric cart simulation

- Identify unknown parameter values of a simulation model
- Measure movements of an electric cart with known power
- Adapt parameters of an simulation model to match those measurements



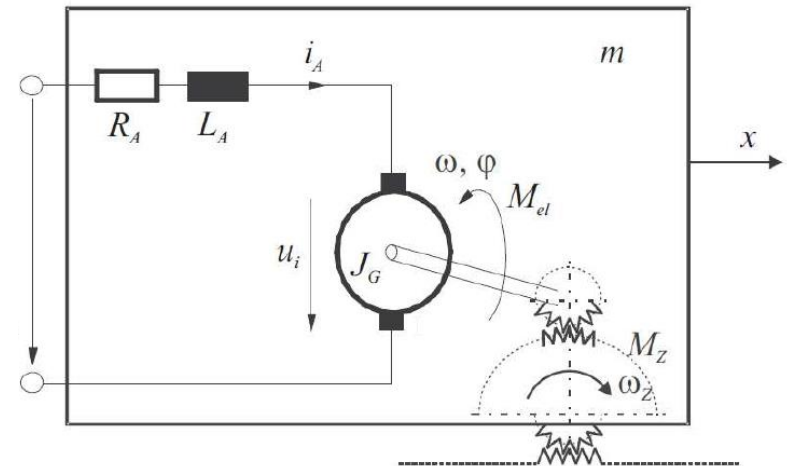
# Electric cart simulation

- Identify friction coefficients  $d_1$ ,  $F_C$  and mass  $m$
- Voltage  $u_A$  and initial values for position  $x$ , velocity  $v$  and amperage  $i_A$  are known
- Simulate changes according to differential equations

$$\dot{x} = v$$

$$\dot{v} = -\frac{d_1}{\tilde{m}} \cdot v - \frac{1}{\tilde{m}} F_C \text{sign}(v) + \frac{k_m \cdot n}{r \cdot \tilde{m}} \cdot i_A$$

$$\dot{i}_A = -\frac{k_m \cdot n}{L_A \cdot r} \cdot v - \frac{R_A}{L_A} \cdot i_A + \frac{u_A}{L_A}$$

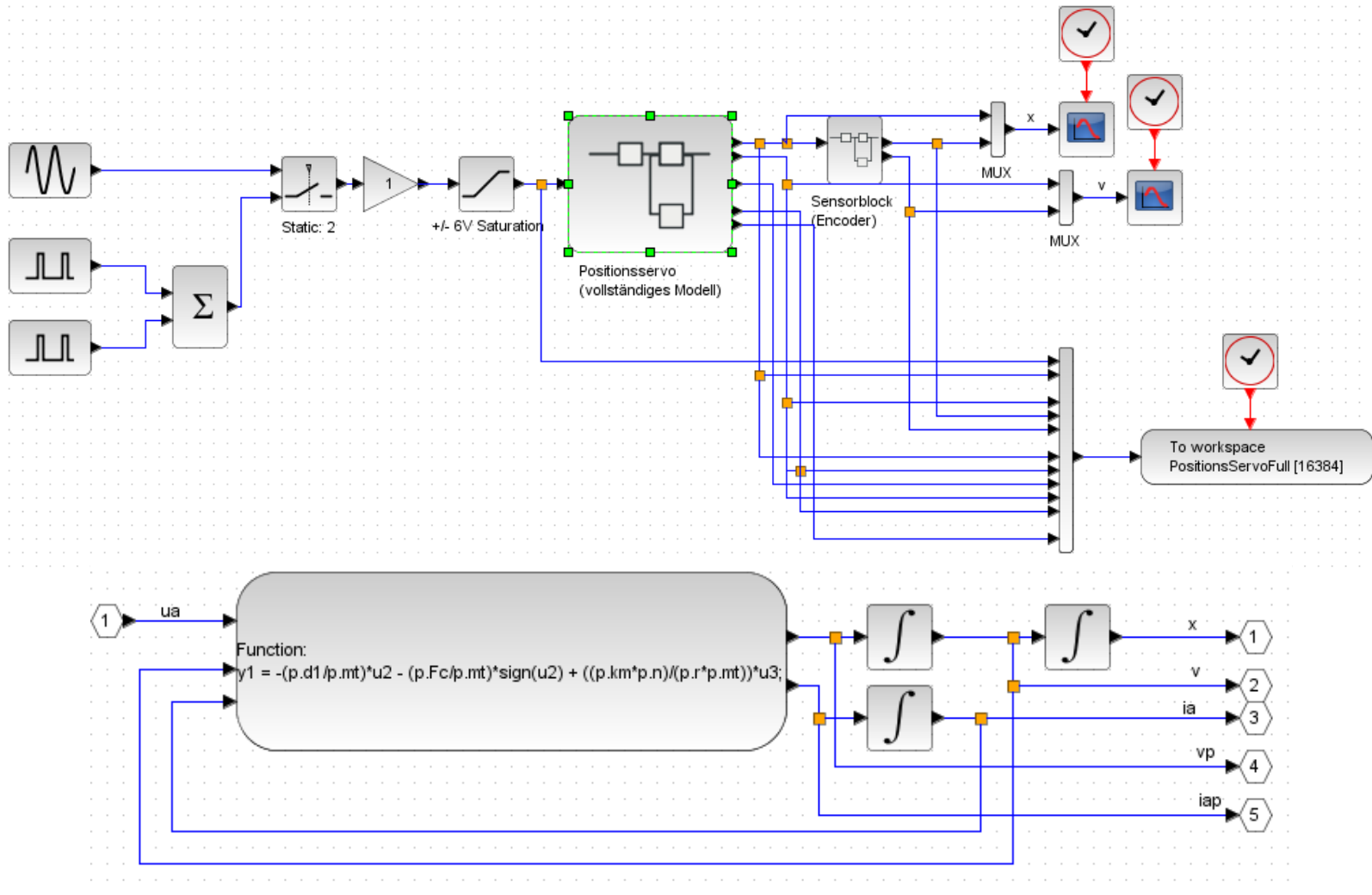




# Measurements

Time	Input ua	x	v
1.808	0	1.38E-06	-4.60E-05
1.809	0	1.38E-06	-2.63E-05
1.81	0	1.38E-06	-5.23E-05
1.811	0	1.37E-06	2.10E-05
1.812	0	1.38E-06	-4.22E-05
1.813	0	1.37E-06	-2.54E-05
1.814	0	1.35E-06	4.60E-05
1.815	0	1.36E-06	2.63E-05
1.816	0	1.36E-06	5.23E-05
1.817	0	1.37E-06	-2.10E-05
1.818	0	1.36E-06	4.22E-05
1.819	0	1.37E-06	2.54E-05
1.82	0	1.38E-06	-4.60E-05

# Simulation in Scilab

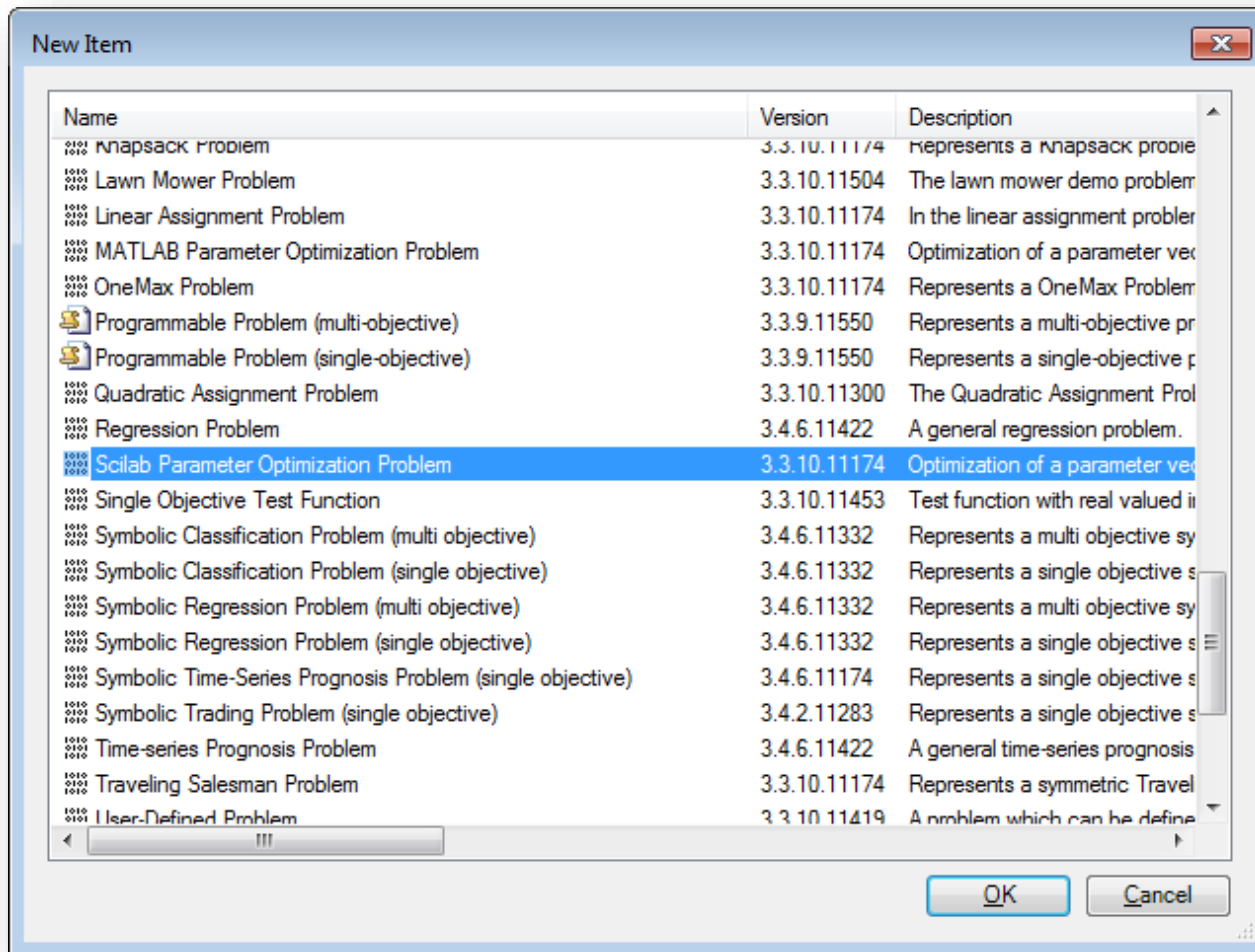


# Parameter Optimization



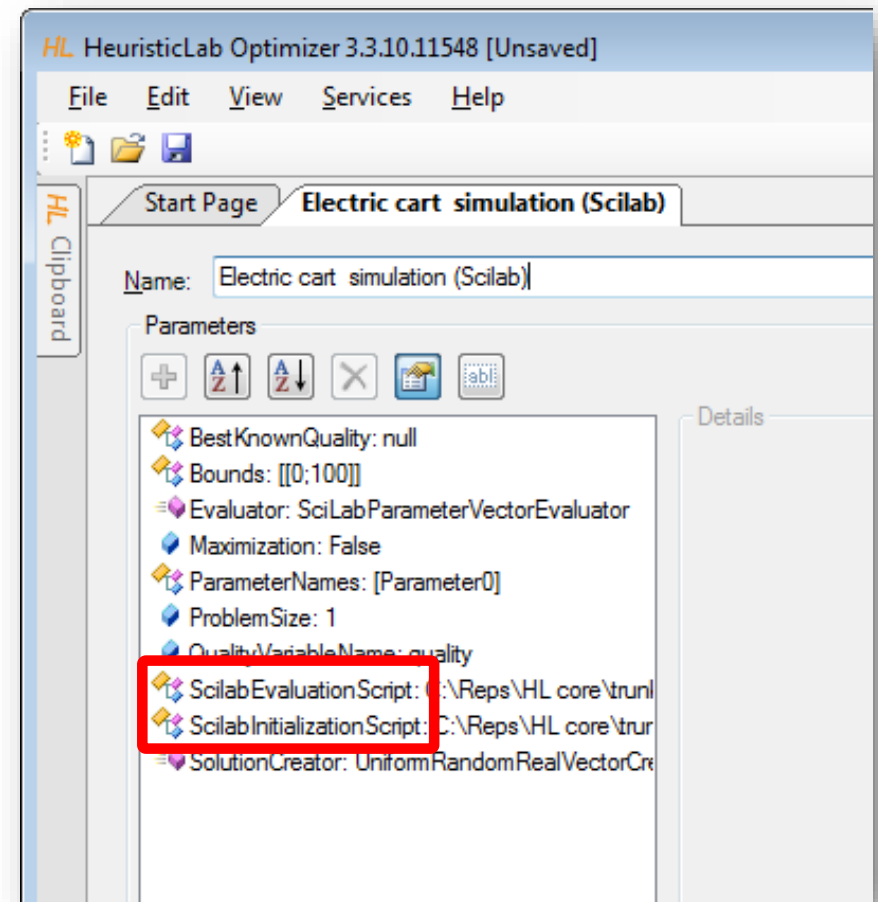
- Create a new Scilab parameter optimization problem in HeuristicLab
- Configure the problem with your scripts in HeuristicLab
- Optimize

# Parameter Optimization



# Parameter Optimization

- Specify path to Scilab scripts
- Initialization script
- Evaluation script



# Initialization Script

- Sets constants and time intervals
- Loads the simulation model
- Reads the measured values from a csv file

```
cd "C:\Reps\HL core\trunk\documentation\Tutorials\Scilab Files"

T = 0.01;
Ts = 5;

// parameters of the dc-motor and the gear
p.Ra = 1.63; // terminal resistance
p.La = 270e-6; // terminal inductance
p.km = 37.7e-3; // torque constant
p.n = 1; // gear transmission ratio
p.r = 6e-3; // radian of the pinion
p.Ja = 41e-7; // moment of inertia (power train)

[result]=importXcosDiagram('SimulatePositionsServoReduced_NoScope.zcos')
original = servo.values(:,2); //2...x, 3...v, 4...x_encoder, 5...v_encoder
data = csvRead('PositionsServoReduced.csv', ',', '.', 'double', [], [], [], 1);
original = data(:,3);
```

# Evaluation Script

- Configures and runs the simulation with values from HeuristicLab
- Calculates quality as sum of absolute errors between simulated and measured values

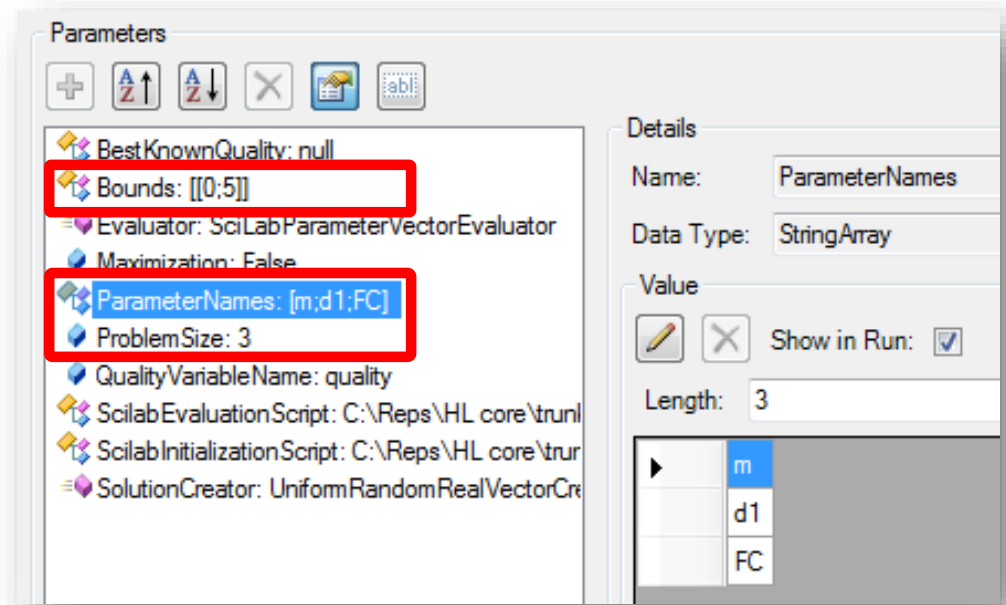
```
// parameters of the cart
p.m = m; // mass of the cart
p.d1 = d1; // viscous friction coefficient
p.Fc = FC; // Coulomb friction force

// equivalent parameters for the model
p.mr = p.Ja*(p.n/p.r)^2; // equivalent mass to moment of inertia
p.mt = p.m + p.mr; // equivalent mass (total)
p.del = (p.n/p.r*p.km)^2/p.Ra; // linear damping from motor
p.dt = p.d1 + p.del; // linear damping coefficient
p.beta = p.n*p.km/p.r/p.Ra; // input transformation

xcos_simulate(scs_m,4);
values = servo.values(:,2); //2...x, 3...v, 4...x_encoder, 5...v_encoder
quality = sum(abs(values - original));
disp(quality);
```

# Parameter Optimization

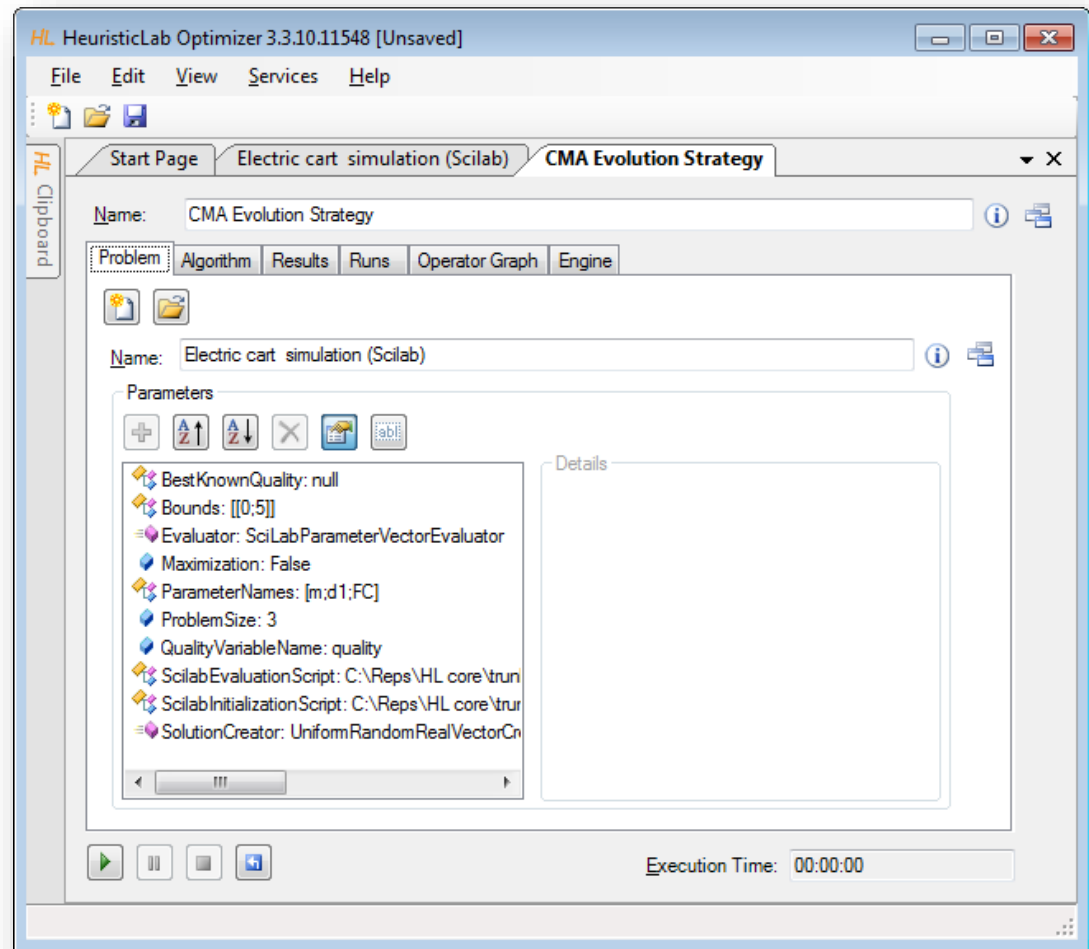
- Configure problem size
- Configure parameter names
- Parameter names are created as variables in Scilab
- Adapt bounds





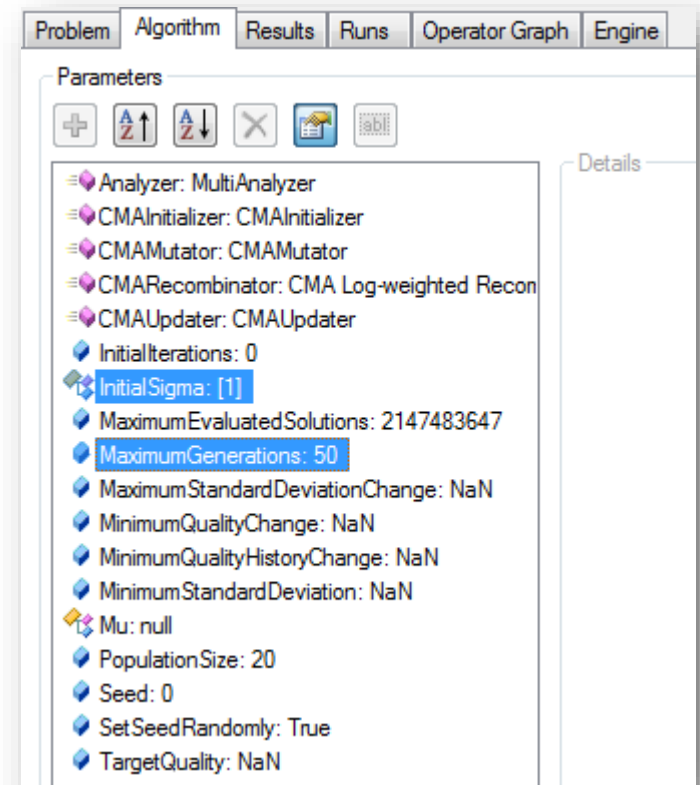
# Parameter Optimization

- Create CMA-ES
- Drop problem on algorithm



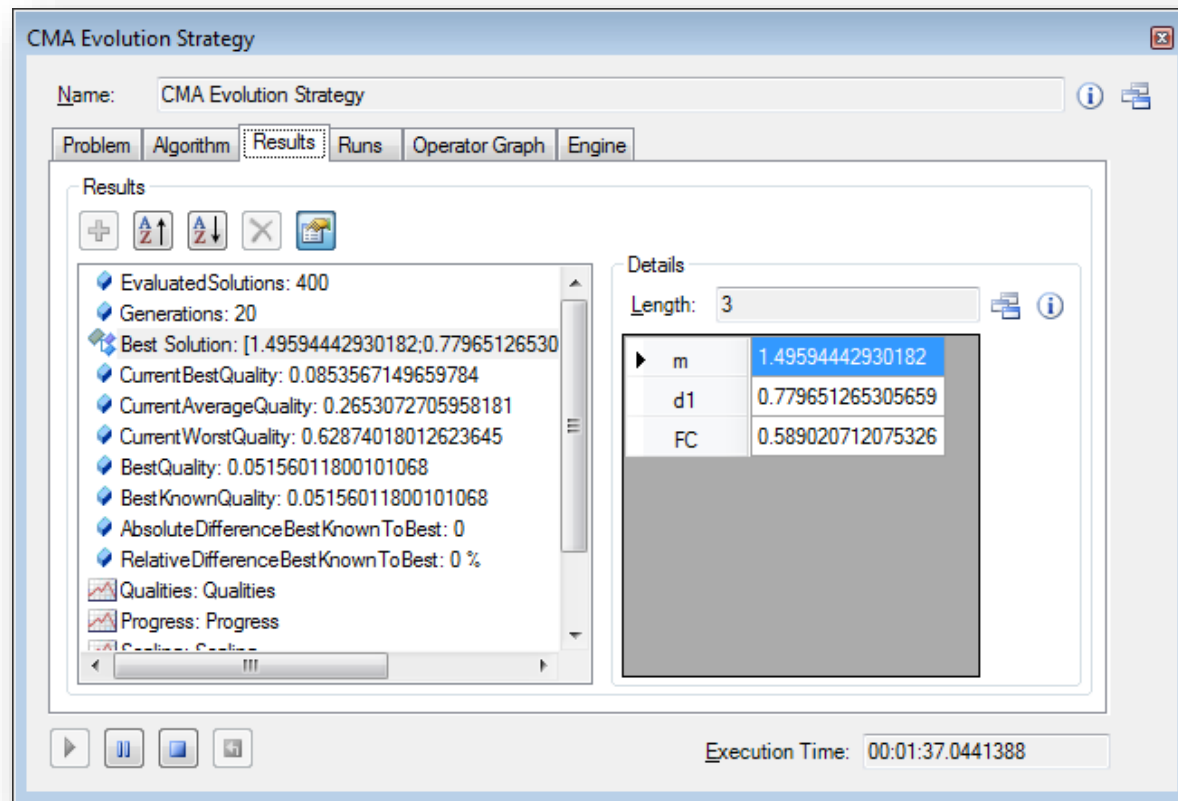
# Parameter Optimization

- Configure algorithm
  - Initial Sigma 1.0
  - Maximum Generations 50
- Enable CMAAnalyzer



# Parameter Optimization

- Optimal values ( $m = 1.5$ ,  $d1 = 1$ ,  $FC = 0.5$ )

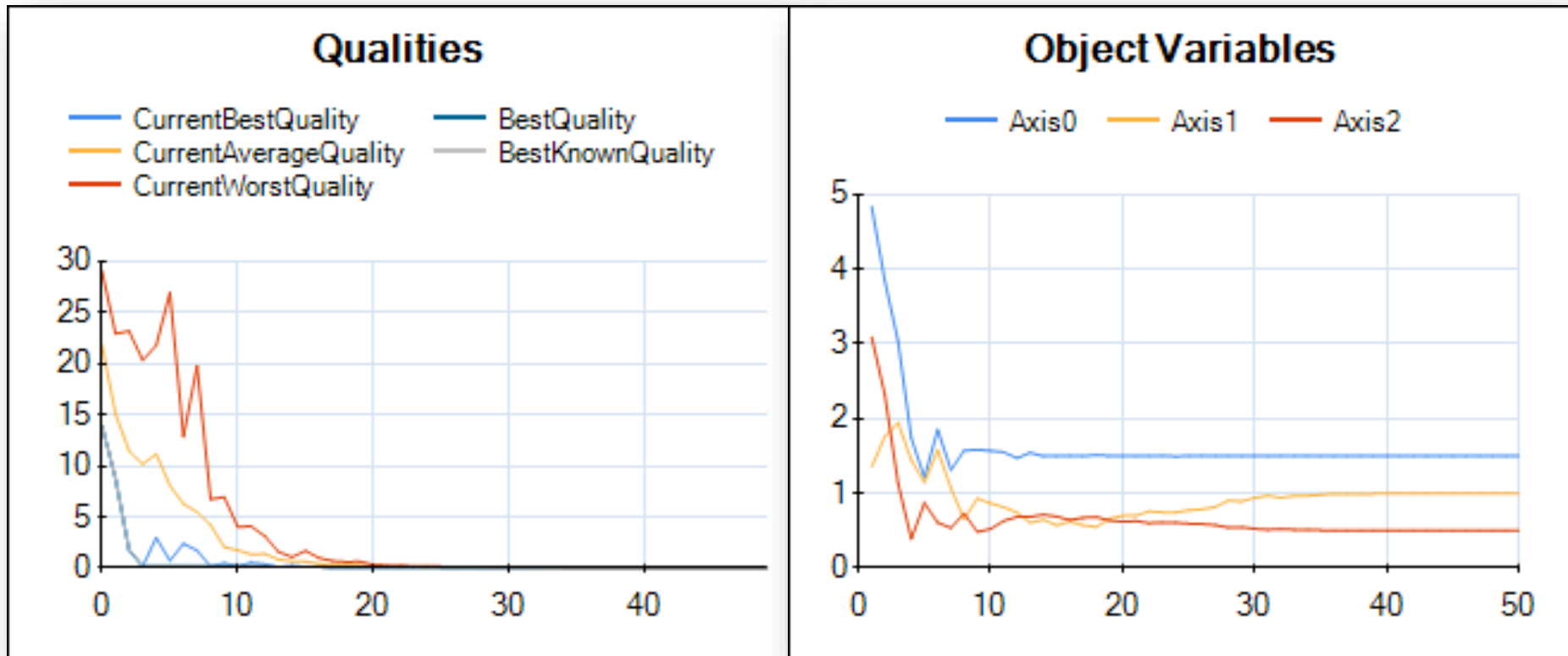


The screenshot displays the 'CMA Evolution Strategy' window. The 'Results' tab is active, showing a list of statistics and a 'Details' table. The 'Details' table lists the optimized parameters: m, d1, and FC.

Parameter	Value
m	1.49594442930182
d1	0.779651265305659
FC	0.589020712075326

Additional statistics shown in the Results pane include: Evaluated Solutions: 400, Generations: 20, Best Solution: [1.49594442930182; 0.779651265305659], Current Best Quality: 0.0853567149659784, Current Average Quality: 0.2653072705958181, Current Worst Quality: 0.62874018012623645, Best Quality: 0.05156011800101068, Best Known Quality: 0.05156011800101068, Absolute Difference Best Known To Best: 0, and Relative Difference Best Known To Best: 0%. The execution time is 00:01:37.0441388.

# Parameter Optimization



# Agenda

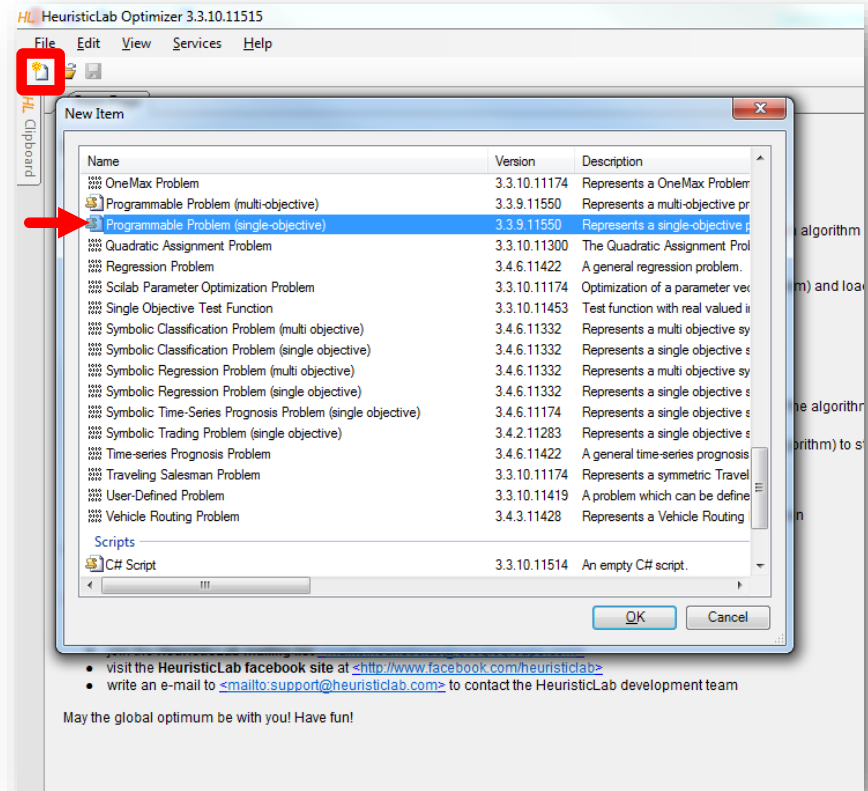
- Objectives of the Tutorial
- Introduction
- Where to get HeuristicLab?
- Plugin Infrastructure
- Graphical User Interface
- Available Algorithms & Problems
  
- **Demonstration Part I: External Evaluation Problem**
- **Demonstration Part II: MATLAB and Scilab Parameter Optimization Problem**
- **Demonstration Part III: Programmable Problem**
  
- Some Additional Features
- Planned Features
- Team
- Suggested Readings
- Bibliography
- Questions & Answers

# Demonstration Part III: Programmable Problem

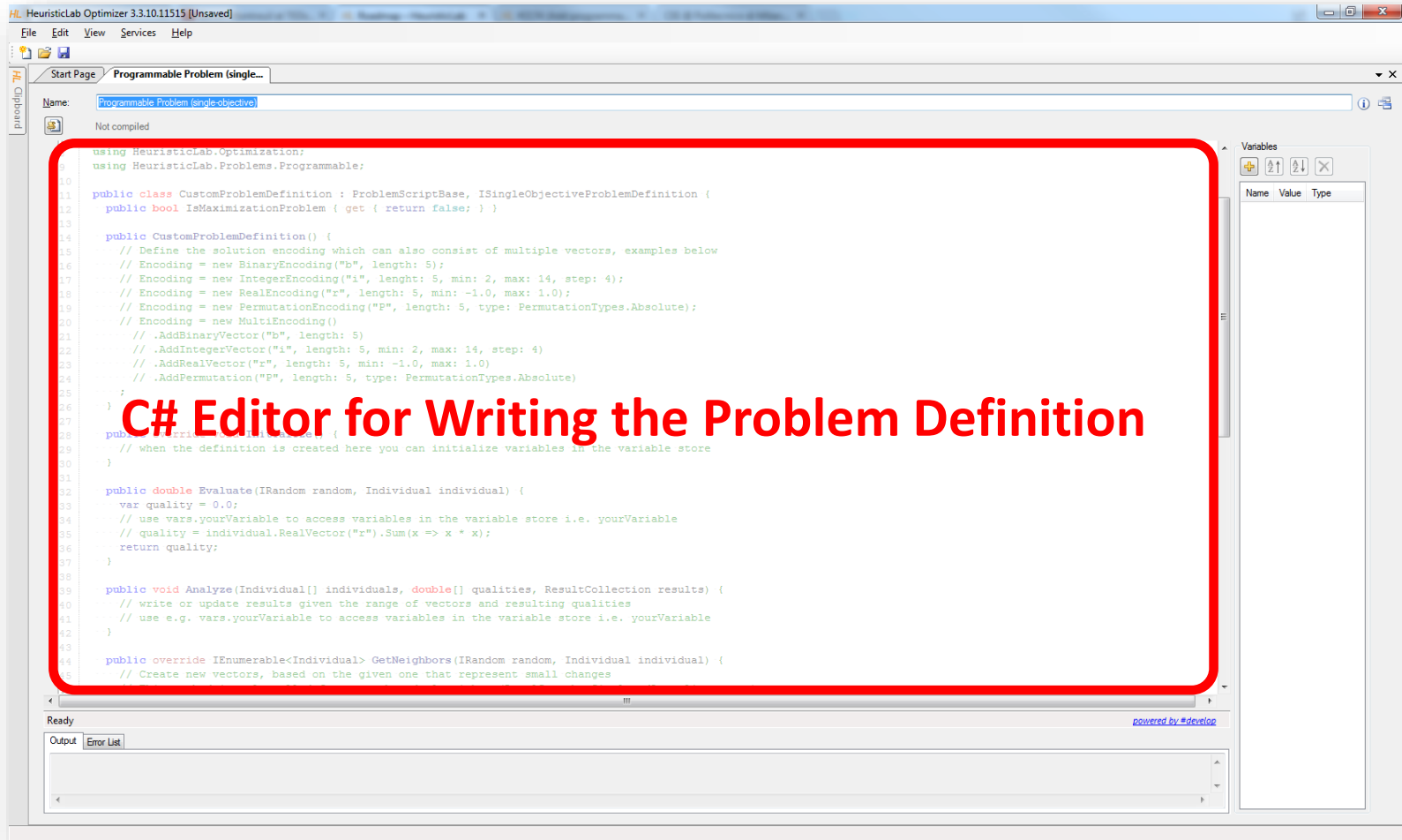
- Singleobjective Function Optimization
  - Solving the Styblinski-Tang function
- Multiobjective Function Optimization
  - Solving the Fonseca and Fleming function
- Non-linear Curve Fitting
  - Fitting a 2 dimensional Gaussian distribution to noisy data

# Singleobjective Function Opt.

- Click on „New Item“ to get a list of creatables
- Create a new Programmable Problem (single-objective) by double clicking it



# Singleobjective Function Opt.



```
using HeuristicLab.Optimization;
using HeuristicLab.Problems.Programmable;

public class CustomProblemDefinition : ProblemScriptBase, ISingleObjectiveProblemDefinition {
    public bool IsMaximizationProblem { get { return false; } }

    public CustomProblemDefinition() {
        // Define the solution encoding which can also consist of multiple vectors, examples below
        // Encoding = new BinaryEncoding("b", length: 5);
        // Encoding = new IntegerEncoding("i", length: 5, min: 2, max: 14, step: 4);
        // Encoding = new RealEncoding("r", length: 5, min: -1.0, max: 1.0);
        // Encoding = new PermutationEncoding("p", length: 5, type: PermutationTypes.Absolute);
        // Encoding = new MultiEncoding()
        //     .AddBinaryVector("b", length: 5)
        //     .AddIntegerVector("i", length: 5, min: 2, max: 14, step: 4)
        //     .AddRealVector("r", length: 5, min: -1.0, max: 1.0)
        //     .AddPermutation("p", length: 5, type: PermutationTypes.Absolute)
    }

    public double Evaluate(IRandom random, Individual individual) {
        var quality = 0.0;
        // use vars.yourVariable to access variables in the variable store i.e. yourVariable
        // quality = individual.RealVector("r").Sum(x => x * x);
        return quality;
    }

    public void Analyze(Individual[] individuals, double[] qualities, ResultCollection results) {
        // write or update results given the range of vectors and resulting qualities
        // use e.g. vars.yourVariable to access variables in the variable store i.e. yourVariable
    }

    public override IEnumerable<Individual> GetNeighbors(IRandom random, Individual individual) {
        // Create new vectors, based on the given one that represent small changes
    }
}
```

**C# Editor for Writing the Problem Definition**

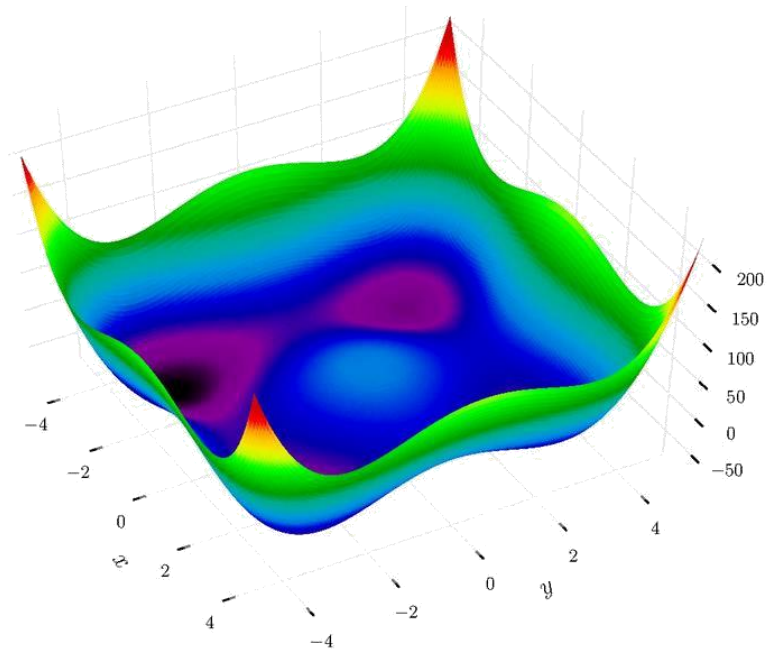


# Singleobjective Function Opt.

- Styblinski-Tang function:

$$f(x) = \frac{\sum_{i=1}^n x_i^4 - 16x_i^2 + 5x_i}{2}$$

with  $-5 \leq x_i \leq 5$



# Singleobjective Function Opt.

- Choose an appropriate solution encoding
  - 20-dimensional real-valued vector
  - Minimize the fitness value

```
public bool Maximization { get { return false; } }
```

```
public override void Initialize() {  
    // Define the solution encoding which can also consist of multiple vectors, examples below  
    // Encoding = new BinaryEncoding("b", length: 5);  
    // Encoding = new IntegerEncoding("i", length: 5, min: 2, max: 14, step: 4);  
    Encoding = new RealEncoding("vector", length: 20, min: -5.0, max: 5.0);  
    // Encoding = new PermutationEncoding("P", length: 5, type: PermutationTypes.Absolute);  
    // Encoding = new MultiEncoding()  
        // .AddBinaryVector("b", length: 5)  
        // .AddIntegerVector("i", length: 5, min: 2, max: 14, step: 4)  
        // .AddRealVector("r", length: 5, min: -1.0, max: 1.0)  
        // .AddPermutation("P", length: 5, type: PermutationTypes.Absolute)  
    ;  
}
```

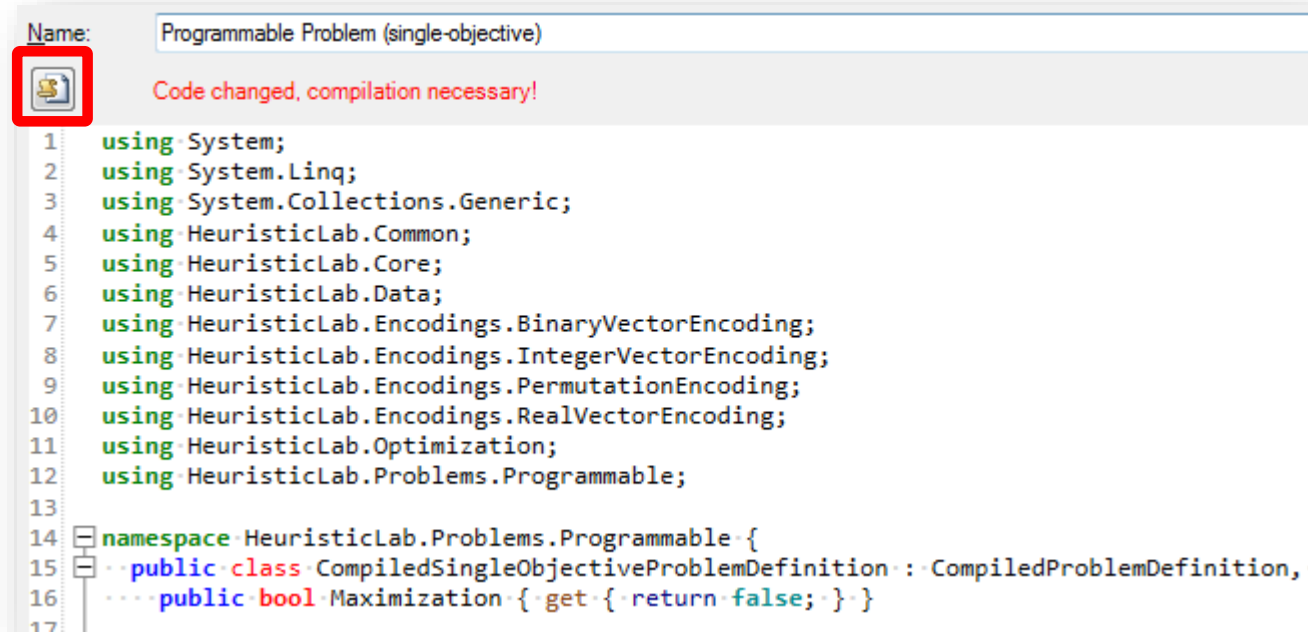
# Singleobjective Function Opt.

- Define the fitness function

```
public double Evaluate(Individual individual, IRandom random) {  
    var vector = individual.RealVector("vector");  
    return vector.Sum(x => x * x * x * x - 16.0 * x * x + 5 * x) / 2.0;  
}
```

# Singleobjective Function Opt.

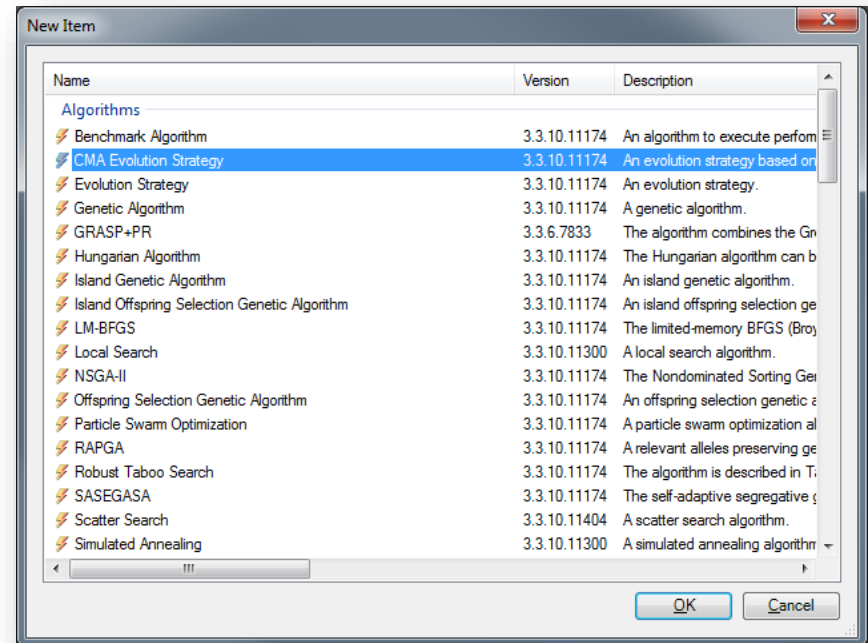
- Compile the problem definition



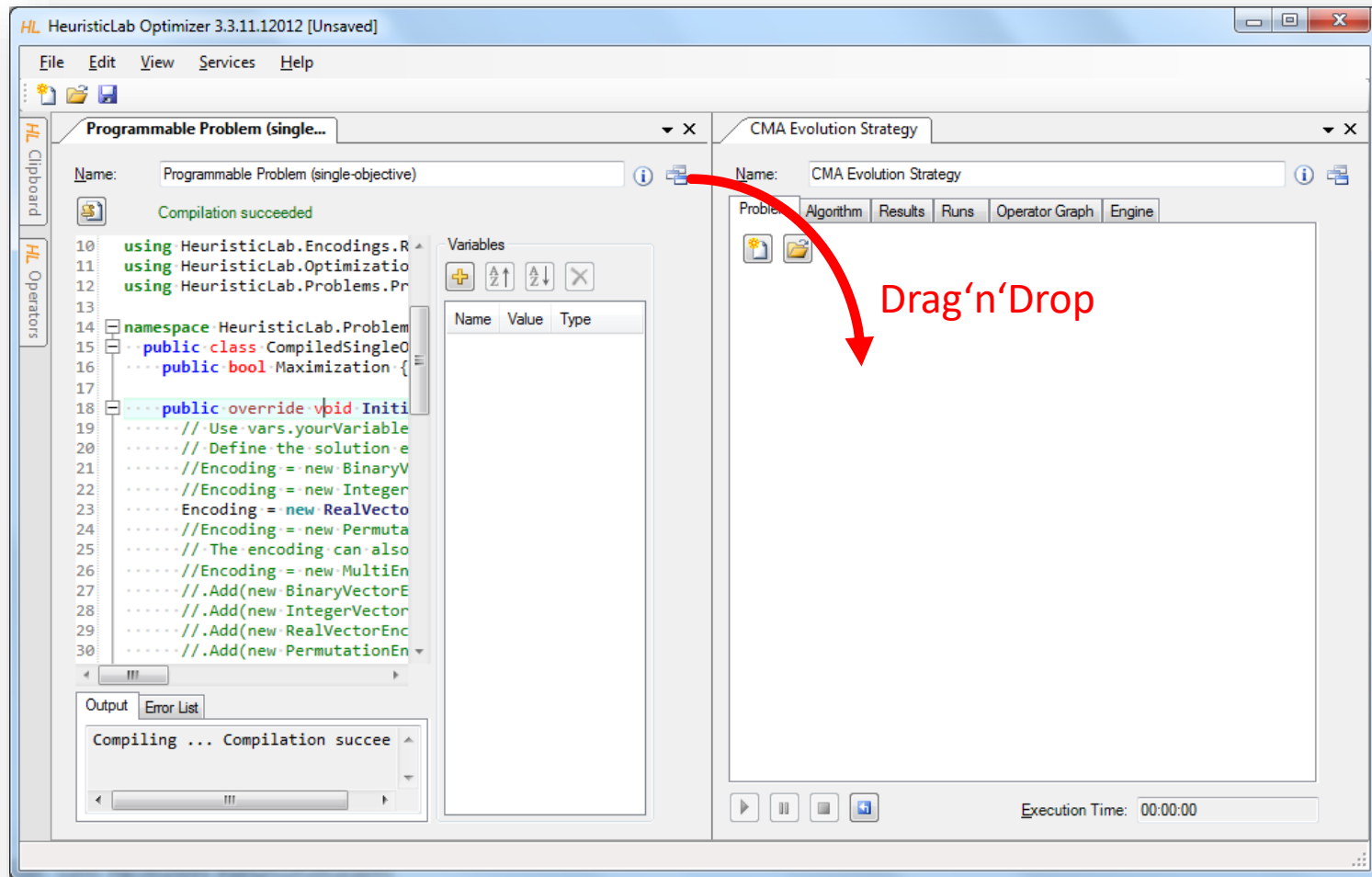
```
Name: Programmable Problem (single-objective)
Code changed, compilation necessary!
1 using System;
2 using System.Linq;
3 using System.Collections.Generic;
4 using HeuristicLab.Common;
5 using HeuristicLab.Core;
6 using HeuristicLab.Data;
7 using HeuristicLab.Encodings.BinaryVectorEncoding;
8 using HeuristicLab.Encodings.IntegerVectorEncoding;
9 using HeuristicLab.Encodings.PermutationEncoding;
10 using HeuristicLab.Encodings.RealVectorEncoding;
11 using HeuristicLab.Optimization;
12 using HeuristicLab.Problems.Programmable;
13
14 namespace HeuristicLab.Problems.Programmable {
15     public class CompiledSingleObjectiveProblemDefinition : CompiledProblemDefinition,
16         public bool Maximization { get { return false; } }
17 }
```

# Singleobjective Function Opt.

- Create a suitable optimization algorithm
- Select CMA Evolution Strategy
- Click OK

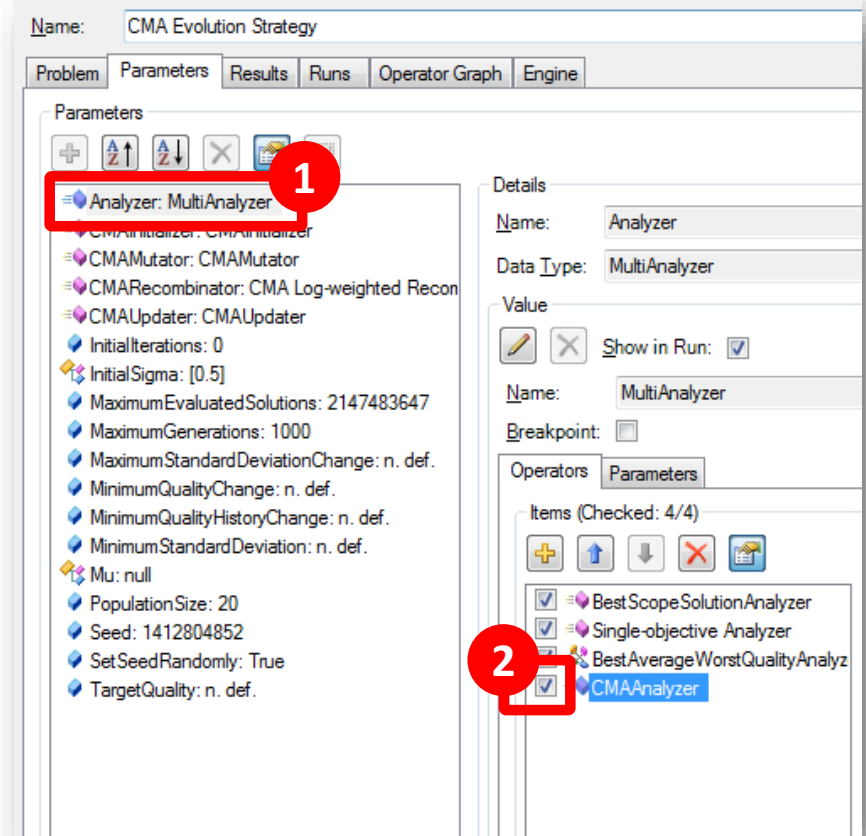


# Singleobjective Function Opt.



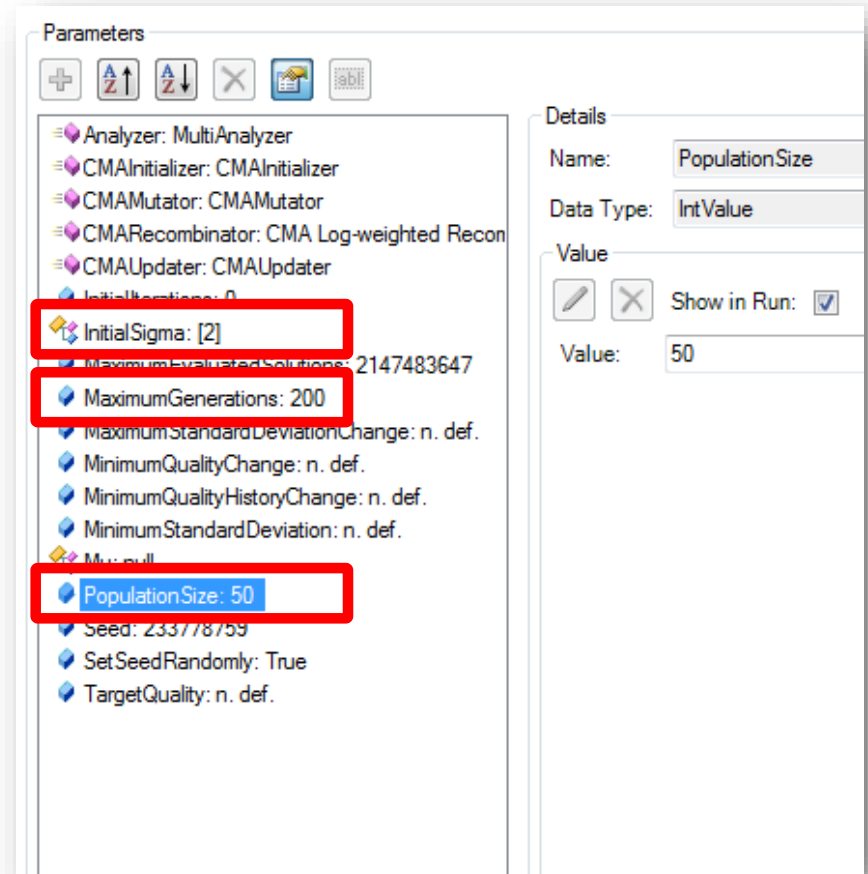
# Singleobjective Function Opt.

- Switch to the Parameters tab
- Click on the Analyzer parameter
- Check CMAAnalyzer to get more detailed results



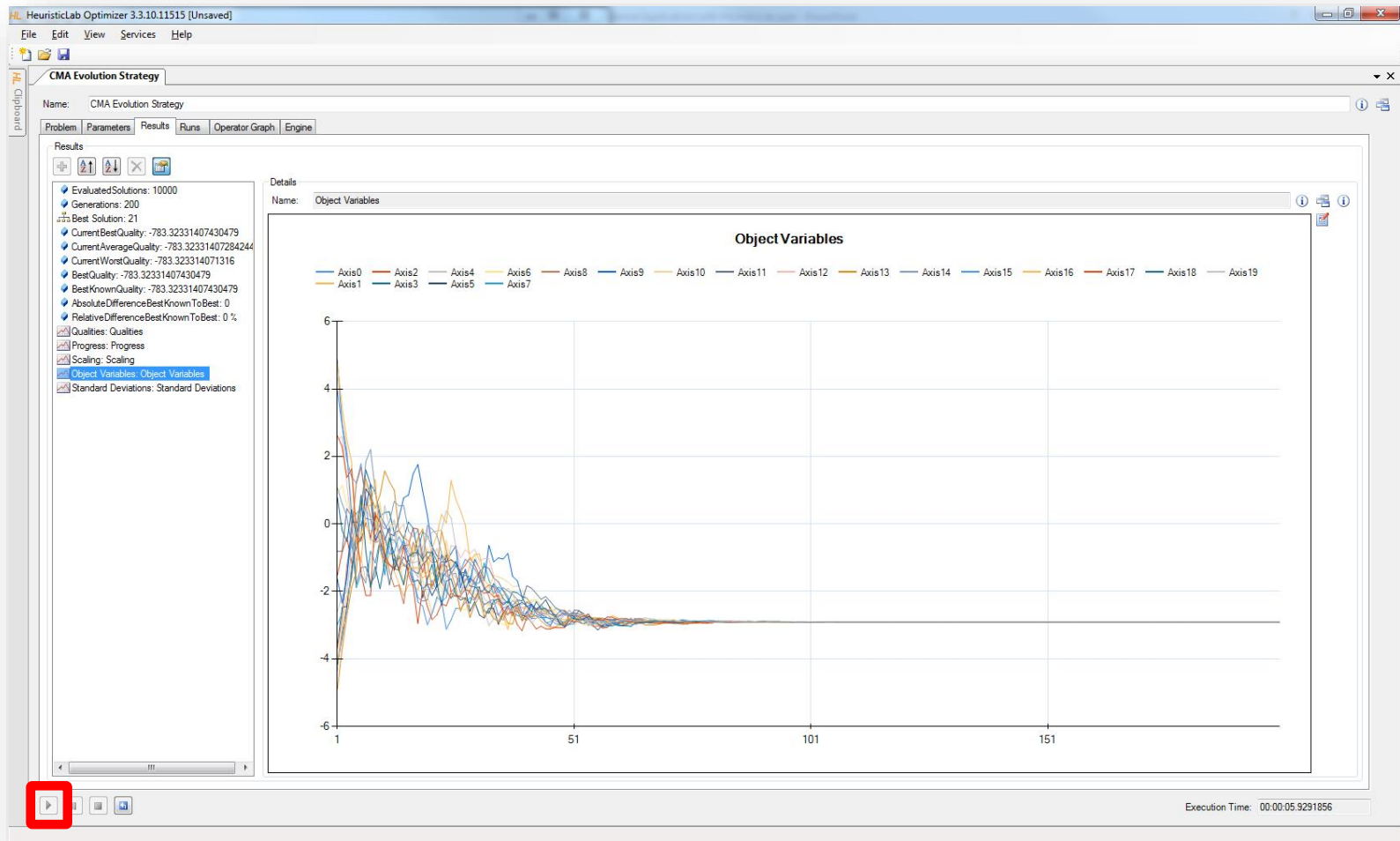
# Singleobjective Function Opt.

- Choose suitable parameters
  - InitialSigma: 2
  - MaximumGenerations: 200
  - PopulationSize: 50





# Singleobjective Function Opt.

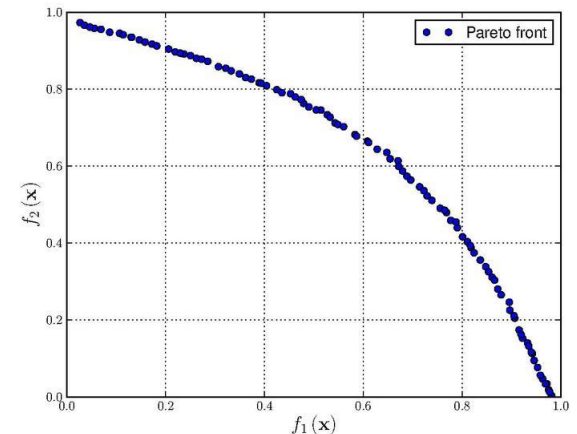


# Multiobjective Function Opt.

- Fonseca and Fleming function:

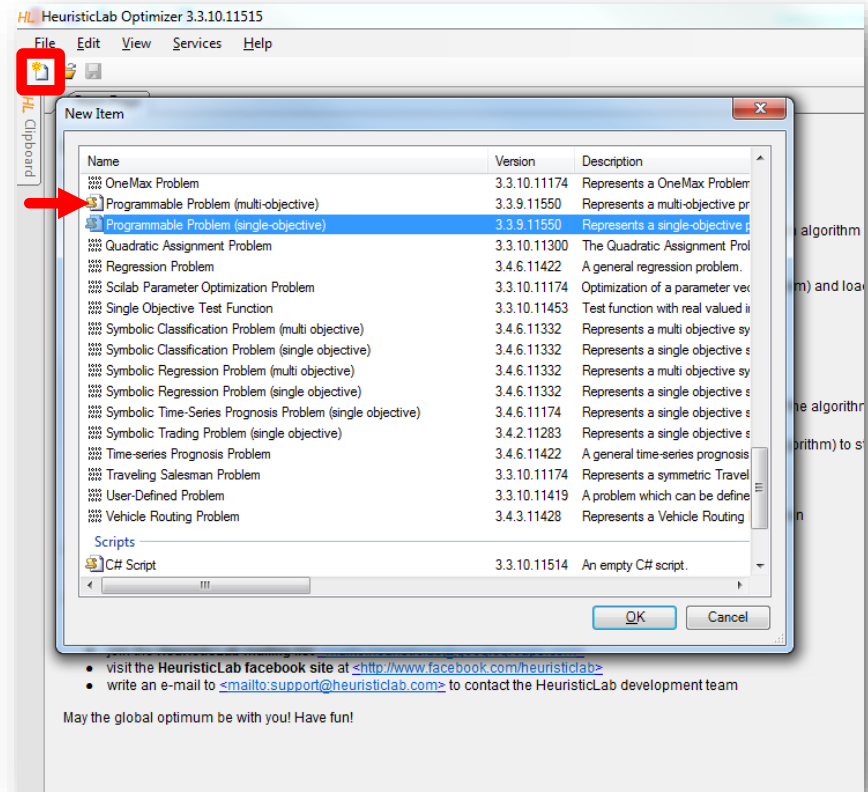
$$\text{Minimize} = \begin{cases} f_1(x) = 1 - e^{-\sum_{i=1}^n (x_i - \frac{1}{\sqrt{n}})^2} \\ f_2(x) = 1 - e^{-\sum_{i=1}^n (x_i + \frac{1}{\sqrt{n}})^2} \end{cases}$$

with  $-4 \leq x \leq 4$



# Multiobjective Function Opt.

- Click on „New Item“ to get a list of creatables
- Create a new Programmable Problem (multi-objective) by double clicking it



# Multiobjective Function Opt.

- Choose an appropriate solution encoding
  - 10-dimensional real-valued vector
  - Minimize all fitness values

```
public bool[] Maximization { get { return new [] { false, false }; } }

public override void Initialize() {
    // Define the solution encoding which can also consist of multiple vectors, examples below
    // Encoding = new BinaryEncoding("b", length: 5);
    // Encoding = new IntegerEncoding("i", length: 5, min: 2, max: 14, step: 4);
    Encoding = new RealEncoding("vector", length: 10, min: -4.0, max: 4.0);
    // Encoding = new PermutationEncoding("P", length: 5, type: PermutationTypes.Absolute);
    // Encoding = new MultiEncoding()
    //     .AddBinaryVector("b", length: 5)
    //     .AddIntegerVector("i", length: 5, min: 2, max: 14, step: 4)
    //     .AddRealVector("r", length: 5, min: -1.0, max: 1.0)
    //     .AddPermutation("P", length: 5, type: PermutationTypes.Absolute)
    ;
}
```

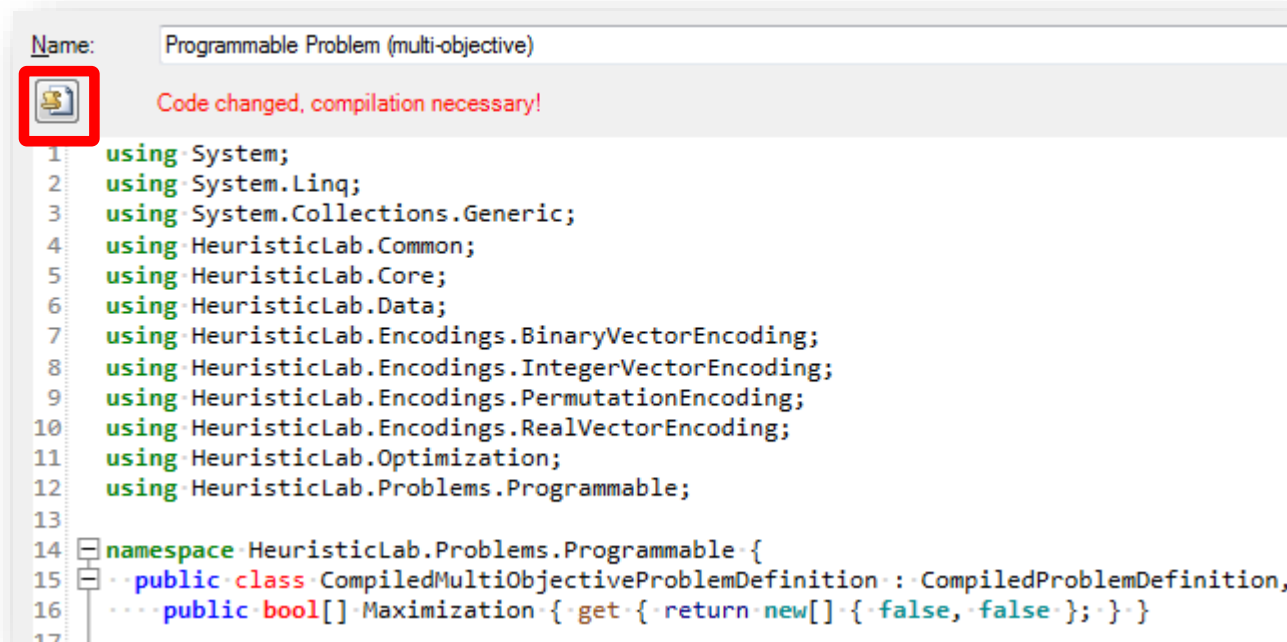
# Multiobjective Function Opt.

- Define the fitness functions

```
public double[] Evaluate(Individual individual, IRandom random) {  
    var qualities = new double[2];  
    var vector = individual.RealVector("vector");  
    var n = vector.Length;  
    qualities[0] = 1.0 - Math.Exp(- vector.Sum(x => Math.Pow(x - 1.0/Math.Sqrt(n), 2)));  
    qualities[1] = 1.0 - Math.Exp(- vector.Sum(x => Math.Pow(x + 1.0/Math.Sqrt(n), 2)));  
    return qualities;  
}
```

# Multiobjective Function Opt.

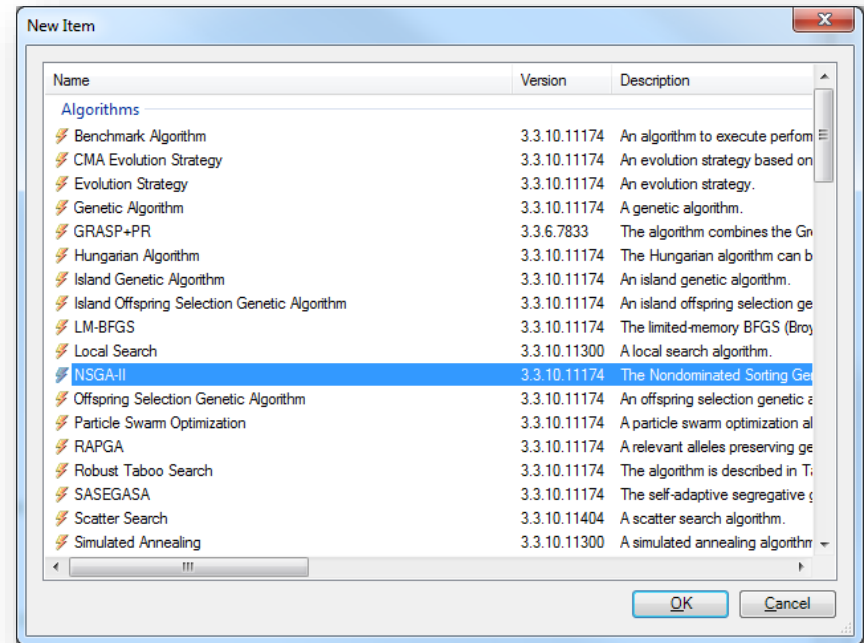
- Compile the problem definition



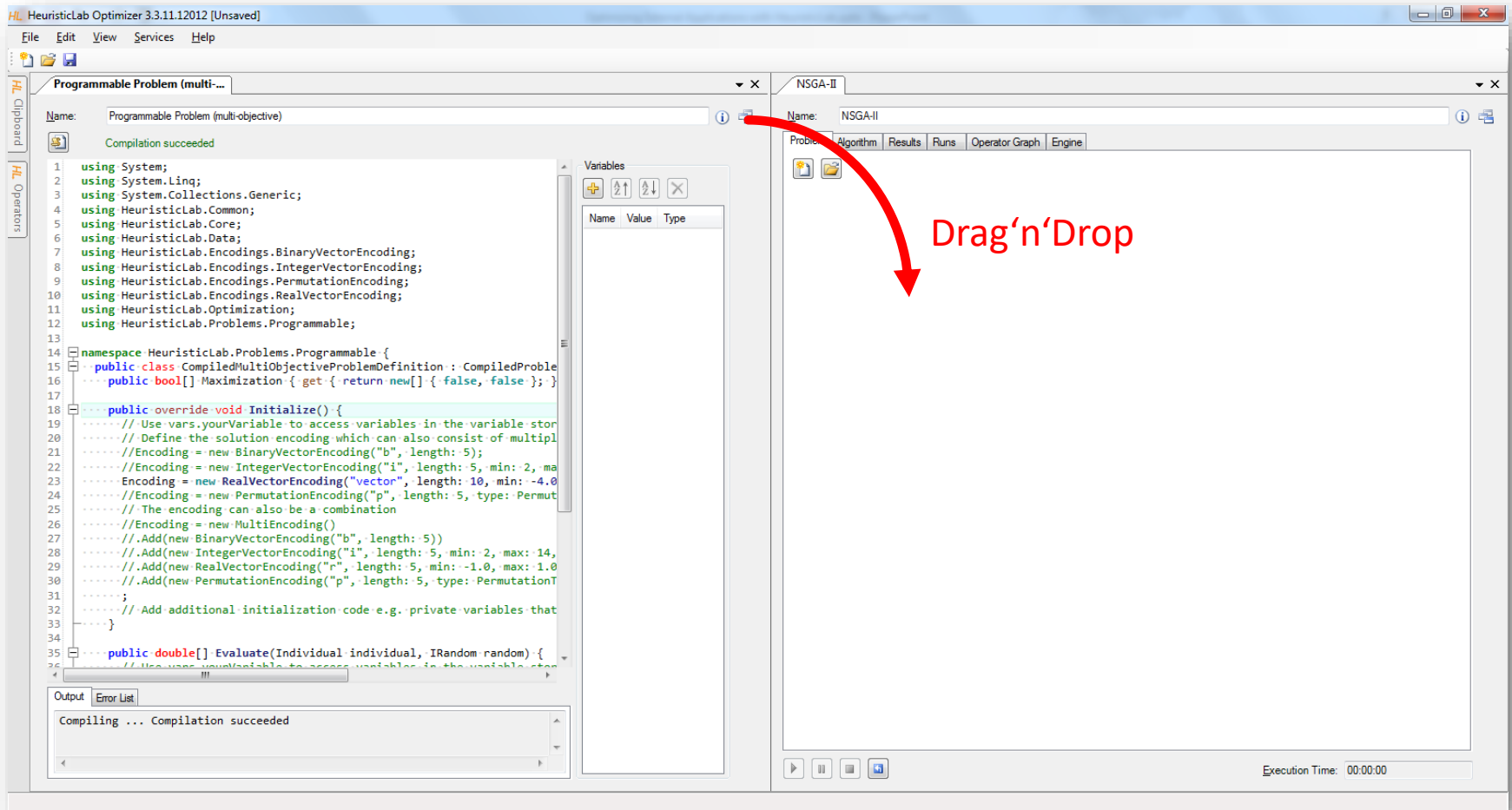
```
Name: Programmable Problem (multi-objective)
Code changed, compilation necessary!
1 using System;
2 using System.Linq;
3 using System.Collections.Generic;
4 using HeuristicLab.Common;
5 using HeuristicLab.Core;
6 using HeuristicLab.Data;
7 using HeuristicLab.Encodings.BinaryVectorEncoding;
8 using HeuristicLab.Encodings.IntegerVectorEncoding;
9 using HeuristicLab.Encodings.PermutationEncoding;
10 using HeuristicLab.Encodings.RealVectorEncoding;
11 using HeuristicLab.Optimization;
12 using HeuristicLab.Problems.Programmable;
13
14 namespace HeuristicLab.Problems.Programmable {
15     public class CompiledMultiObjectiveProblemDefinition : CompiledProblemDefinition,
16         public bool[] Maximization { get { return new[] { false, false }; } }
17 }
```

# Multiobjective Function Opt.

- Create a suitable optimization algorithm
- Select NSGA-II
- Click OK



# Multiobjective Function Opt.



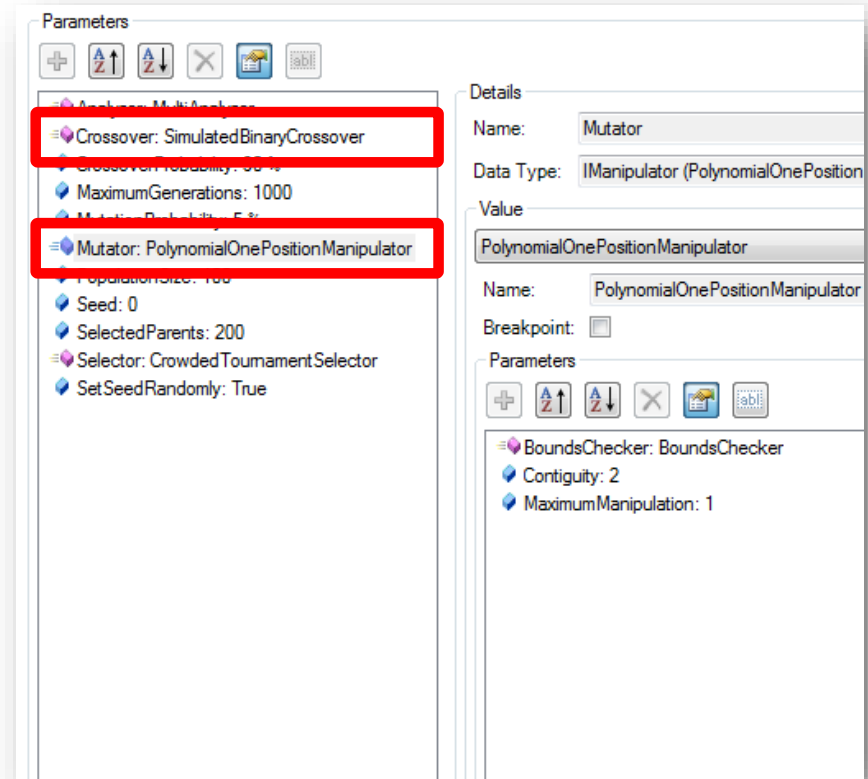
The screenshot displays the HeuristicLab Optimizer interface. On the left, a code editor shows the definition of a multi-objective problem. The code includes various HeuristicLab namespaces and defines a `CompiledMultiObjectiveProblemDefinition` class with an `Initialize()` method that sets up encodings for binary, integer, real, and permutation variables. The right pane shows the NSGA-II algorithm configuration. A red arrow points from the NSGA-II configuration area to the code editor, with the text "Drag'n'Drop" next to it, indicating that the algorithm can be dragged into the problem configuration.

```
1 using System;
2 using System.Linq;
3 using System.Collections.Generic;
4 using HeuristicLab.Common;
5 using HeuristicLab.Core;
6 using HeuristicLab.Data;
7 using HeuristicLab.Encodings.BinaryVectorEncoding;
8 using HeuristicLab.Encodings.IntegerVectorEncoding;
9 using HeuristicLab.Encodings.PermutationEncoding;
10 using HeuristicLab.Encodings.RealVectorEncoding;
11 using HeuristicLab.Optimization;
12 using HeuristicLab.Problems.Programmable;
13
14 namespace HeuristicLab.Problems.Programmable {
15     public class CompiledMultiObjectiveProblemDefinition : CompiledProblemDefinition {
16         public bool[] Maximization { get { return new[] { false, false }; } }
17
18         public override void Initialize() {
19             // Use vars.yourVariable to access variables in the variable store
20             // Define the solution encoding which can also consist of multiple encodings
21             //Encoding = new BinaryVectorEncoding("b", length: 5);
22             //Encoding = new IntegerVectorEncoding("i", length: 5, min: -2, max: 14);
23             //Encoding = new RealVectorEncoding("vector", length: 10, min: -4.0, max: 1.0);
24             //Encoding = new PermutationEncoding("p", length: 5, type: PermutationType.Random);
25             // The encoding can also be a combination of multiple encodings
26             //Encoding = new MultiEncoding();
27             //Add(new BinaryVectorEncoding("b", length: 5));
28             //Add(new IntegerVectorEncoding("i", length: 5, min: -2, max: 14));
29             //Add(new RealVectorEncoding("r", length: 5, min: -1.0, max: 1.0));
30             //Add(new PermutationEncoding("p", length: 5, type: PermutationType.Random));
31             // Add additional initialization code e.g. private variables that are used in the Evaluate method
32         }
33     }
34
35     public double[] Evaluate(Individual individual, IRandom random) {
36         // Use vars.yourVariable to access variables in the variable store
37     }
38 }
```

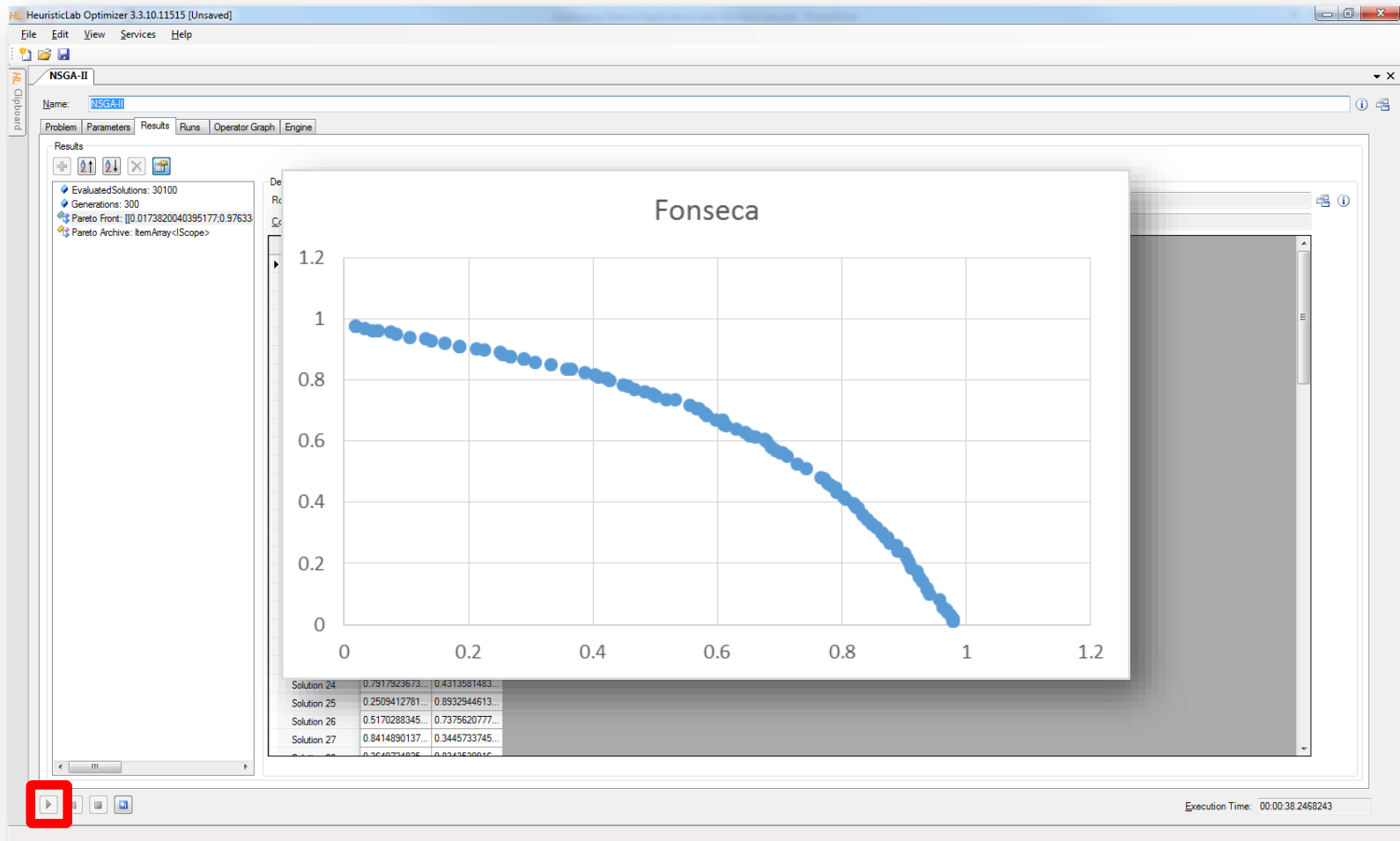


# Multiobjective Function Opt.

- Adjust the parameters
- Set Crossover: SBX
- Set Mutator: Polynomial

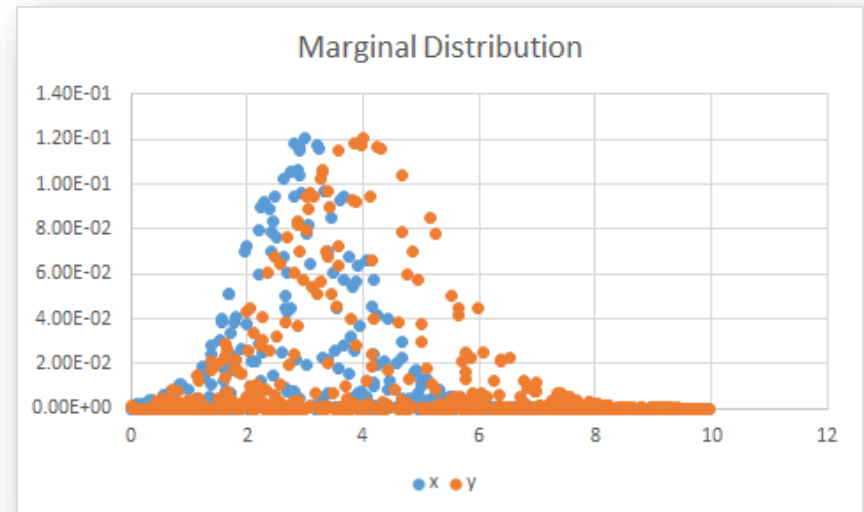


# Multiobjective Function Opt.



# Non-linear Curve Fitting

- In this example: Fitting a 2 dimensional Gaussian distribution to noisy data
- We will create a random dataset as instance
- We will then fit the parameters



# Non-linear Curve Fitting

- The probability density function for a  $k$  dimensional Gaussian distribution is given

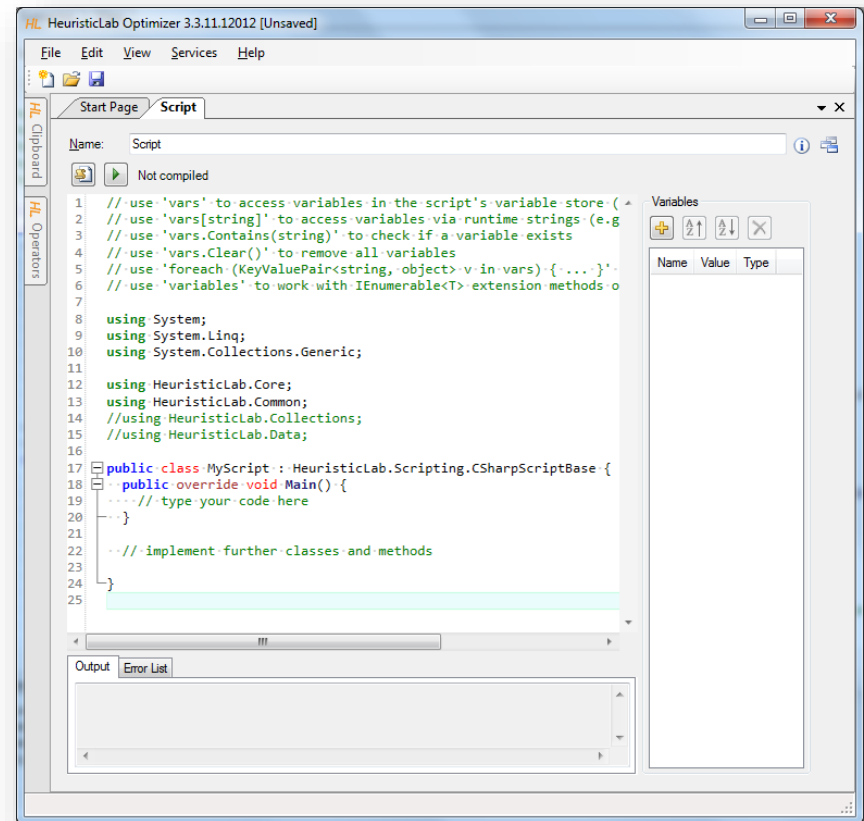
$$f_{\mathbf{x}}(x_1, \dots, x_k) = \frac{1}{\sqrt{(2\pi)^k |\Sigma|}} \exp\left(-\frac{1}{2}(\mathbf{x} - \boldsymbol{\mu})^T \Sigma^{-1}(\mathbf{x} - \boldsymbol{\mu})\right)$$

- For 2 dimensional Gaussian distribution we need to fit a total of 5 parameters
  - $\boldsymbol{\mu}$  (2 dimensions)
  - $\Sigma$  (3 dimensions due to symmetry)

Source: [http://en.wikipedia.org/wiki/Multivariate\\_normal\\_distribution](http://en.wikipedia.org/wiki/Multivariate_normal_distribution)

# Non-linear Curve Fitting

- To generate the dataset, first create a new C# Script
- Then enter the code that generates the data on the next slide



HL HeuristicLab Optimizer 3.3.11.12012 [Unsaved]

```
File Edit View Services Help
Start Page Script
Name: Script
Not compiled
1 // use 'vars' to access variables in the script's variable store (
2 // use 'vars[string]' to access variables via runtime strings (e.g
3 // use 'vars.Contains(string)' to check if a variable exists
4 // use 'vars.Clear()' to remove all variables
5 // use 'foreach (KeyValuePair<string, object> v in vars) {...}'
6 // use 'variables' to work with IEnumerable<T> extension methods o
7
8 using System;
9 using System.Linq;
10 using System.Collections.Generic;
11
12 using HeuristicLab.Core;
13 using HeuristicLab.Common;
14 //using HeuristicLab.Collections;
15 //using HeuristicLab.Data;
16
17 public class MyScript : HeuristicLab.Scripting.CSharpScriptBase {
18     public override void Main() {
19         // type your code here
20     }
21     // implement further classes and methods
22 }
23
24
25
```

Variables

Name	Value	Type
------	-------	------

Output Error List

# Non-linear Curve Fitting

```
public class MyScript : HeuristicLab.Scripting.CSharpScriptBase {
    public override void Main() {
        var cov = new double[,] { { 1, 0.5 }, { 0.5, 2 } };
        var invCov = GetInverse(cov);
        var mu = new double[] { 3, 4 };

        var rand = new MersenneTwister();
        var nd = new NormalDistributedRandom(rand, 0, 0.01);

        var sampleSize = 500;
        var data = new DoubleMatrix(sampleSize, 3);
        for (var i = 0; i < sampleSize; i++) {
            data[i, 0] = rand.NextDouble() * 10;
            data[i, 1] = rand.NextDouble() * 10;
            data[i, 2] = TwoDGauss(data[i, 0], data[i, 1], mu, cov, invCov) + nd.NextDouble();
        }
        vars.data = data;
    }

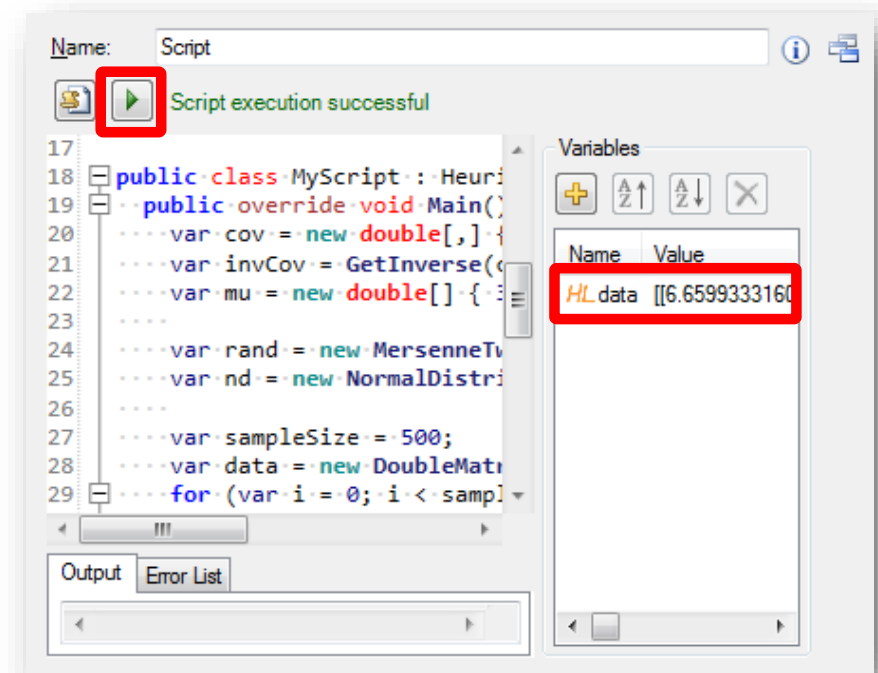
    private double TwoDGauss(double x, double y, double[] mu, double[,] cov, double[,] invCov) {
        var a = x - mu[0];
        var b = y - mu[1];
        return 1.0 / (2.0 * Math.PI * Math.Sqrt(GetDeterminant(cov)))
            * Math.Exp(-0.5 * ((a * invCov[0, 0] + b * invCov[1, 0]) * a + (a * invCov[0, 1] + b * invCov[1, 1]) * b));
    }

    private double[,] GetInverse(double[,] m) {
        var det = GetDeterminant(m);
        return new double[,] { { m[1, 1] / det, -m[0, 1] / det }, { -m[1, 0] / det, m[0, 0] / det } };
    }

    private double GetDeterminant(double[,] m) {
        return m[0, 0] * m[1, 1] - m[0, 1] * m[1, 0];
    }
}
```

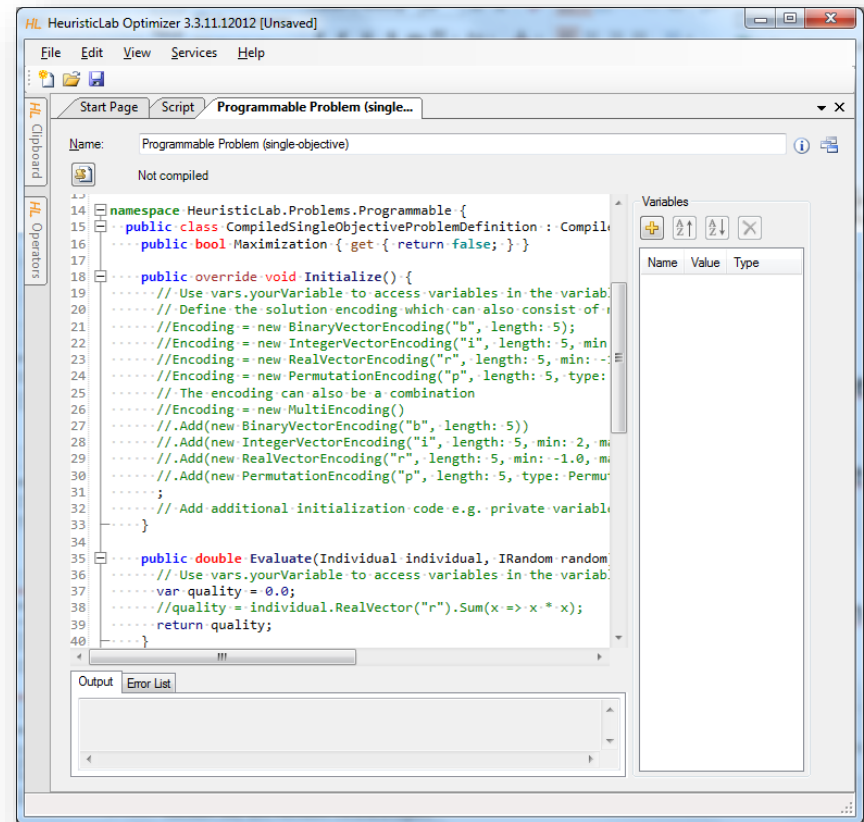
# Non-linear Curve Fitting

- Run the script by clicking the run button or by hitting F5
- The data will be generated as a matrix and appear in the VariableStore



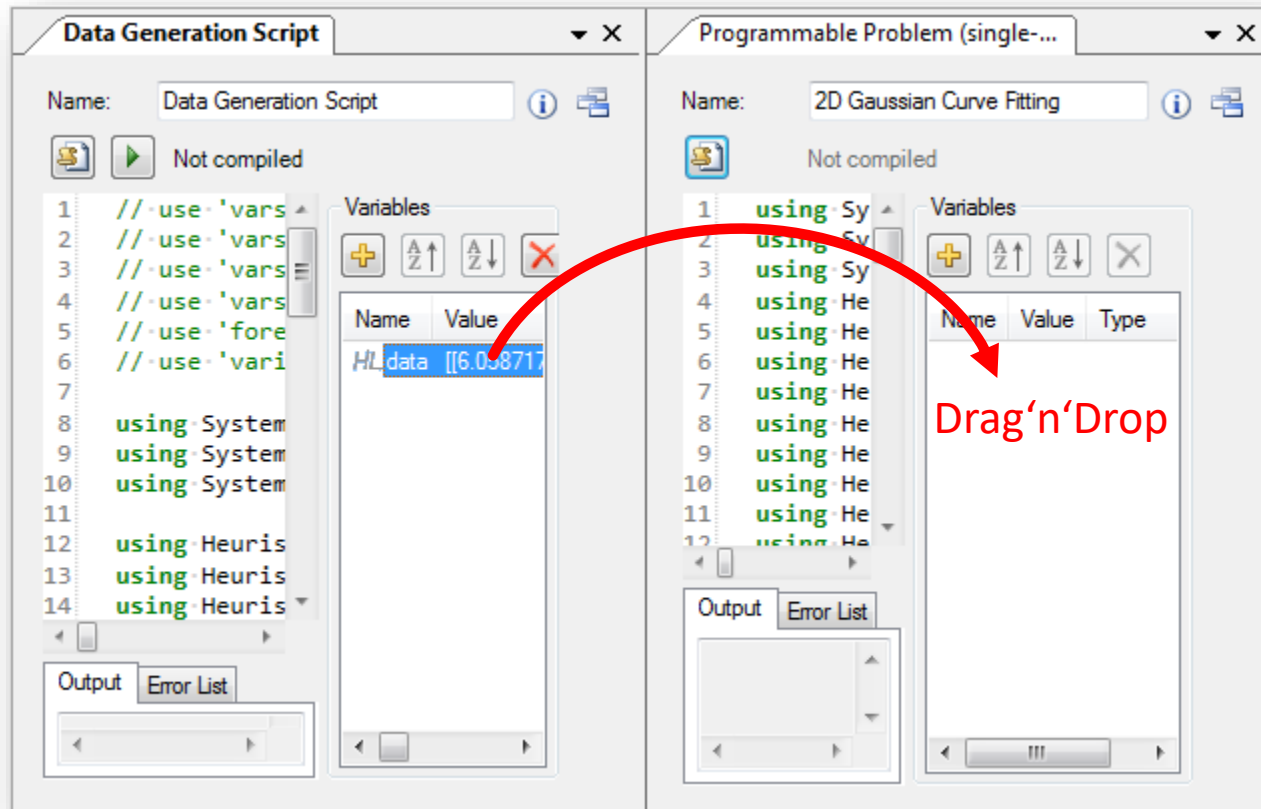
# Non-linear Curve Fitting

- Create a new single-objective programmable problem
- Drag'n'drop the data from the script onto the problem's VariableStore
- Code the problem definition
- Compile the problem





# Non-linear Curve Fitting



# Non-linear Curve Fitting

```
public bool Maximization { get { return false; } }

public override void Initialize() {
    Encoding = new RealVectorEncoding("r", length: 5, min: 0.0, max: 10.0);
}

public double Evaluate(Individual individual, IRandom random) {
    var vec = individual.RealVector("r");
    var mu = new double[] { vec[0], vec[1] };
    var cov = new double[,] { { vec[2], vec[3] }, { vec[3], vec[4] } };
    var invCov = GetInverse(cov);

    var data = (DoubleMatrix)vars.data;
    var quality = 0.0;
    for (var i = 0; i < data.Rows; i++) {
        var estimated = TwoDGauss(data[i, 0], data[i, 1], mu, cov, invCov);
        if (double.IsNaN(estimated) || double.IsInfinity(estimated)) quality += 1000;
        else quality += (estimated - data[i, 2]) * (estimated - data[i, 2]);
    }
    return quality / data.Rows;
}

private double TwoDGauss(double x, double y, double[] mu, double[,] cov, double[,] invCov) {
    var a = x - mu[0];
    var b = y - mu[1];
    return 1.0 / (2.0 * Math.PI * Math.Sqrt(GetDeterminant(cov)))
        * Math.Exp(-0.5 * ((a * invCov[0, 0] + b * invCov[1, 0]) * a + (a * invCov[0, 1] + b * invCov[1, 1]) * b));
}

private double[,] GetInverse(double[,] m) {
    var det = GetDeterminant(m);
    return new double[,] { { m[1, 1] / det, -m[0, 1] / det }, { -m[1, 0] / det, m[0, 0] / det } };
}

private double GetDeterminant(double[,] m) {
    return m[0, 0] * m[1, 1] - m[0, 1] * m[1, 0];
}
```

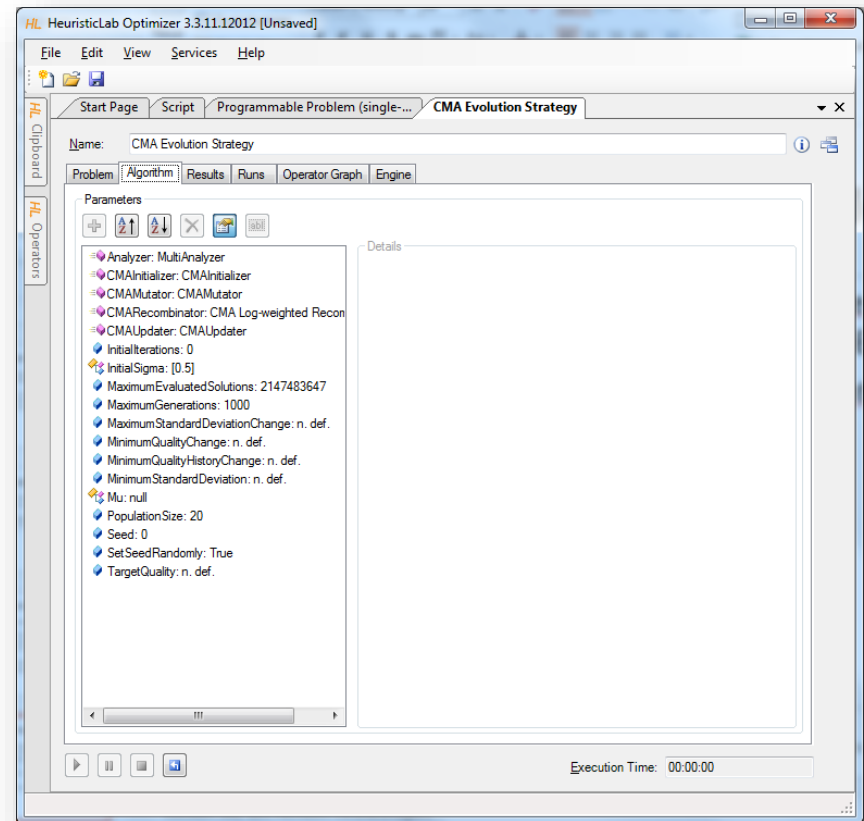
# Non-linear Curve Fitting

- Note that in the evaluation function we took care of degenerate cases
- If the estimation of the model is not a double number or infinity, an arbitrary, but high number is returned as a goodness of fit

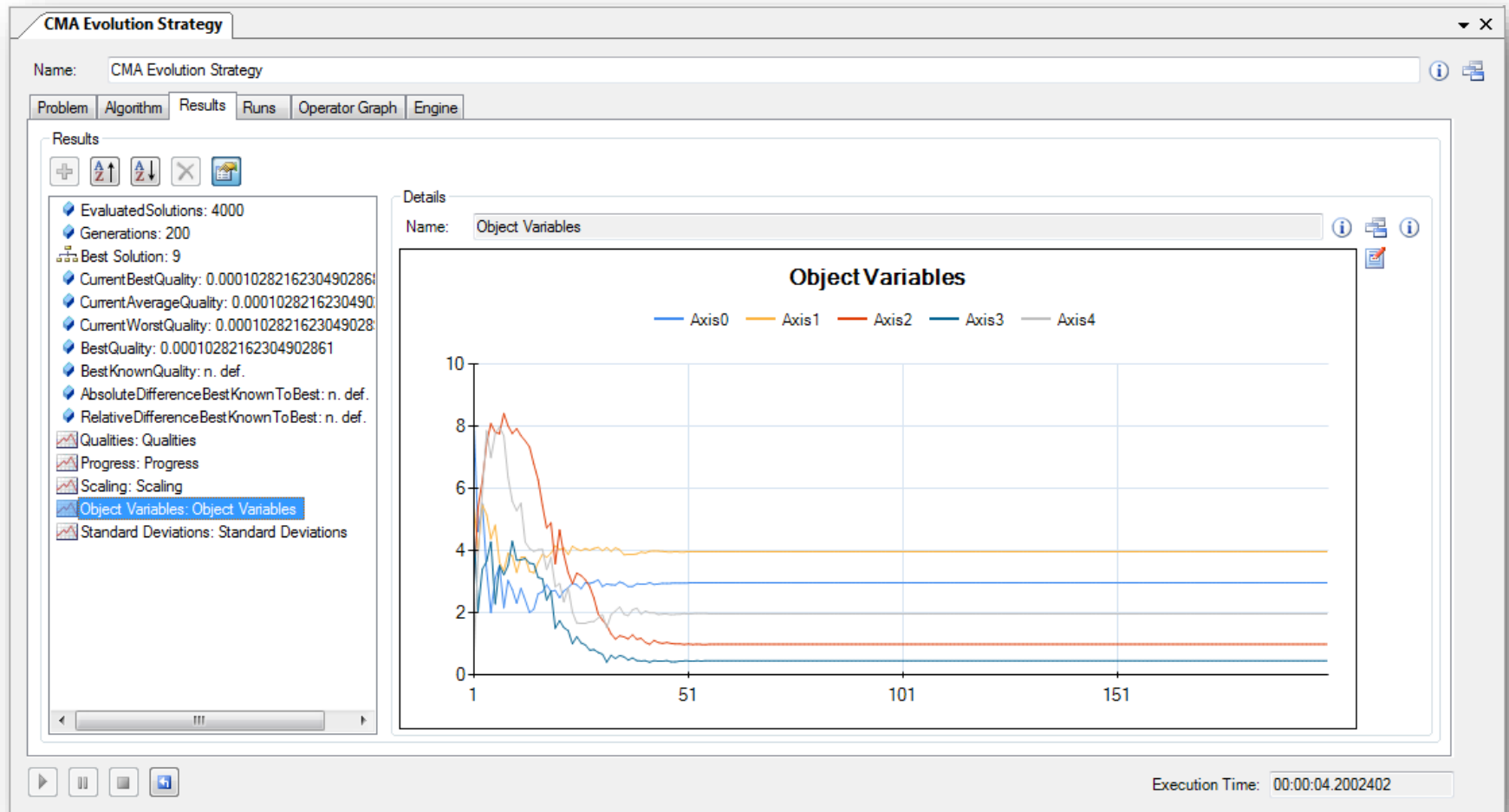
```
for (var i = 0; i < data.Rows; i++) {  
    var estimated = TwoDGauss(data[i, 0], data[i, 1], mu, cov, invCov);  
    if (double.IsNaN(estimated) || double.IsInfinity(estimated)) quality += 1000;  
    else quality += (estimated - data[i, 2]) * (estimated - data[i, 2]);  
}
```

# Non-linear Curve Fitting

- Create a new suitable algorithm, e.g. CMA-ES
- Drop the problem onto the algorithm
- Set the algorithm parameters
  - MaximumGenerations: 200
  - InitialSigma: 5
- Run the algorithm



# Non-linear Curve Fitting



# Agenda

- Objectives of the Tutorial
- Introduction
- Where to get HeuristicLab?
- Plugin Infrastructure
- Graphical User Interface
- Available Algorithms & Problems
  
- **Demonstration Part I: External Evaluation Problem**
- **Demonstration Part II: MATLAB and Scilab Parameter Optimization Problem**
- **Demonstration Part III: Programmable Problem**
  
- Some Additional Features
- Planned Features
- Team
- Suggested Readings
- Bibliography
- Questions & Answers

# Some Additional Features

- HeuristicLab Hive
  - parallel and distributed execution of algorithms and experiments on many computers in a network
- Optimization Knowledge Base (OKB)
  - database to store algorithms, problems, parameters and results
  - open to the public
  - open for other frameworks
  - analyze and store characteristics of problem instances and problem classes
- Parameter grid tests and meta-optimization
  - automatically create experiments to test large ranges of parameters
  - apply heuristic optimization algorithms to find optimal parameter settings for heuristic optimization algorithms
- Statistics
  - statistical tests and automated statistical analysis



# Planned Features

- Algorithms & Problems
  - steady-state genetic algorithm
  - unified tabu search for vehicle routing
  - estimation of distribution algorithms
  - evolution of arbitrary code (controller, etc.)
  - ...
- Cloud Computing
  - port HeuristicLab Hive to Windows Azure
- Have a look at the HeuristicLab roadmap
  - <http://dev.heuristiclab.com/trac.fcgi/roadmap>
- Any other ideas, requests or recommendations?
  - join our HeuristicLab Google group [heuristiclab@googlegroups.com](mailto:heuristiclab@googlegroups.com)
  - write an e-mail to [support@heuristiclab.com](mailto:support@heuristiclab.com)



# HeuristicLab Team



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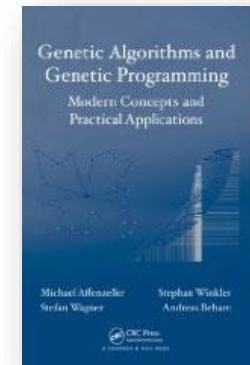
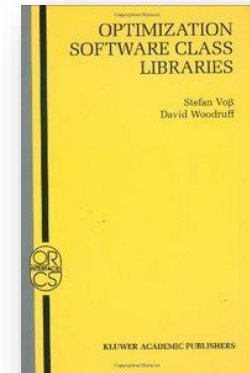
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# Suggested Readings

- S. Voß, D. Woodruff (Edts.)  
**Optimization Software Class Libraries**  
Kluwer Academic Publishers, 2002
- M. Affenzeller, S. Winkler, S. Wagner, A. Beham  
**Genetic Algorithms and Genetic Programming**  
**Modern Concepts and Practical Applications**  
CRC Press, 2009



# Bibliography

- S. Wagner, M. Affenzeller  
**HeuristicLab: A generic and extensible optimization environment**  
Adaptive and Natural Computing Algorithms, pp. 538-541  
Springer, 2005
- S. Wagner, S. Winkler, R. Braune, G. Kronberger, A. Beham, M. Affenzeller  
**Benefits of plugin-based heuristic optimization software systems**  
Computer Aided Systems Theory - EUROCAST 2007, Lecture Notes in Computer Science, vol. 4739, pp. 747-754  
Springer, 2007
- S. Wagner, G. Kronberger, A. Beham, S. Winkler, M. Affenzeller  
**Modeling of heuristic optimization algorithms**  
Proceedings of the 20th European Modeling and Simulation Symposium, pp. 106-111  
DIPTEM University of Genova, 2008
- S. Wagner, G. Kronberger, A. Beham, S. Winkler, M. Affenzeller  
**Model driven rapid prototyping of heuristic optimization algorithms**  
Computer Aided Systems Theory - EUROCAST 2009, Lecture Notes in Computer Science, vol. 5717, pp. 729-736  
Springer, 2009
- S. Wagner  
**Heuristic optimization software systems - Modeling of heuristic optimization algorithms in the HeuristicLab software environment**  
Ph.D. thesis, Johannes Kepler University Linz, Austria, 2009.
- S. Wagner, A. Beham, G. Kronberger, M. Kommenda, E. Pitzer, M. Kofler, S. Vonolfen, S. Winkler, V. Dorfer, M. Affenzeller  
**HeuristicLab 3.3: A unified approach to metaheuristic optimization**  
Actas del séptimo congreso español sobre Metaheurísticas, Algoritmos Evolutivos y Bioinspirados (MAEB'2010), 2010
- S. Wagner, G. Kronberger, A. Beham, M. Kommenda, A. Scheibenpflug, E. Pitzer, S. Vonolfen, M. Kofler, S. Winkler, V. Dorfer, M. Affenzeller  
**Architecture and Design of the HeuristicLab Optimization Environment**  
Advanced Methods and Applications in Computational Intelligence, vol. 6, pp. 197-261, Springer, 2014
- Detailed list of all publications of the HEAL research group: <http://research.fh-ooe.at/de/orgunit/356#showpublications>

# Questions & Answers



<http://dev.heuristiclab.com>

[heuristiclab@googlegroups.com](mailto:heuristiclab@googlegroups.com)

<http://www.youtube.com/heuristiclab>

<http://www.facebook.com/heuristiclab>